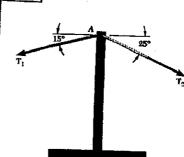


GIVEN: COMPONENT OF 200-N FORCE ALONG 6-6" MUST BE 120 N. DETERMINE BY TRIGONOMETRY (a) ANGLE & (b) COMPONENT

ALONG a-a'.



GIVEN: RESULTANT R OF I, AND I MUST BE VERTICAL AND Tz = 1000 lb. FIND (a) T, : (b) R

F= 200N

(a) USING TRIANGLE RULE AND LAW OF SINES! sin a _ sin 450 120 H _ Z00 H Sin 0 = 0.41426

X = 25.1°

(b) B=180-45°+25.1° = 109.9°

LAW OF SINES; Fac. = ZOO N Sin 45°

Faa, = (200 N) Sin 109, 9° sin 45°

F = 266 N

T_= IDDO ID

2.8

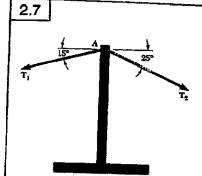
TRIANGLE RULE AND LAW OF SINES! $= \frac{10001b}{\sin 75^{\circ}} = \frac{R}{\sin 40^{\circ}}$

(a) SOLVING FOR T,:

T, = (1000 16) 3165 = 938.28 16, T = 938 16

(b) SOLVING FOR R:

R=(1000 16) \$\frac{\sin 40^\circ}{\sin 75^\circ} = 665.46 \begin{array}{c} R = 665 \begin{array}{c} B \end{array}



GIVEN: RESULTANT R OF T AND T MUST BE VERTICAL AND T, = 800 16

FIND: (a) T_2

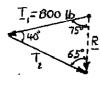
(b) R

2.9

GIVEN: RESULTANT R OF THE TWO FORCES MUST BE HORIZONTAL AND P= 35 N. FIND:

(a) ANGLE of (J) R

TRIANGLE RULE AND LAW OF SINES ;



 $\frac{T_1}{\sin 65^\circ} = \frac{T_2}{\sin 75^\circ} = \frac{R}{\sin 40^\circ}$ $\frac{8001b}{\sin 65} = \frac{7}{5 \sin 75} = \frac{R}{\sin 90}$

(a) SOLVING FOR Tz:

 $T_2 = (800 \text{ B}) \frac{\sin 75^\circ}{\sin 65^\circ} = 852.6 \text{ 16}$

T = B53 b

(6) SOLVING FOR R:

R = (B001b) \frac{\sin 40^\circ}{\sin.65^\circ} = 567,4 1b

R=567 16

TRIANGLE RULE:

P=35N 50 N (a) LAW OF SINES! Sin a = Sin 25"

Since = 50 N Sin 25°

SIN Q = 0.60374 , & = 37.140

Q = 37.1°

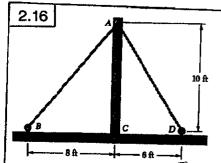
(b) B = 180°-25°-37.14° = 117.86°

LAW OF SINES!

 $\frac{R}{Sin B} = \frac{35N}{sin 25^{h}}$

 $R = (35N) \frac{\sin 117.86^{\circ}}{5in 25^{\circ}} = 73.218 N$

R=73,2 N



GIVEN:

TAB = 120 Ib

TAD = 40 Ib

FIND:

RESULTANT R

OF THE PORCES

EXERTED AT A

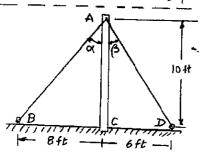
BY AB AND AD

 $\tan \alpha = \frac{9}{10}$

 $tan / 5 = \frac{6}{10}$

x = 38.66°

B = 30.96°



FROM FORCE TRIANGLE:

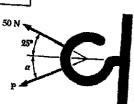
 $T_{AB} = 120 \text{ kg}$ |x| |x|

LAW OF COSINES: $R^{L}=(120)^{2}+(40)^{2}-1$ (120)(40) cos 110.38⁴ = 14,400 + 1600 - 9600 (-0.34824) $R^{2}=19,343$ R=139.09 |6 LAW OF SINES

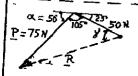
 $\frac{3 \cdot 10^{\circ} - \alpha - \beta}{40 \cdot 10} = \frac{\sin 8}{137.00 \cdot 10}$ $\frac{\sin 8}{40 \cdot 10} = \frac{\sin 10.38^{\circ}}{137.00 \cdot 10}$ $\frac{\sin 8}{40 \cdot 10} = \frac{15.64^{\circ}}{137.00 \cdot 10}$ $\frac{\cos 8}{40 \cdot 10} = \frac{15.64^{\circ}}{137.00 \cdot 10}$ $\frac{\cos 8}{40 \cdot 10} = \frac{15.64^{\circ}}{137.00 \cdot 10}$

R= 139,1167 67.0°

2.17



GIVEN:
P = 75 H , Q = 50°
FIND:
RESULTANT R OF
THE TWO FORCES
SHOWN.

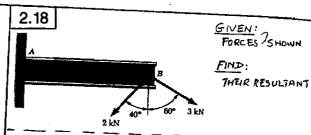


FROM FURCE TRIANGLE: LAW OF COSINES: R2=(75)2+(50)-2(15)(50) (06105° = 5625+ 2500-7500(-025082) R2=10066 R=100.33 N

LAW OF SINES: $\frac{\sin \delta}{75N} = \frac{\sin 105^{\circ}}{100,33N}$ $\sin \delta = 0.72206 \quad \delta = 46.22^{\circ}$

R = 8 - 25° = 46.22-25 = 21.22°

R = 100.3 N. 721.2°



2ky 74 46 B 80 R 60° 3kN FROM FURCE TRIANGLE:
LAW OF COSINES!

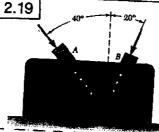
R2 = (2) + (3) - 2(2)(3) cos By

R4 = 10,716 R = 3.304 KN

LAW OF SINES!

Sin 8 = Sin 80 Y = 36.59°

 $\beta = 180^{\circ} - (80^{\circ} + 36.59^{\circ}) = 63.41^{\circ}$ $\phi = 180^{\circ} - (\beta + 50^{\circ}) = 66.59^{\circ}$ $R = 3.30 \text{ kM} \subseteq 66.6^{\circ}$



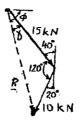
GIVEN:

FA = 15 kM

FB = 10 kM

FIND:

RESULTANT OF FORCES
EXERTED ON BRACKET
BY MEMBERS A AND B.

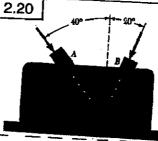


FROM FORCE TRIANGLE:

LAW OF COSINES: $R^2 = (15)^2 + (10)^2 - 2(15)(10) \cos 120^2$ $R^2 = 475$ R = 21.794LAW OF SINES:

Sind = $\frac{\sin 120^\circ}{21.794 \text{kN}}$ $\phi = 50^\circ + \gamma = 50^\circ + 23.41^\circ - 73.41^\circ$

R = 21.8 KN 5 73,40



GIVEN:

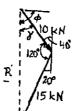
FA = 10 kN

FB = 15 kN

FIND:

RESULTANT OF FA

RESULTANT OF FORCES
EXERTED ON BRACKET
BY MEMBERS A AND B.



FROM FORCE TRIANGLE:

LAW OF COSINES:

R^2 = (10)^2 + (15)^2 - 2(10)(15) cos 120

R^2 = 475

R = 21.794 kN

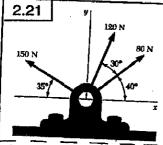
LAW OF SINES:

Sin 8 = Sin 120

15 kN = 21.794kN

8 = 36.59°

 $\frac{\sin \delta}{15 \text{ kN}} = \frac{\sin 120}{21,794 \text{ kN}} \qquad \delta = 36.59^{\circ}$ $\phi = 50^{\circ} + \delta = 50^{\circ} + 36.59^{\circ} = 86.59^{\circ}$ $R = 21.8 \text{ kN} = 86.6^{\circ}$



GIVEN: MAGNITUDES AND DIRECTIONS OF FORCES

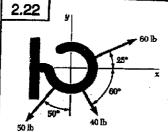
FIND:

2 AND Y COMPONENTS OF THE FORCES.

80-N FORCE: F=+ (80N) cos 40 覧=+ 61.3 N $F_3 = +(80 \text{ N}) \sin 40^\circ$, 元 = + 51.4N

170-N FORCE: F=+(120N)cos 70" F_=+ 41.0N Fr = +(120H) Sin70, Fy =+ 1128N

Fz=- (150N) cos 35, F =- 122.9N F. = + (150N)sin35, Fy =+ 86,0 N



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GIVEN!

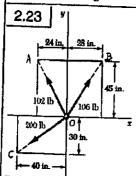
MAGNITUDES AND DIRECTIONS OF FORCES

X AND Y COMPONENTS OF THE FORCES.

40-16 PORCE: F=+(40/6) Cos60=+20,00/6, F=+20,016 F = - (4014) sin 60 = -34.64 14 F = -34.616

50-16 FORCE: F =- (50%) Sin 50 =-38.30%, F =-38.316 F= - (5016) cos 50 = - 32.1416, F= - 32.116

60-16 FORCE: F2=+(6016)cos 25°=+54.38 14 F2=+54.4 16 =+ (60b)sin25"=+25.34 16, F=+25,416 €



GIVEN: FORCES AND DIMENSIONS SHOWN. <u>FI</u>ND: X AND 4 COMPONENTS OF FORCES

WE COMPUTE THE FOLLOWING DISTANCES:

OA = V(24)2+(45)2 = 51 in.

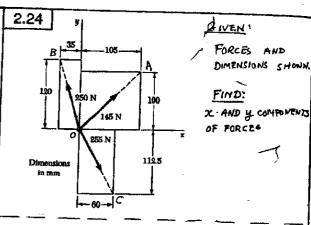
 $OB = \sqrt{(28)^2 + (45)^2} = 53 \text{ in.}$ $0 = \sqrt{(40)^2 + (30)^2} = 50 \text{ in.}$

102-16 FORCE: F = - (102 16) 24 F,=- 48.016 Fg =+(102/b) 45 Fy =+ 90.0 16

106-15 FORCE: F2 =+ (106 16) 28 F, = + 56.0 lb FH = +(10611) # Fy = + 90.0 1b

200-16 FORCE: F =- (200 16) 40 F = - 160.0 16

F=- (2001) 30 F = - 120.0 16



145 -N FORCE: $OA = \sqrt{(105)^2 + (100)^2} = 145 \, \text{mm}$ Fz = + (145 N) 105 MM F= + 1050 N

Fy = + (145N) 100 mm

F = + 100.0N

250-N FORCE: OB=V(35)2+(120)2 = 125 mm F = - (250 N) 35 mm F =- 70,0 N

Fy = + (250 N) 120 mm

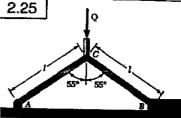
F, = + 240 N

255-N FORCE: OC=V(60)2+(112.5)2 =127.5 mm F =+ (255N) 60 mm F, = +120.0 N

F = - (255N) 112,5mm

127.5 mm

F = --225 N



GIVEN: (1) CB EXERTS FORCE PON B ALONG CB (2) HORIZONTAL COMPONENT OF P

15 Px = 1200 N. FIND:

(a) MAGNITUDE P (b) VERT. COMP. P.

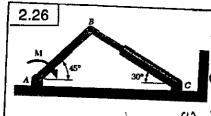


(a) P_k = P sin 55° $P = \frac{P_x}{\sin 55^\circ} = \frac{1200 \, N}{\sin 55^\circ} = 1464.9 \, N$

P=1465 N

(b) $P_x = P_y \tan 55^\circ$ $P_y = \frac{P_x}{\tan 55^\circ} = \frac{1200 \,\text{N}}{\tan 55^\circ} = 840.2 \,\text{N}$

P = 840 N+



GIVEN:

(1) FORCE P EXERTED

BY BC ON AB IS

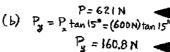
DIRECTED ALONG BC.

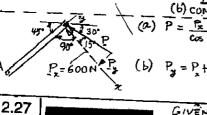
(2) COMPONENT OF P

(2) component of P LAB 15 GOON FIND: (a) P

(b) comp. of P Along AB
P = 1x = 600 N

cos 15" = 500 N





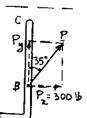
GIVEN:

(1) FORCE P EXERTED
BY 8D ON ABC 15
DIRECTED ALONG BD.

(2) HORIZ. COMPONENT
OF P 15 Px = 300 lb.

FIND:

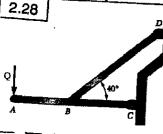
(a) MAGNITUDE P



(a) $P = \frac{P_2}{\sin 35^\circ} = \frac{300 \text{ lb}}{\sin 35^\circ}$ P = 523 lb

(b)
$$P_y = \frac{P_z}{\tan 35^\circ} = \frac{300 \text{ lb}}{\tan 35^\circ}$$

Py = 428 16



GIVEN:

(1) FORCE P EXERTED

BY BD ON ABC IS

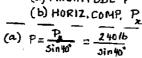
DIRECTED ALONG BD

(2) VERT. COMPONENT

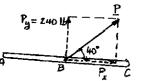
OF P IS P = 240 lb.

FIND:

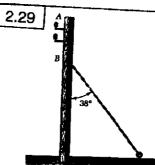
(A) MAGNITUDE P



P= 373 /b



(b) $P_2 = \frac{B}{\tan 40^\circ} = \frac{24016}{\tan 40^\circ}$



GIVEN:

(1) FORCE PEXERIED BY 2D

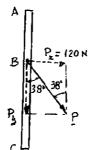
ON POLE IS DIRECTED ALONG BD.

(2) COMPONENT OF P 1 TO

AC 15 120 N.

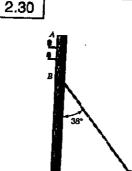
FIND:

FIND:
(a) MHG NITUDE P
(b) COMPONENT OF P
ALONG AC.



(a) $P = \frac{P_2}{\sin 38^\circ} = \frac{120 \text{ H}}{\sin 38^\circ} = 194.91 \text{ N}$ P = 194.9 N

(b) $P_y = \frac{P_z}{\tan 3\theta} = \frac{120 \text{ M}}{\tan 3\theta} = 153.59 \text{ N}$ $P_y = 153.6 \text{ N}$



GIVEN.

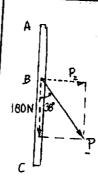
(I) FORCE PEXERTED BYBD ON POLE IS DIRECTED PLONE BD

(2) COMPONENT OF P ALDING

FIND:

(A) HAGNITUDE P

(6) COMPONENT OF P

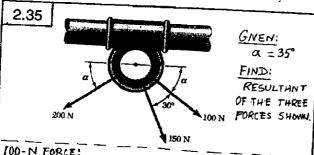


(a) $P = \frac{180N}{\cos 38^\circ} = 228.4 N$

P= 228 N

(b) $P_z = (180 \text{ N}) \tan 30^\circ = 140,63 \text{ N}$

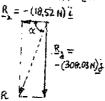
P= 140.6 N

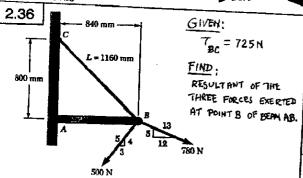




$$F_2 = -(200\text{ N})\cos 35^\circ = -163.03\text{ N}, \quad F_3 = -(200\text{ N})\sin 35^\circ = -114.72\text{ N}$$

FORCE	2 COMP. (N)	H COMP. (N)
100 N	+81.92	-57.36
150 N	+63,39	-135,95
200 N	-163,83	~114.72
	R =-18.52	R==-308,03



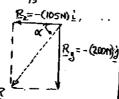


FORCE EXERTED BY CABLE BC:

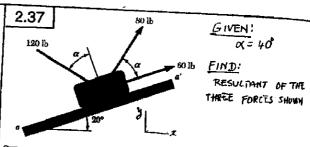
F=-(500N)書=-300N, F3 = - (500) 4 = - 400 H 780-N FORCE:

 $f_2 = + (780N) \frac{12}{13} = + 720N$ Fy =- (780N) 5 =- 300 N

FORCE	"X COMP. (N)	A COME (N)
TBE 725H	-525	+500
200 N	-300	- 400
780 N	+720	- 500
	Rx=-105	Ry = -200



$$\tan \alpha = \frac{200N}{105 N}$$
 $\alpha = 62.30^{\circ}$
 $R = \frac{200 N}{\sin 62.30^{\circ}} = 225.9 N$

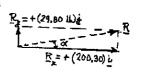


60-	Ь	FO	RCE	3
F,=+	(6	O IJ,) cos	20

Fz=+(80b)cos60°=+40.00 lb, Fy = +(80 16) sin 60 = + 69.28 16 120-16 FORCE!

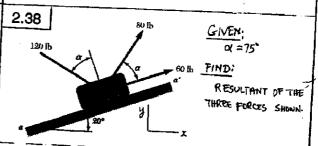
Fz =+ (1201b) cos 30 = + 103.92 lb, Fz = - (1201b) sin 30 = - 60,00 lb

FORCE	XCOMP (16)	A CONE (1P)
60 lb	+56.38	+20.52
8016	+40,00	+69,28
1201	+103,92	
	Rz=+200.30	



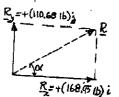
$$tan Q = \frac{29.80 \, lb}{200.50 \, lb} \qquad \alpha = 8.462^{\circ}$$

$$R = \frac{24.80 \, \text{b}}{\sin 8.46 \, \text{c}} = 202.51 \, \text{lb}$$
 $R = 203 \, \text{lb}$ & 8.46°



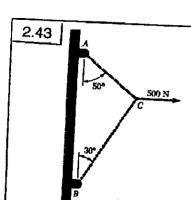
60-16 FORGE:

FORCE	X COMP. (IL)	y COMP. (W)
601P	+56.38	
80 lb	-6.97	+79.70
1201	+119.54	+10,46
	R=+168.95	Ry=+110.60



$$\tan \alpha = \frac{110.68 \, lb}{168.45 \, lb}$$
 $\alpha = 33.23$

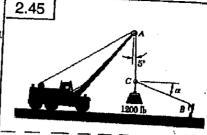
$$R = \frac{110.68 \text{ lb}}{5 \text{ in } 32.13^{\circ}} = 201.98 \text{ lb}$$



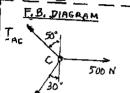
GIVEN: CABLES AC AND BC ARE LOADED AS SHOWN

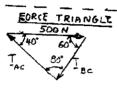
FIND; (a) TENSION IN AC.

(b) TENSION IN BC.



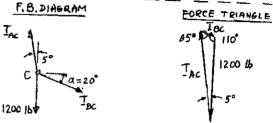
GIVEN; a = 20° FIND: TENSION IN (a) Ac (b) BC





(a)
$$T_{AC} = \frac{500 \text{ N}}{\sin 80^{\circ}} \sin 60^{\circ} = 439.7 \text{ N}$$

(b) $T_{BC} = \frac{500 \text{ N}}{\sin 80^{\circ}} \sin 40^{\circ} = 326.4 \text{ N}$

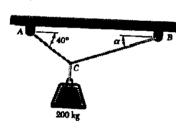


(a)
$$T_{AC} = \frac{1200 \text{ b}}{\sin 65^{\circ}} \sin 110^{\circ} = 1244,2 \text{ b}$$

1200 B

(b)
$$T_{BC} = \frac{1200 \, \text{B}}{3 \text{in 65}} \sin 5^\circ = 115,40 \, \text{B}$$

2.44



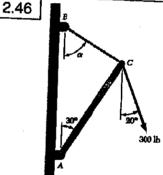
<u> GIVE</u>N (1) CABLES AC AND BC ARE LOADED AS SHOWN

FIND:

TENSION IN (a) AC

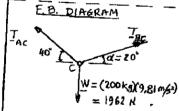
(b) BC

FORCE TRIANGLE



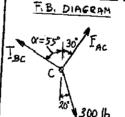
(1) $\alpha = 55$ °. (2) BOOM AC EXERTS ON PIN C A FORCE ALONG AC. FIND: (a) Fa (b) T_{BC}

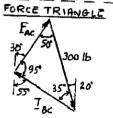
GIVEN:





LAW OF SINES! TAC = TBC = 1962H Sin60"

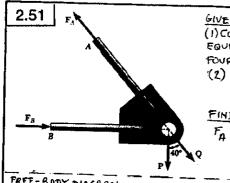




LAW OF SINES;

(a)
$$F_{AC} = \frac{300}{5in95}$$
, $\sin 95^{\circ} = 172.73$ | $F_{AC} = 172.7$ | $F_{AC} = 172.7$

(b)
$$T_{Bc} = \frac{3001b}{\sin 95}$$
 $\sin 50 = 230.7 /b$ $T_{Bc} = 231 lb$



GIVEN: (1) CONNECTION IN EQUILIBRIUM UNDER FOUR FORCES

(2) P= 500 1b Q= 650 B

FA AND FA

FREE-BODY DIAGRAM

RESOLVING THE FORCES INTO & AND & COMPONENTS!

- 4 FAsin 50'j -FACES 50 1 50) (650 16) 6550 4 - (650 lb)5in50] P= -(500 16);

R = FA+FA+P+Q=D

-FACOS 50 i + FASIN 50 d + FBi -500 j + 650 cos 50 i

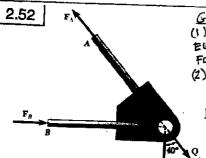
EQUATING TO ZERO THE COEFF. OF LAND :

(1) Fasin 50"-500 - 650 sin 50"= 0

FA= 1303 lb ◀

(1) -FA 00550" + FB +650 WS 50" = 0 FB = (1303 16) CUSSO" - (6500 CUSSO")

FR= 42016



GIVEN:

(1) CONVECTION IN EQUILIBRIUM UNDER FOUR FORCES (2) FA = 750 B

FB = 400 H

FIND! P AND Q

FREE-BODY DIAGRAM:

RESOLUNG THE FORCES INTO X AND & COMPONENTS

Fa=75014- 750 sin 50 j P=-Pj - 40 sin 50 à

R = P+ Q+FA+FB = 0 -Pi+ Qcosso i-Qsin 50 j - 750 cosso i+750 sin 50 j + 400i = 0

EQUATING TO ZERO THE COEFF OF & AND 2:

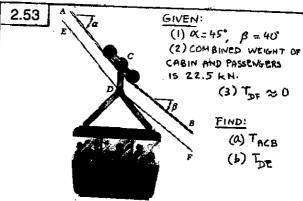
Q cosso - 750 cos 50 +400 = 0

Q=127,7 b

1 -P-Qsinso+750sinso=0

P=- (127.7 lb) sinso+ (750 B) sinso

P= 47716



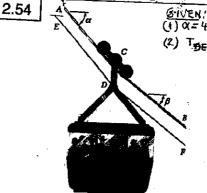
FREE-BODY DIAGRAM (CABIN CONSIDERED AS PARTICLE) TACE TACE COS 40 - T COS 45"- T COS 45"=0 0.05894 TACB - 0.7071 Te=0 (1) -TACOS in 40°+TACISIN 45°+T sin45° 22.5 LN ¥

0.06432 TACB + 0.7071T = \$2.5 (a) ADD (1) AND(2); 0.12326 TACB = 22.5 TACB = 182.54 KN TACB =182.5KN

(b) FROM (1): $T_{DE} = \frac{0.05B94}{0.7071}$ (182,54)

TDE = 15.22kH

NOTE: IN PROBS. 2.53 AND 2.54 THE CABIN IS CONSIDERED AS A PARTICLE. IF CONSIDERED AS A RIGID BODY (CHAR. 4) IT WOULD BE FOUND THAT ITS CENTER OF GRAVITY SHOULD BE LOCATED TO THE LEFT OF & FOR GD TO BE VERTICAL.



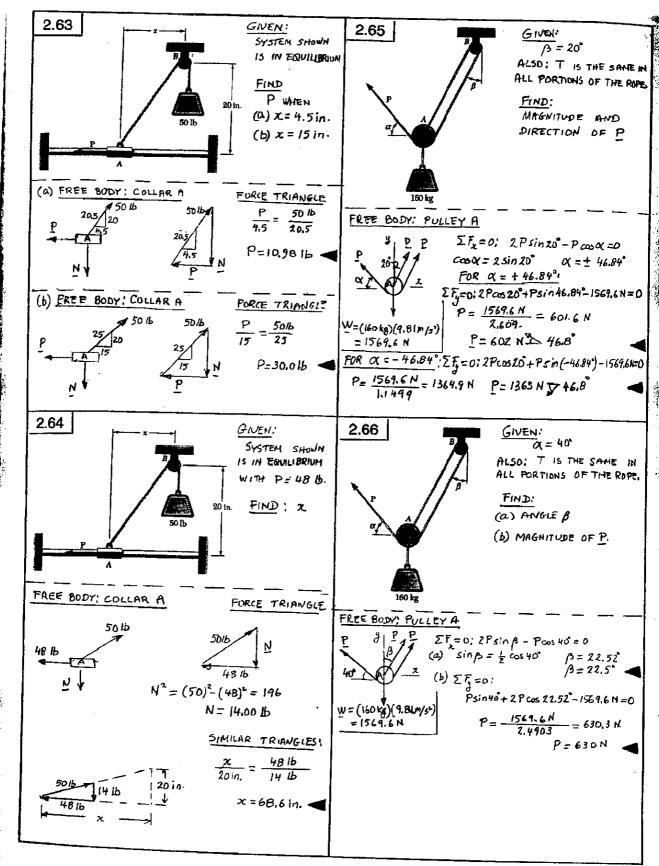
(1) \a=48°, \b=38' (2) TOE = 18 KN, TOF 20

> FIND! (a) combined WEIGHT OF CABIN PASSENGERS, AND SUPPORT SYSTEM (6) TACE

FREE-BODY DIAGRAM (CABIN CONSIDERED AS PARTICLE) TACO (b) ∑ Fx = 0: TACB COS 38-TACB COS 48-(18 km) COS 48-0 JA KN 4 0.1189 TACB - 12.044 KN = 0 4B*, (b) TACE=101,3 KN

(a) Efg=0; TACB sin 48-TACB sin 38+ (18 KM) sin 48-W=0 W= (101.3 kn)(sin 48"-sin 38")+(18 kH)sin 18" = 26.29 KN

(a) W = 26.3 KN



DING

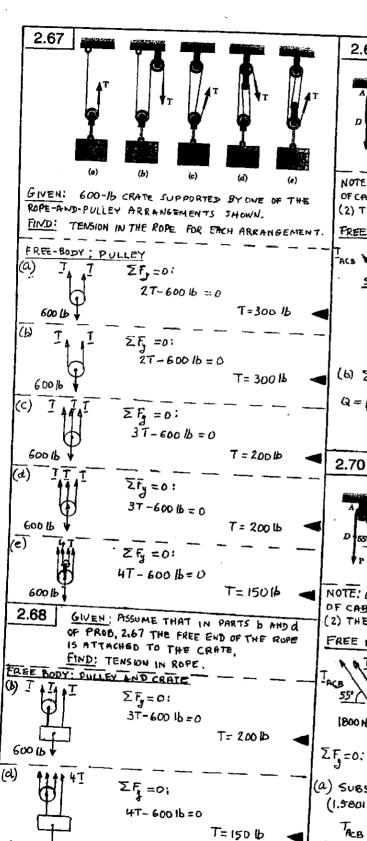
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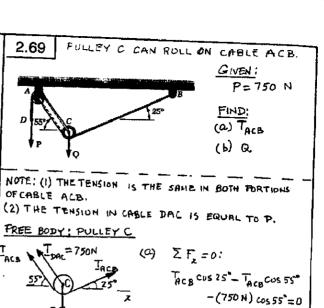
962

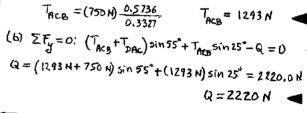
·H

E



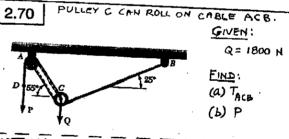
600 lb





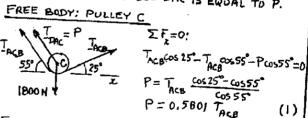
TACA (cos 15" - cos 55") = 750 cus 55"

(1)



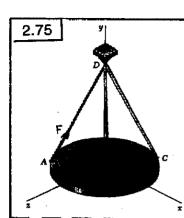
NOTE! (1) THE TENSION IS THE SAME IN BOTH PORTIONS OF CABLE ACB.

(2) THE TENSION IN CABLE DAC IS EQUAL TO P.



ΣF =0: (TACB + P) sin 55° + TACB sin 25° -/800 N=0 (a) SUBSTITUTE FOR P FROM (i) INTO (2); (1.5001 sin 55° + sin 25°) TACB = 1800 N

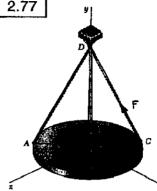
TACA = 1048,4 N TACB = 1048 N (b) CARRY INTO (1): P=0,5801 (1048.4N) P = 608 N -



GIVEN: (I) WIRES FORM 30 ANGLES WITH VERTICAL (2) FORCE EXERTED BY AD ON PLATE HAS COMPONENT F= 110,3N

FIND: (a) TENSION IN AD

(b) ANGLES Ox, O, Oz THAT FORCE EXERTED AT A FORMS WITH THE COORDINATE AXES.



GIVEN: (I) WIRES FORM 30 ANGLES WITH VERTICAL (2) TENSION IN CD 15 60 lb.

FIND: (a) COMPONENTS OF FORCE EXERTED AT C. (b) ANGLES 0, 0, 02 THAT FORCE FORMS WITH THE COORSINATE

(a)
$$F_x = F \sin 30^{\circ} \sin 50^{\circ} = 110.3 \text{ N}$$
 (GIVEN)
$$F = \frac{110.3 \text{ N}}{\sin 30^{\circ} \sin 50^{\circ}} = 207.97 \text{ N} \qquad F = 208 \text{ N}$$

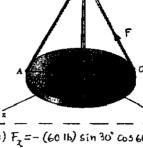
(b)
$$\cos \theta_{\lambda} = \frac{F_{x}}{F} = \frac{110.3 \text{ N}}{207.47 \text{ N}} = 0.3830 \quad \theta_{\lambda} = 67.5$$

$$F_y = F\cos 30^\circ$$
, $\cos \theta_0 = \frac{F_2}{F} = \cos 30^\circ$. Thus: $\theta_0 = 30.0^\circ$ (b) $\cos \theta_{\chi} = \frac{F_{\chi}}{F} = \frac{-15.00 \, \text{lb}}{60 \, \text{lb}} = -0.2500$, $\theta_{\chi} = 104.5^\circ$

$$F_2 = -F \sin 30^{\circ} \cos 50^{\circ}$$

= - (287.97 N) sin 30° cos 50° = -92.552 N
 $\cos \theta_2 = \frac{F_2}{F} = \frac{-92.552 \text{ N}}{287.97\text{N}} = -0.3214$

B, = 108.7°



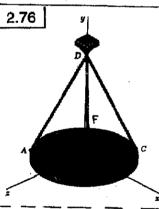
(a) F₂ =- (60 lb) sin 30° cos 60° F, = -15,00/b + Fy = (60 16) cos 30" = 51.96 /b Fy=+52.016 -F = (60 b) sin 30 sin 60 = 25.98 lb F2 = + 26,016 -

(b)
$$\cos \theta_x = \frac{F_x}{F} = \frac{-15.001b}{601b} = -0.2500, \quad \theta_x = 104.5^{\circ}$$

$$\cos \theta_y = \frac{F_y}{F} = \frac{+51.96 \text{ lb}}{60 \text{ lb}} = 0.8660, \quad \theta_y = 30.0^{\circ}$$

$$\cos \theta_2 = \frac{F_2}{F} = \frac{+25.981b}{601b} = 0.9330$$
 $\theta_2 = 64.3^b$

NOTE: VALUE OBTAINED FOR BY CHECKS WITH GIVEN DATA.

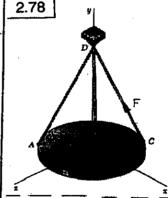


GIVEN:

(I) WIRES FORM 30" ANGLES WITH VERTICAL (2) FORCE EXERTED BY BD ON PLATE HAS COMPONENT F = -32,14N.

FIND:

(a) TENSION IN BD (b) ANGLES Ox, 07, 02 THAT FORCE EXERTED AT B FURMS WITH THE COURDINATE AXES.



GIVEN: (1) WIRES FORH 30 ANGLES WITH VERTICAL. (2) FORCE EXERTED BY CD UN PLATE HAS

COMPONENT F=-20,016 FIND:

(a) TENSION IN CD. (b) ANGLES BZIBY, B. THAT FORCE EXERTED AT C PORMS WITH THE COURDINATE AXES.

(a)
$$F_2 = -F \sin 30^{\circ}\cos 40^{\circ} = -32.14 \text{ N}$$
 (GIVEN)
$$F = \frac{32.14 \text{ N}}{\sin 30^{\circ} \sin 40^{\circ}} = 100.0 \text{ N} \qquad F = 100.0 \text{ N}$$

$$\cos \theta_{x} = \frac{F_{x}}{F} = \frac{-38.30 \text{ N}}{100.0 \text{ N}} = -0.3830$$
 $\theta_{x} = 112.5^{\circ}$

$$F_y = F\cos 30$$
, $\cos \theta_y = \frac{F_z}{F} = \cos 30$, Thus: $\theta_y = 30.0^{\circ}$
 $\cos \theta_z = \frac{F_z}{F} = \frac{-32.14 \,\text{N}}{100.0 \,\text{N}} = -0.3214$ $\theta_z = 108.7^{\circ}$

(a) F =- F sin 30 cos 60° =- 20,0 lb (GIVEN)

$$F = \frac{20.0 \, lb}{\sin 30^{\circ} \cos 60^{\circ}} = 80.0 \, lb$$
 $F = 80.0 \, lb$

(b)
$$\cos \theta_x = \frac{F_x}{F} = \frac{-20.01b}{80.01b} = -0.2500$$
 $\theta_x = 104.5^\circ$

$$F_y = F\cos 30$$
, $\cos \theta_y = \frac{F_x}{F} = \cos 30$. Thus: $\theta_y = 30.0^\circ$

$$\cos \theta_2 = \frac{F_2}{F} = \frac{34.641 \text{ lb}}{80.0 \text{ lb}} = 0.4330$$
 $\theta_2 = 64$,

2.79 GIVEN: F=(260N)i-(320N)j-	+(800H) <u>k</u>
FIND: MAGNITUDE AND DIREC	TION OF F
$F = \sqrt{F_{x}^{2} + F_{y}^{2} + F_{x}^{2}} = \sqrt{(260)^{2} + (320)^{2} + (80)^{2}}$	0)2, F=900N'
$\cos \theta_2 = \frac{F_z}{F} = \frac{260 \text{ N}}{900 \text{ N}} = 0.2889$	$\theta_{x} = 73.2^{\circ} \blacktriangleleft$
$\cos \theta = \frac{F_0}{F} = \frac{-320N}{900N} = -0.3556$	gy=110.8° ◀
$\cos \theta_2 = \frac{F_2}{F} - \frac{BOON}{9000} = 0.8889$	$\theta_2 = 27.3^{\circ} \blacktriangleleft$
2.80 GIVEN: F=(320 N)L +(400 H)	-(250N) <u>k</u>
FIND: MAGNITUDE AND DIREC	TION OFF,
$F = \sqrt{F_x^2 + F_y^2 + F_z^2} = \sqrt{(320)^2 + (400)^2 + (250)^2}$, F=570N
$\cos \theta_2 = \frac{F_2}{F} = \frac{320 \text{ N}}{570 \text{ N}} = 0.5614$	$\theta_z = 55.8$
$\cos \theta_{y} = \frac{F_{y}}{F} = \frac{400N}{570N} = 0.7018$	$\theta_y = 45.4^{\circ}$
$\cos \theta_{k} = \frac{F_{2}}{F} = \frac{-250 \text{N}}{570 \text{N}} = -0.4386$	θ ₂ =116,0° ◀
2.81 GIVEN: FORCE WITH \$ = 69 AND F3 = -174.0 6	1.3°, 0 ₂ =57.9°
FIND: (a) By, (b) Fx, F2, AND F.	•
(a) TO DETERMINE BY WE USE THE	RELATION
$\cos^2 \theta_x + \cos^2 \theta_y + \cos^2 \theta_z = 1$ $\cos^2 \theta_z = 1$	- Cos ez - cus ez
SINCE Fy <0, WE MUST HAVE COSO,	<0, THUS!
$\cos \theta_1 = -\sqrt{1-\cos^2 69.3^{\circ}-\cos^2 57.9^{\circ}} = -0.76$	99, θ ₄ =140,3° ◀
(b) $F = \frac{F_8}{c_0 + c_0} = \frac{-174.0 \cdot 1b}{-0.7699} = 226.0 \cdot 1b$	F= 226 /b -
Fx = Fcos 0x = (226.0 16) cos 69.3°	F = 79.9 16
F2 = Fcos 8 = (226.0 16) cos 57.9°	F=12011b
2.82 GIVEN: FORCE WITH &= 70. AND F =- 52,0 Ib	9°, 0,=144,9°
FIND: (a) 0, (b) F, Fy, AND F.	
(a) TO DETERMINE & WE USE THE RE	LATION
(03 th + 03 th + cos to =), cos to = 1-c	osto _z – costo _d
SINCE F <0, WE MUST HAVE COS 02	
cos 02= -VI- cos 70,90- cos 144.90= -0,4728	, θ ₂ =118,2° -
(b) $F = \frac{F_a}{\cos q} = \frac{-52.0 \text{ lb}}{-0.4728} = 110.0 \text{ lb}$	F=11016 -
Fz= Fcos 0x = (110.0 16) cos 70.9"	F _x = 36.0 lb ◀
Fy = Fosey = (110.0 16) cos 144.9°	Fy=-90.016 ◀
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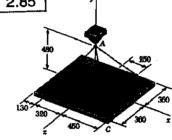
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2.83	GIVEN: F= 230N, 0,= 32.	5°, F=-60N, F=>0
	FIND (a) Fx AND Fz, (b) &	S AND θa
(a) F ₂ =	Fcos 0 = (230 N) cos 32,5°	Fz=194.0N
F1= F2+	F1+F2: (230 N)= (194.0N)2	t(-60n)3+72
$F_2 = +\sqrt{(2)}$	30)-(141)-(60)	F =+108.0 N
(b) cos 8	=Fy/F=-60/230=-0.2609	B=1021, ◀
cos to	= F2/F= 108/230 = +0,4696	$\theta_{\bullet} = 62.0^{\circ}$

FIND; (a) F_{a} AND F_{a} , (b) θ_{a} AND θ_{d} .

(a) $F_{a} = F \cos \theta_{a} = (210 \text{ N}) \cos 151.2^{\circ}$ $F_{a} = -184.0 \text{ N}$ $F^{2} = F_{a}^{2} + F_{a}^{2} + F_{a}^{2}$; $(210 \text{ N})^{2} = (80 \text{ N})^{2} + F_{d}^{2} + (-184.0 \text{ N})^{2}$ $F_{a} = -\sqrt{(210)^{2} - (80)^{2} - (184.0)^{2}}$ $F_{a} = -67.6^{\circ}$

GIVEN: F=210N, F= 80N, 0, =1562, F4 <0



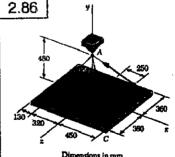
TENSION IN CABLE
AB IS 408 N.

FIND:

COMPONENTS OF
FORCE EXERTED ON

PLATE AT B.

 $\begin{array}{ll}
BA = 320i + 480j - 360k & BA = \sqrt{(320)^2 + (480)^2 + (360)^2} = 680 \\
F = FA = FBA = \frac{408 \text{ N}}{680 \text{ mm}} [(320\text{mm})i + (480\text{ mm})j - (360\text{mm})k] \\
F = (192 \text{ N})i + (288 \text{ N})j - (216 \text{ N})k \\
F = + 192 \text{ N}, F = + 288 \text{ N}, F = -216 \text{ N}
\end{array}$



GIVEN: TENSION IN CABLE AD 15 429 N.

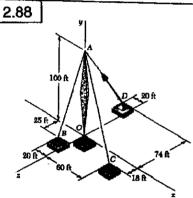
FIND: COMPONENTS OF PURCE EXERTED ON PLATE AT D.

2.87 20 ft 80 ft 74 ft 18 ft

GIVEN: TENSION IN WIRE AB 15 525 16.

FIND:

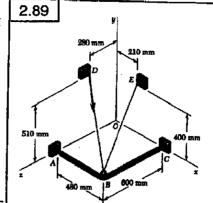
COMPONENTS OF
FORCE EXERTED
ON BOLT B BY
WIRE AB.



GIVEN: TENSION IN WIRE AD IS 315 lb.

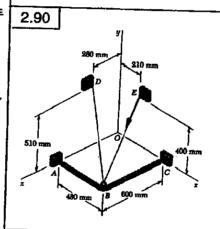
FIND:
COMPONENTS OF
FORCE EXERTED
ON BOLT D BY
WIRE AD.

 $\overrightarrow{DA} = (20 \text{ ft}) \cdot \underbrace{i}_{i} + (100 \text{ ft}) \cdot \underbrace{j}_{i} + (74 \text{ ft}) \cdot \underline{k}$ $DA = \sqrt{(20)^{2} + (100)^{2} + (74)^{2}} = 126 \text{ ft}$ $\overrightarrow{F} = F \partial_{DA} = F \cdot \frac{\overrightarrow{DA}}{DA} = \frac{3157b}{1267b} [(20 \text{ ft}) \cdot \underline{i} + (100 \text{ ft}) \cdot \underline{j} + (74 \text{ ft}) \cdot \underline{k}]$ $\overrightarrow{F} = (50 \text{ fb}) \cdot \underline{i}_{i} + (250 \text{ fb}) \cdot \underline{j}_{i} + (185 \text{ fb}) \cdot \underline{k}$ $F_{2} = +50 \text{ fb}, \quad F_{3} = +250 \text{ fb}, \quad F_{4} = +185 \text{ fb}$



GIVEN: TENSION IN CABLE DBE 15 385 N.

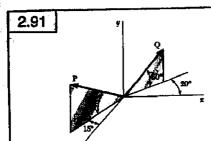
FIND:
COMPONENTS OF
FORCE EXERTED
BY CABLE ON D.



GIVEN: TENSION IN CABLE DBE 15 385 N.

FINDI COMPONENTS OF FORCE EXERTED BY CABLEON E

 $EB = (270 \text{ mm}) L - (400 \text{ mm}) \frac{1}{3} + (600 \text{ mm}) \frac{1}{6}$ $EB = \sqrt{(270)^2 + (400)^2 + (600)^2} = 770 \text{ nm}$ $F = F \frac{2}{EB} = \frac{385 \text{ N}}{FB} = \frac{385 \text{ N}}{770 \text{ nm}} [(270 \text{ nm}) L - (400 \text{ nm}) \frac{1}{3} + (600 \text{ nm}) \frac{1}{6}].$ $F = (135 \text{ N}) L - (200 \text{ N}) \frac{1}{2} + (300 \text{ N}) \frac{1}{6}$ $F_z = + 135 \text{ N}, \quad F_y = -200 \text{ N}, \quad f_z = +300 \text{ N}$

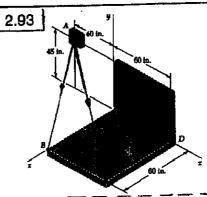


GIVEN : P=300 N. Q=400 H

MAGNITUDE AND DIRECTION OF RESULTANT OF PAND Q.

FORCE P: P=- (300 N) cos 30 sin 15° = - 67.24 N
P=+ (300 N) sin 30° = + 150.00 N
P=+ (300 N) cos 30° cos 15° = + 250.95 N
P=- (67.24 N) L+ (150.00 N) J+ (250.95 N) L

FORCE Q: $Q_z = + (400 \text{ M}) \cos 50^{\circ} \cos 20^{\circ} = + 241.61 \text{ M}$ $Q_z = + (400 \text{ M}) \sin 50^{\circ} = + 306.42 \text{ M}$ $Q_z = - (400 \text{ M}) \cos 50^{\circ} \sin 20^{\circ} = -87.44 \text{ M}$ $Q_z = + (241.61 \text{ M}) \cdot \cdot + (306.42 \text{ M}) \cdot j - (87.94 \text{ M}) \cdot k$



GIVEN: TAB = 425 16 TAC = 510 16

FIND: MAGNITUDE AND DIRECTION OF RESULTANT OF FORCES AT A.

 $\overrightarrow{AB} = (40 \text{ in}) \underline{i} - (45 \text{ in}) \underline{j} + (60 \text{ in}) \underline{k} \qquad \overrightarrow{AB} = \sqrt{(40)^2 + (45)^2 + (60)^2} = 85 \text{ in}$ $\overrightarrow{AC} = (100 \text{ in}) \underline{i} - (45 \text{ in}) \underline{j} + (60 \text{ in}) \underline{k} \qquad \overrightarrow{AC} = \sqrt{(100)^2 + (45)^2 + (60)^2} = 125 \text{ in}$ $\overrightarrow{E_{AB}} = \overrightarrow{F_{AB}} = \overrightarrow{F_{AB}} = \overrightarrow{AB} = \frac{425 \text{ lb}}{85 \text{ in}} \left[(40 \text{ in}) \underline{i} - (45 \text{ in}) \underline{j} + (60 \text{ in.}) \underline{k} \right]$ $\overrightarrow{F_{AB}} = (200 \text{ lb}) \underline{i} - (225 \text{ lb}) \underline{j} + (300 \text{ lb}) \underline{k}$

 $F_{AC} = F_{AC} \frac{AC}{AC} = \frac{510 \text{ M}}{125 \text{ in}} \left[(100 \text{ in}) \dot{\textbf{i}} - (45 \text{ in}) \dot{\textbf{j}} + (60 \text{ in}) \dot{\textbf{k}} \right]$ $F_{AC} = (408 \text{ lb}) \dot{\textbf{i}} = (183.6 \text{ lb}) \dot{\textbf{j}} + (244.8 \text{ lb}) \dot{\textbf{k}}$

R = FAS+FAC = (608 b) - (408.6 b) + (544.8 b) k, R= 912.92 b

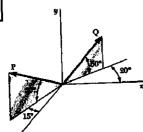
R = 913 16

 $\cos \theta_{x} = R_{x}/R = 608/912.92 = 0.6660$ $\cos \theta_{y} = R_{y}/R = -408.6/912.12 = -0.4476$ $\cos \theta_{y} = R_{y}/R = 544.8/912.92 = 0.5968$

2.94

θ₁ = 48.2° θ₁ = 116.6° θ₂ = 53.4°

2.92



GIVEN:

P = 400 H Q = 300 M

HAGNITUDE AUD
DIRECTION OF
RESULTANT
OF PAND Q.

FORCE P: $P_{x=}$ - (400 N) cos 30° sin 15°= - 89.66 N $P_{y=}$ + (400 N) sin 30°= + 200.00 N $P_{z=}$ + (400 N) cos 30° cos 15°= +334.61 N $P_{z=}$ - (89.66 N) $\frac{1}{6}$ + (200.00 N) $\frac{1}{6}$ + (334.61 N) $\frac{1}{6}$

PORCE $\underline{\alpha}$: G'_{z} =+(300 N)cos 50cos 20°=+ 1B1.21 N G'_{z} =+(300 N) si n 50°=+ 229.81 N G_{z} =-(300 N)cos 50°sin 20°=-65.45 N $\underline{\alpha}$ =(1B1.21 N) \underline{i} +(229.81N) \underline{i} -(65.95 N) \underline{k}

RESULTANT:

 $R = P + Q = (41.55 \text{ N}) \cdot \cdot + (429.81 \text{ N}) \cdot \cdot + (268.66 \text{ N}) \cdot \cdot \cdot$ $R = \sqrt{(41.55)^2 + (429.81)^2 + (268.66)^2} = 515.07 \text{ N}, R = 515 \text{ N}$ $\cos \theta_{x} = R_{x}/R = (41.55 \text{ N})(515.07 \text{ N}) = 0.1777 \qquad \theta_{y} = 79.8^{\circ}$

cos 0 = R /R = (429, 0) N)/(5/5.07 N) = 0.8345 cos 0 = R /R = (268.66N)/(5/5.07 N) = 0.5216 AB = (40 in.) i - (45 in.) j + (60 in) k AB

GIVEN: T_{AB} = 510 lb T_{AC} = 425 lb

FIND:

MAGNITUDE AND DIRECTION OF RESULTANT OF FORCES AT A.

 $\overrightarrow{AB} = (40 \text{ in.}) \cdot (45 \text{ in.}) \cdot + (60 \text{ in.}) \cdot AB = \sqrt{(40)^2 + (45)^2 + (60)^2} = 85 \text{ in.}$ $\overrightarrow{AC} = (100 \text{ in.}) \cdot - (45 \text{ in.}) \cdot + (60 \text{ in.}) \cdot AC = \sqrt{(100)^2 + (45)^2 + (60)^2} = 125 \text{ in.}$

 $F_{AB} = F_{AB} = F_{AB} = \frac{510 \text{ lb}}{85 \text{ in}} [(40 \text{ in.}) \dot{i} - (45 \text{ in.}) \dot{j} + (60 \text{ in.}) \dot{k}]$ $F_{AB} = (240 \text{ lb}) \dot{i} - (270 \text{ lb}) \dot{j} + (360 \text{ lb}) \dot{k}$

 $F_{AC} = F_{AC} = F_{AC} = \frac{AC}{AC} = \frac{4251b}{125in} [(100 in)i - (45 in)j + (60 in)k]$ $F_{AC} = (340 lb)i - (153 lb)j + (204 lb)k$

R = FAB + FAC = (580 16) i - (423 16) j + (564 16)k, R=912.92 16
R= 913 10 ■

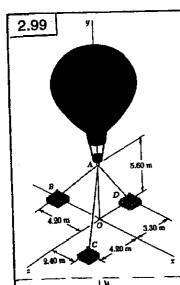
 $\cos \theta_z = R_z/R = 580/912.92 = 0.6353$ $\cos \theta_z = R_z/R = -425/912.92 = -0.4633$ $\cos \theta_z = R_z/R = 564/912.92 = 0.6178$

0,=117,6°

0,=548

0, = 33. 4°

0,=58.6°



GIVEN: TAB = 259 N

FIND:

VERTICAL FORCE P

EXERTED AT A BY THE BALLOON.

FIG. P 2.99, P 2.100, P2.101, AND P2.102

FREE BODY: A FORGES APPLIED AT A

TAB TACY D 3,50M

ARE T T T T AB , AC , AD ,

AND P, WHERE P = Pi.

TO EXPRESS THE OTHER

FORCES IN TERMS OF THE

UNIT VECTORS, WE WRITE

 $\begin{array}{lll}
\vec{AB} = -(4.20 \, \text{m}) \, \underline{i} - (5.60 \, \text{m}) \, \underline{j} & \vec{AB} = 7.00 \, \text{m} \\
\vec{AC} = (2.40 \, \text{m}) \, \underline{i} - (5.60 \, \text{m}) \, \underline{j} + (4.20 \, \text{m}) \, \underline{k}, & \vec{AC} = 7.40 \, \text{m} \\
\vec{AD} = -(5,60 \, \text{m}) \, \underline{j} - (3.30 \, \text{m}) \, \underline{k}, & \vec{AD} = 6.50 \, \text{m} \\
\vec{T}_{AB} = T_{AB} \frac{\gamma}{AB} = T_{AB} \frac{\vec{AB}}{AB} = (-0.6 \, \underline{i} - 0.8 \, \underline{j}) \, T_{AB}
\end{array}$

$$T_{AC} = T_{AC} \frac{\lambda_{AC}}{\lambda_{AC}} = T_{AC} \frac{AC}{AC} = \left(\frac{24}{74} \dot{i} - \frac{56}{74} \dot{i} + \frac{42}{74} \dot{k}\right) T_{AC}$$

$$T_{AD} = T_{AD} \frac{\lambda_{AD}}{\lambda_{AD}} = T_{AD} \frac{AB}{AB} = \left(-\frac{56}{45} \dot{i} - \frac{33}{65} \dot{k}\right) T_{AD}$$

EQUILIBRIUM CONDITION :

BY

'2<u>k</u>

Substituting the expressions obtained for I_{AB} , I_{AC} , and I_{AD} and factoring \dot{b} , \dot{a} , and \dot{k} :

$$\begin{array}{l} \left(-0.6\ T_{AB} + \frac{24}{74}\ T_{AL}\right) \stackrel{\mathcal{L}}{L} \\ + \left(-0.8\ T_{AB} - \frac{56}{74}\ T_{AC} - \frac{56}{65}\ T_{AD} + P\right) \stackrel{\mathcal{L}}{g} \\ + \left(\frac{42}{77}\ T_{AC} - \frac{33}{65}\ T_{AD}\right) \stackrel{\mathcal{L}}{k} = 0 \end{array}$$

ERUMTING TO ZERO THE COEFFICIENTS OF 1, 1, 6:

$$\bullet \quad -0.8 \, T_{AB} - \frac{36}{74} \, T_{AC} - \frac{56}{65} \, T_{AD} + P = 0 \tag{2}$$

$$\frac{42}{74} T_{AC} - \frac{33}{65} T_{AD} = 0$$
 (3)

CONTINUED

2.99 CONTINUED

MAKING $T_{AB} = 159 \, \text{M}$ IN EQ.(1) AND SOLVING FOR TAC: $T_{AC} = \frac{74}{24} (0.6)(259 \, \text{N}) \qquad \text{TAC} = 479.15 \, \text{M}$ CARRYING INTO EQ.(3) AND SOLVING FOR TAD: $T_{AD} = \frac{65}{33} \frac{42}{74} (479.15 \, \text{N}) \qquad T_{AD} = 535.66 \, \text{M}$ SUBSTITUTING FOR T_{AB} , T_{AC} , T_{AD} INTO (2) AND SOLVING FOR P: $P = 0.8(259 \, \text{N}) + \frac{56}{74} (479.15 \, \text{N}) + \frac{76}{65} (535.66 \, \text{N}) = 1031.3 \, \text{N}$ $P = 1031 \, \text{N}$

2.100 GIVEN: TAC = 444 N

GER FIGURE FIND: VERTICAL FORCE P EXERTED
ON LEFT) AT A BY THE BALLOON

SEE LEFT-HAND COLUMN FOR DERIVATION OF EAS.(1),(2),(3),

NAKING TAC = 444 N IN EWS. (1) AND (3) AND SOLVING

FOR TAB AND TAD:

TAB = 24 N

TAB = 240 N

TAB = 240 N

SUBSTITUTING FOR TAB | TAC | TAD INTO (2) AND SOLVING

FOR P:

P = 0.8 (240 N) + 56 (444 N) + 56 (446,36N) = 955.6 N

2.101 (SEE FIGURE ON UPPER LEFT)

GIVEN: TAD = 481 N

FIND: VERTICAL FORCE PEXERTED AT A BY THE BALLOON

SEE LEFT-MAND COLUMN FOR DERIVATION OF EGS. (1), (2), (3).

MAKING T_{AD} = 481N IN Eq. (3) AND SOLVING FOR TAC: $T_{AC} = \frac{74}{42} \frac{33}{65} (481 \text{ N})$ Tac = 430.26 N

CARRYING INTO EQ. (1) AND SOLVING FOR TAB! $T_{AB} = \frac{24}{0.6(74)} (430.26 \text{ N})$ Tag = 232.57 N

SUBSTITUTING FOR T_{AB} , T_{AC} , T_{AB} INTO (2) AND SOLVING-FOR P: $P = 0.8(232.57 \text{ N}) + \frac{56}{74}(430.26 \text{ N}) + \frac{56}{65}(481 \text{ N}) = ,926.06 \text{ N}$

2.102 (SEE FIGURE ON UPPER LEFT)

GIVEN: BACKON EXERTS FORCE P=800N AT A.

FIND: TENSION IN EACH CABLE

SEE LETT-HAND COLUMN FOR DERIVATION OF EAS. (0, (2), (3)).

FROM EQ. (1): $T_{AB} = \frac{24}{0.6(74)}$ AC $T_{AB} = 0.54054$ TAC

FROM EQ. (3): $T_{AD} = \frac{65}{33} \frac{42}{74}$ TAC $T_{AD} = 1.1179$ TAC

SUBSTITUTE FOR T_{AB} AND T_{AD} INTO EQ. (2): $-0.8(0.54054 T_{AC}) - \frac{56}{74} T_{AC} - \frac{56}{65} (1.1179 T_{AC}) + P = 0$ $2.1523 T_{AC} = P$ $T_{AC} = \frac{800N}{2.1523}$ $T_{AC} = 371.69 N$ SUBSTITUTE INTO EX PRESSIONS FOR T_{AB} AND T_{AD} : $T_{AB} = 0.54054(371.69 N) = 200.91N$ $T_{AD} = 1.1179(371.69 N) = 415.51 N$ $T_{AB} = 201N$, $T_{AC} = 372N$, $T_{AD} = 416N$

CONTINUED 2.111

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RO:

(1)

(2)

(3)

ΞD

;7 A. WE REPEAT THE LAST EUS.

$$-160 lb + \frac{60}{118} T_{AC} - \frac{10}{126} T_{AD} = 0$$
 (1)

$$-800 \text{ lb} - \frac{100}{118} \text{ T}_{AC} - \frac{100}{126} \text{ T}_{AD} + P = 0$$
 (2)

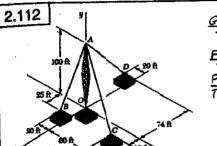
$$200 \text{ Lb} + \frac{18}{118} T_{AC} - \frac{74}{126} T_{AD} = 0$$
AULTIPLY EQ.(1) BY -3, EQ.(3) BY 10,AND ADD:

Tap= 459.519 | 1480 16 - 480 TAD = 0

SUBSTITUTE INTO (1) AND SOLVE FOR THE TAC = 118 (160 + 20 × 459.529) T = 458,118 16

SUBSTITUTE FOR THE TENSIONS IN (2) AND SOME FOR P: P=800 lb+ \frac{100}{118}(458.118 lb) + \frac{100}{126}(459.529 lb) = 1552,94 lb

WEIGHT OF PLATE = P= 1553 16



TAC = 590 16 VERTICAL FORCE P EXERTED BY TOWER ON PIN A.

FREE BODY! A EF = 0: IAB+IT+IAD+ Pi=0 AB = -201-100j+25# AB = 105 ft AC = 601-1001 +18K AC = IIB ft AD = -201-100j -74 k AD = 126 ft

TAB = TAB AB = TAB = (-4 1 - 201+5 K) TAB TAC = TAC 2AC = TAC AC = (60 i - 100 1 + 18 k) TAC $I_{Ab} = T_{Ab} \; 2_{Ab} = T_{Ab} \; \frac{\overrightarrow{AD}}{\overrightarrow{AD}} = \left(-\frac{20}{126} \, \dot{\vec{k}} - \frac{100}{126} \, \dot{\vec{q}} - \frac{74}{126} \, \dot{\vec{k}} \right) T_{AD}$

SUBSTITUTING INTO THE ER. ZF=0 AND FACTORING : 1, 5; (-4 TAB+ 60 TAC- 20 TAS) =

$$+\left(-\frac{20}{21}T_{AB} - \frac{100}{118}T_{AC} - \frac{100}{124}T_{AB} + P\right)\frac{1}{9}$$

$$+\left(\frac{5}{21}T_{AB} + \frac{18}{118}T_{AC} - \frac{74}{126}T_{AB}\right)k = 0$$

SETTING THE COEFF. OFL, & EQUAL TO ZERO:

$$\begin{array}{lll}
\mathbf{D} & -\frac{1}{21} T_{AB} + \frac{60}{118} T_{AC} - \frac{20}{126} T_{AD} = D & \text{(i)} \\
\mathbf{D} & -\frac{20}{21} T_{AB} - \frac{100}{118} T_{AC} - \frac{100}{126} T_{AD} + P = 0 & \text{(2)} \\
\mathbf{D} & \frac{5}{21} T_{AB} + \frac{18}{118} T_{AC} - \frac{74}{126} T_{AD} = 0 & \text{(3)}
\end{array}$$

CONTINUED

2.112

CONTINUED MAKING T = 590 Ib IN EQS. (1),

(1) $-\frac{Q}{L1}T_{AB} - \frac{20}{126}T_{AB} + 300 lb = 0$

[2') 20 TAS - 100 TAD - 500 16 + 9 = 0

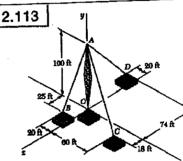
(3') $\frac{5}{21}T_{AB} - \frac{74}{126}T_{AB} + 90 \text{ lb} = 0$

MULTPLY ER.(1') BY 5, EQ.(3') BY 4, AND ADD!

TAD = 591.818 16 ~ 395 TAD + 1860 lb = 0 THE = 21 (300 % - 20 x 591.818 16 TAB = 1081.82 %

SUBSTITUTE FOR THE TENSIONS IN (2') AND SOLVE FOR P. P. 500 B + 20 (108 L82 16) + 100 (591.818 16) = 2000.00 16

WEIGHT OF PLATE = P = 2000 16



GIVEN: TOWER EXERTS ON A AN JAWARD VERTICAL FURCE P OF 1800 lb.

FIND: TENSION IN EACH WIRE.

SEE COLUMN ON THE LEFT FOR DERIVATION OF EGS. (1), (2), AND(3), MAKING P= 1900 Ib IN ER. (2), WE HAVE

 $-\frac{4}{21}T_{AB} + \frac{60}{118}T_{AC} - \frac{20}{126}T_{AD} = 0$ (1)

 $-\frac{20}{2!}T_{AB} - \frac{100}{110}T_{AC} - \frac{100}{126}T_{AB} + 1800 / b = D$ (z)

 $\frac{5}{21} T_{AB} + \frac{18}{110} T_{AC} - \frac{74}{116} T_{AC} = 0$ MULTIPLY (1) BY -74, (3) BY 20, AND ADD: (3)

396 TAB - 4080 TAC = 0 TA = 0,545378 TAB (4)

SUBSTITUTE INTO (1):

$$\left[-\frac{4}{71} + \frac{60}{118}(0.545378)\right]$$
 TAB - $\frac{20}{126}$ TAD = 0

0.0868347 TAB - 20 TAD = 0.547059 TAB (5)

SUBSTITUTE FOR TAC AND T INTO (2) AND SOLVE FOR TAB:
- 20 T - 100 (0,545378 TA) - 100 (0.547059 TAB) + 1800 16 = 0

1.84814 TAB = 1800 16 TAB = 973.636 16

TAB = 974 /b

SUBSTITUTING PROM (6) INTO (4):

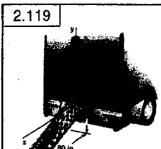
TAC = 0545378 (973.636 15) = 531,000 16

The = 531 H

SUBSTITUTING FROM (6) INTO (5);

TAD = 0,547051 (973.636 16) = 532.637 16

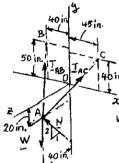
TAD = 533 16



GIVEN!

- (1) 200-16 COUNTERWEIGHT IS IN EQUILIBRIUM UNDER FORCES EXERTED BY ROPES AND FORCE PERPENDICULAR TO CHUTE.
- (2) COORDINATES OF A,B,CARE A (0, -20 in. 40 in.) B (-40 in., 50 in. 0) c (45 in., 40 in., 0) FIND:

TENSION IN EACH ROPE.



FREE BODY : COUNTERWEIGHT **互チ=δ**: Ins+ In+ W+N = 0 ₩=-(200 /b) j

$$\overrightarrow{AB} = -(40 \text{ id.}) \underline{i} + (70 \text{ in.}) \underline{j} - (40 \text{ in.}) \underline{k}$$

$$\overrightarrow{AB} = 90 \text{ in.}$$

$$\overrightarrow{AC} = (45 \text{ in.}) \underline{i} + (60 \text{ in.}) \underline{j} - (40 \text{ in.}) \underline{k}$$

$$\overrightarrow{AC} = B5 \text{ in.}$$

THUS:
$$T_{AB} = T_{AB} \frac{\overrightarrow{AB}}{\overrightarrow{AB}} = (-\frac{4}{7} \frac{1}{2} + \frac{7}{7} \frac{1}{2} - \frac{7}{7} \frac{1}{6}) T_{AB}$$

 $T_{AC} = T_{AC} \frac{\overrightarrow{AC}}{\overrightarrow{AC}} = (\frac{9}{17} \frac{1}{2} + \frac{12}{17} \frac{1}{2} - \frac{8}{17} \frac{1}{6}) T_{AC}$

SUBSTITUTE FOR T ABOTACIN, AND WINTO E FOU AND FACTOR 1, 3, 4:

EQUATING TO ZERO THE COEFFICIENTS OF LILE:

MULTIPLY (3) BY -2 AND ADD (2):

$$\frac{15}{3} T_{AB} + \frac{28}{17} T_{AC} - 200 \ lb = 0 \tag{4}$$

MULTIPLY (1) BY 15, (4) BY 4, AND ADD:

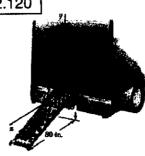
$$\frac{247}{17}T_{AC} - 800 \, lb = 0 \qquad T_{AC} = 55.061 \, lb \quad (5)$$

SUBSTITUTE PROM (5) INTO (1) AND SOLVE FOR TAB :

TAB = 4 . 17 (55,061 16) = 65,587 B

THE TENSIONS IN THE ROPES ARE

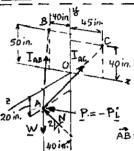




GIVEN:

(1) 200-16 COUNTERWEIGHT/IS IN EMUILIBRIUM UNDER FURCES EXERTED BY THE TWO WURKERS SHOWN, BY A THIRD WORKER WHO PUSHES WITH P = - (40 b) : AND A FORCE PERPENDICULAR TO THE CHUTE. (2) COOR DINATES OF ALB.CARE A (0,-20 to, 40 in) B (-40 in., 50 in., 0)

C (45 in., 40 in., 0) FIND: TENSION IN ROPES AB AND AC.



FREE BODY; COUNTERWEIGHT $\Sigma T = 0$ TAB+ TAC+ W+P+N = 0 W= - (200 lb)+ P = - (40 lb) i N=(學9+學k)N

WE NOTE THAT AB = - (40 in) i + (70 in) j - (40 in)k AC = (45 in) = + (60 in) = - (40 in) k

THUS:
$$T_{AB} = T_{AB} \frac{\overrightarrow{AB}}{AB} = (-\frac{4}{9} \frac{1}{6} + \frac{7}{9} \frac{1}{6} - \frac{4}{9} \frac{1}{6}) T_{AB}$$

$$T_{AC} = T_{AC} \frac{\overrightarrow{AC}}{AC} = (\frac{9}{17} \frac{1}{6} + \frac{12}{17} \frac{1}{9} - \frac{18}{12} \frac{1}{6}) T_{AC}$$

SUBSTITUTE FOR TABITACIN, P, AND W INTO EF=O AND

EQUATING TO ZERO THE COEFFICIENTS OF L, L. E.

(2)
$$\frac{7}{4}T_{AB} + \frac{12}{17}T_{AC} + \frac{2}{15}N - 200 / b = 0$$

MULTIPLY (3) BY -2 AND ADD (2):

$$\frac{15}{7}T_{AB} + \frac{28}{17}T_{AC} - 200 \text{ lb} = 0 \tag{4}$$

MULTIPLY (1) BY IS, (4) BY 4, AND ADD:

SUBSTITUTE FROM (5) INTO (1) AND SOLVE FOR THE ! $T_{AB} = \frac{9}{4} \left[\frac{9}{17} (96,3563 \text{ lb}) - 40 \text{ lb} \right] = 24,777 \text{ lb}$

THE TENSIONS IN THE ROPES ARE

SHES

LAP CARE

HT.

in.

AND

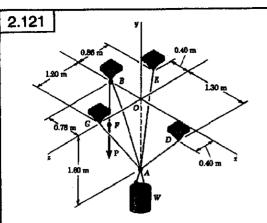
(1)

(2)

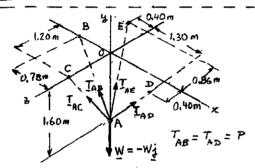
-(3)

(4)

(5)



GIVEN: CONTAINER OF WEIGHT W= 1000 N IS SUSPENDED FROM RING A. CABLES AL AND AE ARE ATTACHED TO RING. CABLE FRAD PASSES THROUGH RING AND OVER PULLEY B. FIND: MAGNITUDE OF FORCE P.



FREE 80DY: RING A $\Sigma F = 0 : T_{AB} + T_{AC} + T_{AD} + T_{AE} - W_j = 0$

AB = - (0.78m) + (1.60m) j AB= 1.78 N AC = 2,00 M

 $\vec{A}\vec{C} = (1.60 \text{ m}) \dot{a} + (1.20 \text{ m}) \ddot{k}$

 $\overrightarrow{AB} = (1.30m)\overrightarrow{i} + (1.40m)\overrightarrow{j} + (0.40m)\cancel{k}$ AD = 2,10 m $\overrightarrow{AE} = -(0.40m)\overrightarrow{i} + (1.60m)\overrightarrow{d} - (0.86m)\cancel{k}$ AE = 1.86 m

 $T_{AB} = P \Delta_{AB} = P \frac{AB}{AB} = (-\frac{0.78}{1.78} \frac{1}{1.78} + \frac{1.6}{1.78} \frac{1}{1.78}) P$

TAC = TAC AC = TAC AC = (0.8 + 0.6 k) TAC

 $T_{AD} = P \frac{\Delta}{2}_{AD} = P \frac{\overline{AD}}{AD} = (\frac{1.3}{2.1} \pm \frac{1.6}{2.1} \pm \frac{0.4}{2.1} \pm \frac{0.4}{2.1} \pm \frac{1}{2.1} \pm \frac{1.6}{2.1} \pm$

 $T_{AE} = T_{AE} \times_{AE} = T_{AE} = \left(-\frac{0.4}{1.86} \pm + \frac{1.6}{1.86} \pm - \frac{0.96}{1.86} \pm\right) T_{AE}$

SUBSTITUTING FOR THE TENSIONS IN Z F = 0 AND FACTORING L. 1 . K:

(-0.78 P+13 P-0.4 TAE) 6 $+\left(\frac{1.6}{1.78}P+0.8T_{AC}+\frac{1.6}{2.1}P+\frac{1.6}{1.56}T_{AE}-W\right)j$ $+(0.6 T_{AC} + \frac{0.4}{2.1} P_{-} \frac{0.86}{1.86} T_{AE}) k = 0$

EQUATING TO ZERO THE COEFFICIENTS OF L, 1, k, WE OBTAIN AFTER REDUCTIONS:

CONTINUED

2.121 CONTINUED

SOLVING(1) FOR TAE:

(D) 0.180845 P - 0.215054 TAE

(1) (2)

1, 66078P+ 0.8 TAC + 0.860215 TAC-W=0 (3)

1 0.190476P+0.6TAC - 0.462366TAE = 0

TAF = 0,840 131 P

CARRYING INTO ERS. (2) AND (3):

1.38416P + 0.8TAC -W=0

- 0-198542 P + 0.67 AC = 0

(w) (5)

MULTIPLY (4) BY 3, (5) BY -4, AND ADD: 7.945 \$5P - 3W =0

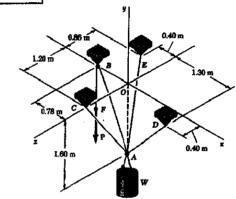
MAKING W= 1000 N:

7:94585P-2000 N=D

P=377.556 N

P=378 N

2.122



GIVEN:

(1) CONTAINER IS SUSPENDED FROM RING A. CABLES AC AND AE ARE ATTACHED TO RING. CABLE FRAD PASSES TROUGH RING AND OVER PULLEY B. (2) TAC= 150 N.

FIND:

- (a) MAGNITUDE OF FORCE P (b) WEIGHT W OF CONTAINER
- SEE SOLUTION OF PROB. 2.121 LEADING TO EGS. (4) AND (5);

2,38416 P + 0.8 TAC-W=0 -0.198342 P+0.6Tac=0

(a) MAKE TAL= 150 N IN EQ.(5):

-0.198342 P + 0.6(150 N) = 0 P = 453.762 N

P= 454 N

(5)

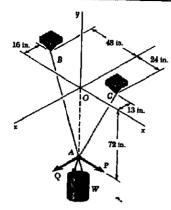
(b) CARRY THE VALUES OF TAC AND P INTO EQ.(4):

2.38416 (453,762 N) + 0.8 (150 N) -W=0

W = 1201.84 N

W= 1202 N

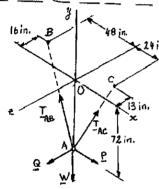
2.123



GIVEN: CONTAINER OF WEIGHT W=270 16 15 SUSPENDED FROM RING A.

CABLE BAC PASSES THROUGH RING A.

FIND: P AND Q FOR EQUILIBRIUM POSITION SHOWN



FREE BODY: RING A WHERE PE PL

TAC =TAAC (SAME TENSION T IN BOTH PORTIONS OF CABLE)

WE HAVE

$$I_{AB} = T 2_{AB} = T \frac{AB}{AB} = \left(-\frac{6}{11} \frac{i}{i} + \frac{9}{11} \frac{j}{i} - \frac{2}{11} \frac{k}{k} \right) T$$

$$I_{AC} = T 2_{AC} = T \frac{AC}{AC} = \left(\frac{24}{17} \frac{i}{i} + \frac{72}{77} \frac{j}{j} - \frac{13}{17} \frac{k}{k} \right) T$$

SUBSTITUTING FOR TAB, TAGS P. G. ANDW INTO EFEU AND FACTORING L. & K:

SUBSTITUTING FOR
$$T_{AB}$$
, T_{ac} , P_{a} , Q_{a} , and W interpretable in Q_{a} , $Q_$

SETTING THE COEFFICIENTS OF L, & EQUAL TO ZERO AND REDUCING!

$$\begin{array}{ccc}
\textcircled{0} & -\frac{10}{77} & \overrightarrow{1} + \overrightarrow{P} = 0 \\
\textcircled{0} & -\frac{10}{77} & -\frac{10}{77}
\end{array}$$
(1)

$$\frac{d}{2} = \frac{135}{77} T - W = 0$$
(2)

MAKING W= 270 Ib IN EQ. (2) AND SOLVING FOR T: T= 27 (270 b) = 154.0 lb

SUBSTITUTING FORT IN EQS. (1) AND (3), WE OBTAIN P=36,016, Q=54.0 16

2.124

(SEE FIGURE ON THE LEFT) GIVEN: (1) Q = 36 16. (2) CABLE BAC PASSES THROUGH RING A.

FIND: WAND P. SEE SOLUTION AT LEFT FOR DERIVATION OF ERS. (1), (2), (3).

MAKING Q = 36 16 IN EQ. (3): -27T+3615=0 T= 27 (36 lb) T=102,667 16 SUBSTITUTING FOR T IN EQS. (1) AND (2):

- 18/77 (102,66716) + P=0

P=24.0 B W=180.016

135 (102.667 16) -W = 0

2.125

GIVEN: (1) COLLARS A AND B CONNECTED BY WIRE OF LENGTH 525 mm (2) P= (341 N) }

(3) 4 = 155 mm FIND: (a) TAB

(b) Q FOR EQUILIBRIUM

 $(AB)^2 = \chi^2 + y^2 + z^2;$ $(525 \text{ mm})^2 = (200 \text{ mm})^2 + (155 \text{ mm})^2 + z^2$ $\overrightarrow{AB} = (200 \text{ mm}) \cdot i - (155 \text{ mm}) \cdot j + (460 \text{ mm}) \cdot k$ $\overrightarrow{AB} = \frac{\overrightarrow{AB}}{\overrightarrow{AB}} = \frac{200}{525} \cdot i - \frac{155}{525} \cdot j + \frac{460}{525} \cdot k$ AB = 525mm

(a) FREE BODY; COLLAR AT \(\bar{\pm}\)E=0; Nzi +Pj+Nz++ TB 2AB=0 SUBSTITUTING FOR AB AND SETTING THE COEFF. OF & ERUAL TO ZERO: P+ (-155 TAB) = 0

MAKING P=341 N AND SOLULING FOR TAB!

TAB = 525 (341 N) Tan = 1155 N

> (b) FREE BODY : COLLAR B $\Sigma F = 0$

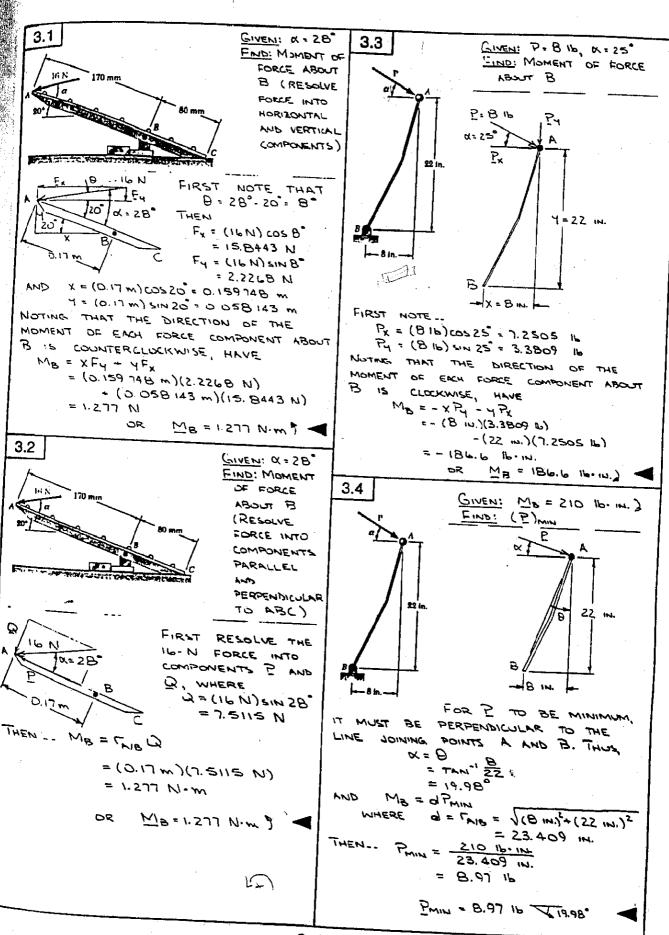


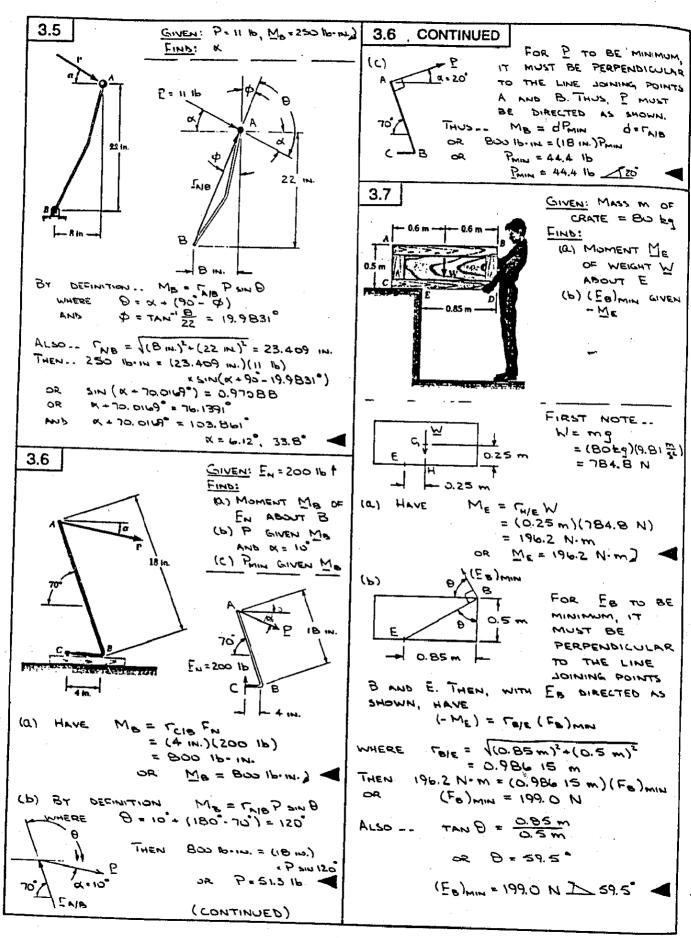
NE + Ny j + Q K - TAB 2AB =0 SUBSTITUTING FOR 2 AM SETTING THE COEFF. OF K EQUAL TO ZERO: $Q = (\frac{460}{525}T_{AB}) = 0$

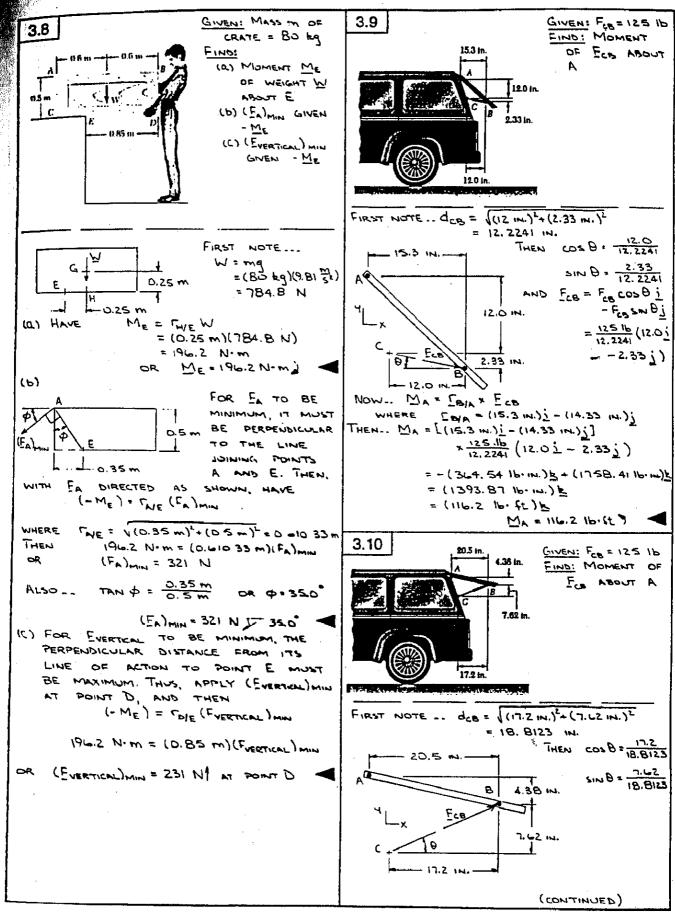
MAKING TAB = 1155 N AND SOLVING FOR Q:

Q = 460 (1155 N)

Q=1012 N



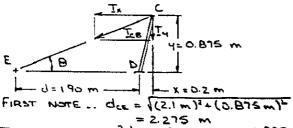




3.10 CONTINUED FCB = FCR COSDIA FCB SIND = 125 16 18, 8/23 (17.21 + 7.62) NOW .. MA = [6/A * Ecb WHERE [18/A = (20,5 m.)] - (4.38 m.)] THEN. Mr = [(20.5 m.)i - (4.38 m.)j] x 125 16 (17.2 1 + 7.62) = (1037.95 1b.IN.) 12+(500.58 1b.III.) 12 = (1538.53 lb.in.) E = (128.2 16.51) E Mx = 128.2 16. 623 -3.11

GIVEN: Top = 1040 N, d= 1.90 m. FIND: MOMENT OF TED ABOUT D; RESOLVE ICE INTO HORIZONTAL AND VERTICAL COMPONENTS APPLIED AT (a) POINT (

(b) POINT E

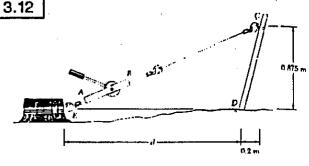


 $\cos \theta = \frac{2.1}{2.275} = \frac{12}{13}$ SIND = 0.875 = 5 THEN $T_{x} = T_{c_{B}} \cos \theta = (1040 \text{ N})(\frac{12}{13}) = 960 \text{ N}$

Ty = Too SIND = (1040 N)(3) . 400 N (a) BY OBSERVATION. Mo = - XTy + YTx $M_b = (0.2 \, \text{m})(400 \, \text{H}) + (0.815 \, \text{m})(960 \, \text{H})$ = 760 N·m

MD = 760 N·m) (6) BY OBSERVATION .. Mo = dTy

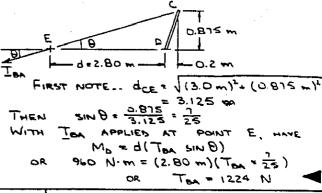
= (1.90 m)(400 N) = 760 N·m Mo: The N.W)

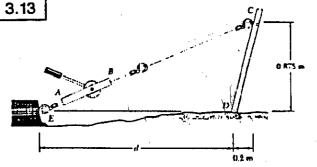


GIVEN: MOMENT OF IBN ABOUT D = 960 N. m. d= 2.80 m

FIND: TON

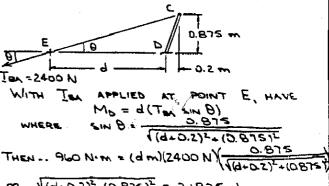
0.875 m



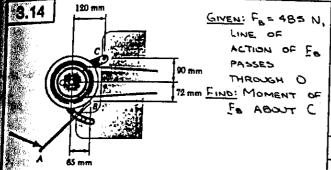


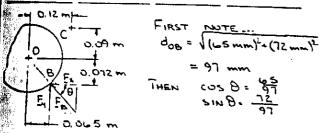
GIVEN: MOMENT OF TEN ABOUT D = 940 N.m. (Tax) max = 2400 N

FIND: dmin



OR V(d+0.2)2+(0.875)2 = 2.1875 d SQUARING BOTH SIDES OF THE EQUATION .. d2 + a4d + a04 + a7656 = 4.7852 d3 3,7852 d2 - 0.4d - 0.8056 = 0 (BUNITHWE)

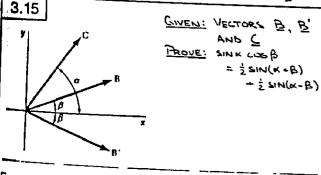




BY OBJERVATION. $M_{c} = -xF_{q} - qF_{x}$ WHERE x = 0.12 m - 0.045 m = 0.065 m q = 0.072 m + 0.09 m = 0.162 mTHEN $M_{c} = -(0.055 m)(360 N)$ = -(0.162 m)(325 N) $= -72.45 N \cdot m$

Mc = 72.5 N-m)

(CONTINUES)



FIRST NOTE.
$$B = B(cos\beta_i + sin\beta_i)$$

 $B' = B(cos\beta_i - sin\beta_i)$
 $C = C(cosx_i + sina_i)$

BY DEFINITION.
$$|\underline{B} \times \underline{C}| = BC \sin(x - B)$$
 (1)
 $|\underline{B}' \cdot \underline{C}| = BC \sin(x + B)$ (2)

3.15 CONTINUED

 $B_{x} = B(\cos \beta + \sin \beta \cos x) E$ $= B(\cos \beta - \sin \beta)$ $= B(\cos \beta - \sin \beta)$

EQUATING THE RIGHT- HAND SIDES OF EQS.

(1) AND (2) TO THE MAGNITUDES OF THE

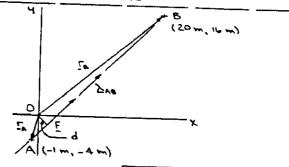
RIGHT- HAND SIDES OF EQS. (3) AND (4),

RESPECTIVELY, YIELDS...

BC $\sin(\alpha-\beta) = BC(\cos\beta\sin\alpha - \sin\beta\cos\alpha)$ (5) BC $\sin(\kappa+\beta) = BC(\cos\beta\sin\alpha + \sin\beta\cos\kappa)$ (6) (5)+(6) $\Rightarrow \sin(\kappa-\beta) + \sin(\alpha+\beta) = 2\cos\beta\sin\alpha$ OR $\sin\kappa\cos\beta = \frac{1}{2}\sin(\alpha+\beta) + \frac{1}{2}\sin(\kappa-\beta)$

3.16 GIVEN: POINTS (20 m, 16 m) AND
(-1 m, -4 m)
Euro: Perpermission

FIND: PERPENDICULAR DISTANCE &
FROM THE ORIGIN TO THE
LINE DRAWN THROUGH THE
POINTS



FIRST NOTE .. das = \[\langle 20 m - (-1m)\rangle^2 + \langle 16 m - (-4m)\rangle^2
= 29 m

Now assume that a force F, of magnitude F, acts at point A and is directed from A to B. Then $F = F \underline{\lambda}_{AB} = \frac{CB - CA}{AB}$ where $\underline{\lambda}_{AB} = \frac{CB - CA}{AB}$

BY DEFINITION. $M_0 = 1 \sum_{i=1}^{n} (2i j + 20j)$ WHERE $\sum_{i=1}^{n} (1 m) j - (4 m) j$

THEN $M_0 = [-(1m)_{\frac{1}{2}} - (4m)_{\frac{1}{2}}] \times \frac{E}{29} (21_{\frac{1}{2}} + 20_{\frac{1}{2}})(N)$ $= \frac{E}{29} [-(20)_{\frac{1}{2}} + (84)_{\frac{1}{2}}] N \cdot m$ $= (\frac{104}{29} F N \cdot m)_{\frac{1}{2}}$

FINALLY .. (129 F) N·m = d(FN)

OR d= 29 m

9 = 5.51 w

3.17	
	FIND: DOIT VECTOR > MORMAL TO THE
1	B WHEN B WHEN
	(a) A = i + 2 j - 5 k
	(a) A = i + 2j - 5 k B = 4i - 7j - 5 k (b) A = 3i - 3j + 2k
Ì	(b) A = 31 - 31 + 2k
	B = -2 <u>i</u> + Cj - 4 k
Br	DEFINITION, THE VECTOR A. B 15
NORMA	L TO THE PLANE DEFINED BY
A ~~	o B Thus, AxB
	$\overline{Y} = \frac{ \overline{Y} \times \overline{B} }{ \overline{Y} \times \overline{B} }$
(OL) HA	NE 1 2 -5
	4 -7 -5
	= (-10-35) <u>i</u> + (-20+5)j
	+ (-7-8) 1
THEN	$= -45\underline{i} - 15\underline{j} - 15\underline{k}$ $1 \underline{A} \times \underline{B} = 15 \sqrt{(-3)^2 + (-1)^2 + (-1)^2}$
	= 15 (11
	:
(P) HA	$ \frac{A \times B}{-2} = \begin{vmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{2} \\ -2 & 6 & -4 \end{vmatrix} $
	-2 6 -4
	= (12-12) + (-4+12);
	+(18-6)15

(b) HAVE
$$\underline{A} \times \underline{B} = \begin{vmatrix} \underline{i} & \underline{j} & \underline{k} \\ 3 & -3 & 2 \end{vmatrix}$$

$$= (12 - 12)\underline{i} + (-4 + 12)\underline{j} \\
+ (18 - 6)\underline{k}$$

$$= 8\underline{j} + 12\underline{k}$$
THEN
$$|\underline{A} \times \underline{B}| = 4\sqrt{(2)^2 + (3)^2}$$

$$= 4\sqrt{13}$$

$$\vdots \quad \underline{\lambda} = \frac{1}{\sqrt{13}}(2\underline{j} + 3\underline{k})$$
3.18 Given: Advances to the second size \underline{B}

3.18 GIVEN: ADJACENT SIDES P AND Q OF A PARALLELOGRAM FIND: AREA OF PARALLELOGRAM WHEN (a) P = -7:+3:-3½ Q = 2:+2:+5½ (b) P = 6:-5:-2½ Q = -2:+5:-½ HAVE. AREA A = |P = Q|

HAVE.. AREA $A = 17 \cdot Q1$ (a) $P \times Q = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -7 & 3 & -3 \end{vmatrix}$ = (15+1)i + (-16+35)j + (-14-16)k = 21j + 29j - 20kTHEN $A = \sqrt{(20)^2 + (29)^2 + (-20)^2}$ A = 41.0(b) $P \times Q = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -2 & 5 & -1 \end{vmatrix}$ = (5+10)j + (4+10)j + (30-10)k = 15j + 10j + 20kTHEN $A = 51(3)^2 + (2)^2 + (4)^2$ A = 26.9

3.19	GIVEN: FORCE E = 6 +4 - E ACTING
	A ruige ta
	FIND: MOMENT OF E ABOUT ORIGIN
	O WHEN
-	(a) <u>r</u> = -2 <u>i</u> + 6 <u>i</u> + 3 <u>8</u>
	(b) [x = 51-3]+7k
	(C) In = -91- 11-11-15E

By DEFINITION $M_0 = \prod_{A} \times \frac{E}{A}$ (a) HAVE... $M_0 = \begin{vmatrix} \frac{1}{2} & \frac{1}{2} & \frac{E}{A} \\ -2 & \frac{1}{2} & \frac{1}{2} \end{vmatrix}$ $= (-6 - 12) \frac{1}{2} + (18 - 2) \frac{1}{2} + (-8 - 3L) \frac{1}{2}$ $= -18 \frac{1}{2} + 16 \frac{1}{2} - 44 \frac{1}{2}$

(b) Have... $M_0 = \begin{vmatrix} \frac{1}{5} & \frac{1}{3} & \frac{1}{7} \\ \frac{5}{6} & \frac{3}{7} & \frac{7}{7} \\ \frac{6}{6} & \frac{4}{7} & \frac{1}{7} \\ \frac{1}{7} & \frac{1}$

(C) HAVE $M_0 = \begin{vmatrix} i & j & k \\ -9 & -6 & i.5 \end{vmatrix}$ = (6-6)i+(9-9)j+(-36+36)k= 0

NOTE: THE ANSWER TO PART C IS AS
EXPECTED SINCE IN AND E ARE
PROPORTIONAL (THUS, THEIR LINES OF
ACTION ARE PARALLEL).

3.20 GINEN: FORCE E = 21-71-36

ACTING AT POINT A

FIND: MOMENT OF E ABOUT ORIGIN

O WHEN

(a) In = 41-31-56

(b) In = 1-3.51-1.56

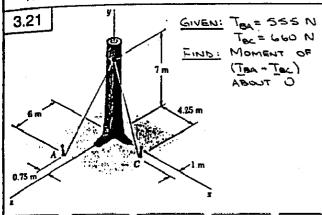
By DEFINITION $M_0 = [A \times E]$ (a) Have $M_0 = [A \times E]$ = (9 - 35)i + (-10 + 12)j + (28 + 6)E = -26i + 2j - 22E

(b) Have.. $M_D = \begin{vmatrix} i & j & k \\ -B & -2 & i \\ 2 & -7 & -3 \end{vmatrix}$ = $(6+7)\frac{1}{2}+(2-24)\frac{1}{2}+(56+4)\frac{1}{2}$

(C) HAVE .. $M_0 = \begin{vmatrix} 1 & 1 & k \\ 1 & -3.5 & -1.5 \\ 2 & -7 & -3 \end{vmatrix}$ = (10.5 - 10.5) + (-3+3) + (-7+7)

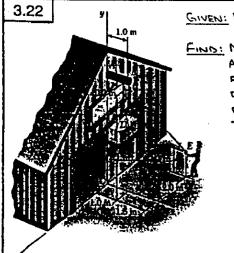


NOTE: THE ANSWER TO PART C IS AS
EXPECTED SINCE IN AND E ARE
PROPORTIONAL (THUS, THEIR LINES OF
ACTION ARE PARALLEL).



FIRST NOTE --
$$d_{BA} = \sqrt{(-0.75)^2 + (-7)^2 + (6)^2}$$

= 9.25 m
 $d_{BC} = \sqrt{(4.25)^2 + (-7)^2 + (1)^2}$
= 8.25 m



GIVEN: MASS M OF

BALE = 26 kg

FIND: MOMENT ABOUT

A OF RESULTANT

FORCE EXERTED

ON THE

PULLEY BY

THE ROPE

(CONTINUED)

3.22 CONTINUED

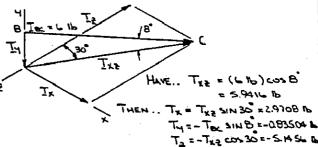
FIRST NOTE .. TO = TOE = WORLE = mg

WHERE $M = 2L bg g = 9.81 \frac{R}{5}L$ NOW. $d_{c} = \sqrt{(1.5)^{2} + (-6.0)^{2} + (-2.0)^{2}} = 6.5 \text{ m}$ THEN $T_{CE} = \frac{T_{CE}}{d_{CE}} CE = \frac{2L g}{6.5} (1.5i - 6j - 2k) (N)$ ALSO .. $T_{CD} = -(2L g)j$ (N)

NOW .. $R = T_{CD} + T_{CE}$ = g(6i - 50j - 8k) (N)AND $M_{A} = T_{CA} \times R$ WHERE $T_{CA} = (1 m)j - (0.3 m)j$ THEN .. $M_{A} = 9.81 \cdot 1 - 0.3 \cdot 0$ $= 9.81 \cdot 2.4j + 8j + (-50 + 1.8)k$ OR $M_{A} = (23.5 \text{ N/m})j + (78.5 \text{ N/m})j - (473 \text{ N/m})k$

3.23 S

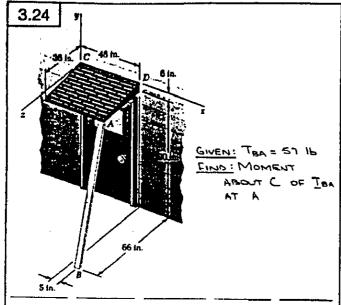
GIVEN: dag = L ft, Tec = L 1b
FIND: MOMENT ABOUT A OF TEC AT B



HOW. $M_A = \sum_{a \in A} \times \sum_{b \in A} (L \sin 45) \frac{1}{2} - (L \cos 45) \frac{1}{2}$ $= \frac{L \ln 4}{2} \left(\frac{1}{2} - \frac{1}{12} \right)$

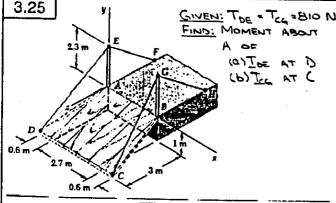
<u> - (2.9708) 글 - i (8016.2)</u>

OR MA =- (254 16-52) - (12.60 16-52) - (12.60 16-52) -



EIRST NOTE. day = ((-5)2+(90)2+(30)2 = 95 in. In = Ton Bh = 50 (-51-901-30E) = 3[-(1416) + (1816) - (416) E] NOW - Mc = [NC = TBA WHERE [NO = (48 m)] + (36 m) + (36 m) + (0.4 cos 40)m Mc = (6)(3) 8 THEN = 18[(L-108)i + (-6-48)j+(144,-1)}] =-(1836 16-14) / (756 16-01) + (258 16-01) /

Me = - (153.0 b. st) + (63.0 1b. st) + (215 b. st) +



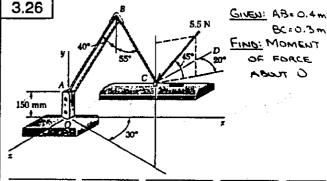
FIRST NOTE: doe = (0.6)2+(33)2+(-3)2 = 4.5 m dea = 1(-0.67+(3.3)2+(-3)2 . 4.5 m THEN TOE + TOE DE + BION (0.61+3.31-38) = 54[(2 N) + (11 N) - (10 N) E) SIMILARLY, Ice = 54[-(2N) - (11 N) - (10 N) E] (a) Now .. MA = TEVA = The WHERE TEN= (2.3m)]

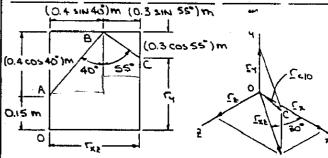
= 2.3j x 54(-2)+11 1 - 10 12) OR MIN = - (1242 N.m) = - (248 N.m) 12 (COMMUNOED)

3.25 CONTINUED

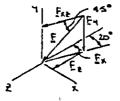
16) HOW - MA - COIX + ICG WHERE TOLK = (2.7 m) + (2.3 m) THEN .. Mx = 54 2.7 2.3 0 = 54[-231 +27] +(29.7+4.4) = }

OR MA =- (1242 N.m) + (1458 N.m) + (1852 N.m) &





HAVE _ [40 = [(0.4 sin 40 + 0.3 sin 55") cos 30]] +[0.15+0.4 cas 40-0.3 cas 55'] j +[(0.4 sm 40+0.3 sm 55°) sm 30°] k = $(0.43549m)_{i} + (0.28434m)_{j}$ + (0.25143m) k



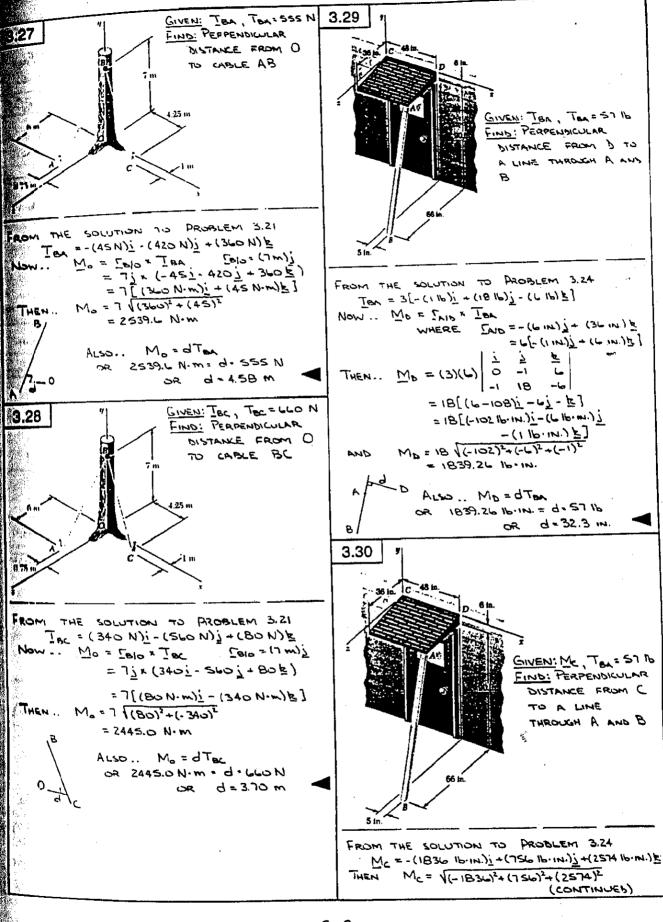
ALSO .. E = 5.5 (- cos +5 sm 20 1 - SIN 45 j

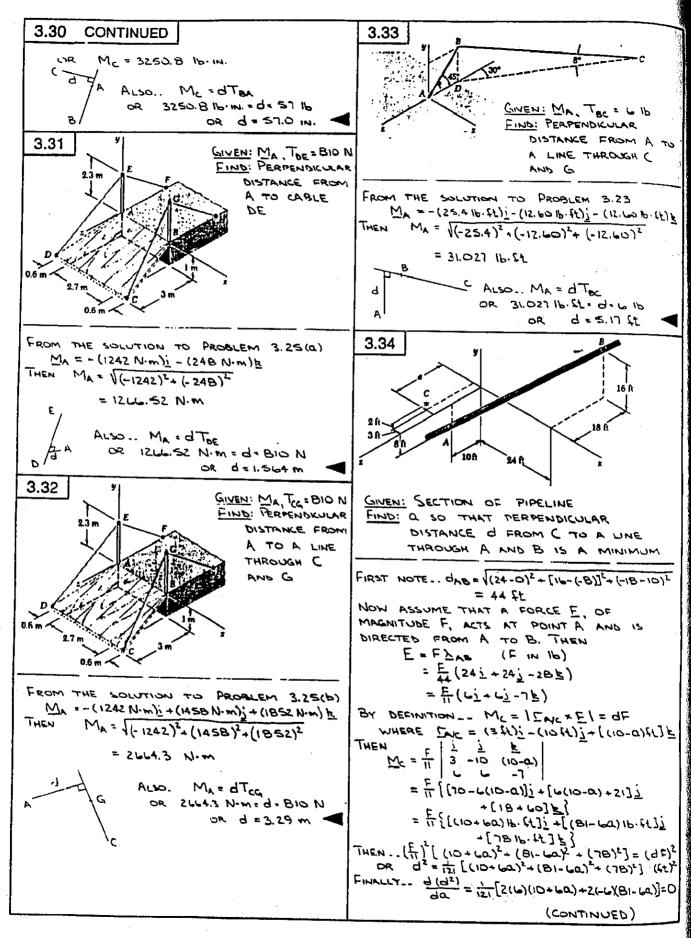
45 COS 20 k) + (05 20 12)

Now .. Mo = Coo x E 0.284 34 0.25143 ୯୦୬ ଅବି = \frac{5}{2} [(0.284 & cos 20 + 0.25143)j

+(-0.25143 sm 20-0.435 49 cos20) + (-0.43549+0.18434 sinzo) E]

OR Mo = (2.02 N·m) i - (1.92L N·m) j - (1.315 N·m) E





CONTINUED 3.34

(10+60) - (81-60)=0 **್** SO THAT FOR OMIN

22 SP.2 = D

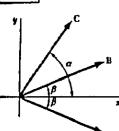
3.35

$$P-\underline{S} = (4\underline{1} + 3\underline{j} - 2\underline{k}) \cdot (\underline{j} + 4\underline{j} + 3\underline{k})$$

= $(4)(1) + (3)(4) + (-2)(3)$
OR $P \cdot \underline{S} = 10$

THUS Q AND & ARE PERPENDICULAR

3.36



GIVEN: B, B, AND C PROVE: COSK COSA = £ cos(x+B) + 2 cos(x-A)

FIRST NOTE.. $B = B(\cos \beta_i + \sin \beta_i)$ B'= B(cospi-sup;) C = C (cosa i + sina i)

BY DEFINITION. B.C = BC cos
$$(\alpha - \beta)$$
 (1)
B'.C = BC cos $(\alpha + \beta)$ (2)

Now B.C = B(cos Bi+ smbj) · C(coski + swaj)

= $BC(\cos\beta\cos\alpha + \sin\beta\sin\alpha)^{-1}$ (3)

B.C = B(corbj- 2mbj)

-C (COSK 1 + SM K)

= BC (cos B cosx - sm B sina) EQUATING THE RIGHT-HAND SIDES OF EQS. (1) AND (2) TO THE RIGHT-HAND SIDES OF EQS. (3) AND (4), RESPECTIVELY, YIELDS $BC \cos(\alpha - \beta) = BC (\cos \beta \cos \alpha + \sin \beta \sin \alpha)$ (5)

BC cos (x+B) = BC (cosp cosx - sup sinx) (6 (5)+(6)=> (05(x-B)+cos(x+B)=2cosBcosa

OR COSK COSB = 2 COS(K+B)+ 2 COS(K-B) €

3.37

GIVEN: GUY WIRES AB AND AC

FIND: ANGLE & FORMED BY AB AND AC

-10.57 MOTE .. AB = ((-6.5)2 + (-8)2 + (2)2 = 10.5 St AC = 1(3)2+(-8)2+(6)2

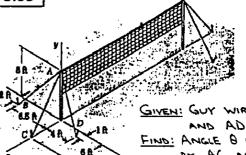
= 10 ft AND AB = - (6.512) - (8 SL) - (2 CD) E

45 = - (8 26)? + (P 69) F BY DEFINITION .. AB. AC = (AB)(AC) cos B OR (-6.51-B1+8k).(-B1+6k)=(10.5)(10)cosB

(-6.5)(0)+(-B)(-B), (2)(6)=105 cos g OR COSB = 0.723 B1

Ð = 43.6°

3.38



GIVEN: GUY WIRES AC

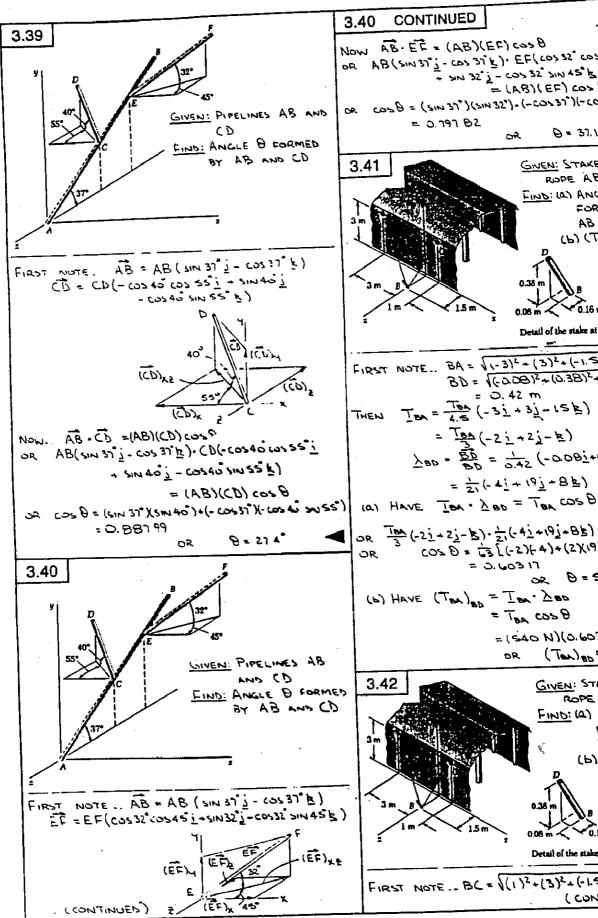
FIND: ANGLE B FORMED BY AC AND AD

FIRST NOTE __ AC = 1(0)2+(-8)2+(C)2 # 01 =

 $AD = \sqrt{(4)^2 + (-8)^2 + (1)^2}$ = 9 ft

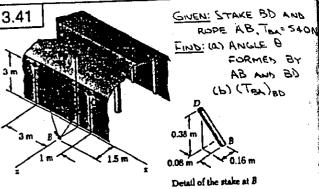
AND AC = - (B St)] + (L St)] AD = (4 + 1) - (8 + 1) + (1 + 1) = CA

BY DEFINITION ... AC. AD = (AC)(AD) cos B OR (-Bj+6k). (4j-Bj+k)= (10)(9) cosB (0)(4) + (-8)(-8) + (6)(1) = 90 cor 8פר ררוב פ בסב אם 0.8E = B DR.



CONTINUED 3.40

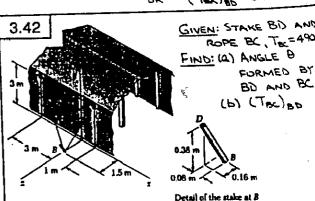
Now AB. EF = (AB)(EF) cos B OR AB(SIN3) 2- COS 3) E). EF(COS 52 COS 45) + NN 32" [- COS 32" NN 45"] $= (AB)(EF)\cos\theta$ OR COSB = (SIN 31°)(SIN 32°)-(-COS37°)(-COS32° SIN 45°) = 0.797 62 B = 37.1°



FIRST NOTE .. BA = V1-312+(3)2+(-1.5)2 = 4.5 m BD = 1(-00012+(0.38)2+(0.16)2 Tex = Tox (-31+31-15k) = Tes (-21+21-k) 180 = BD = 0.42 (-0.081+0.78)+0.161 = \frac{1}{21} (- 4\frac{1}{2} + 19\frac{1}{2} + 8 \frac{1}{2})

OR TEX (-21+21-B) - 1 (-41+191+Bb) = TEX COSB COS B = 63[(-2)+4)+(2)(19)+(-1)(18)] = 0.603 IT 02 B = 52.9°

(b) HAVE (TON) = Im. ZOD = TBA COSB = (SAO N)(0.603 M) (Tex) 80 = 326 N



FIRST NOTE .- BC = \((1)^2 + (3)^2 + (-1.5)^2 = 35 m (CONTINUED)

8.42 CONTINUED

BD= V(-0.08)2+(0.38)2+(0.16)2 = 0.42 m Tex = Tex (1+31-45E)

THEN = Imc (5;+4;-3F)

 $\underline{\lambda}_{BD} = \frac{8\overline{D}}{BD} = \frac{1}{0.42} (-0.08\underline{i} + 0.38\underline{i} + 0.16\underline{k})$

= = (-41+191+8=)

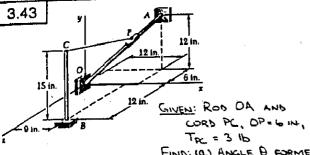
(a) HAVE TOC . A BO = TEC COS 0

DR Te: (21+61-38)-21(41-191-81)=Tec cos8 COLD = 1/47 [(2)(-4)+(6)(19)+(-3)(B)]

= 0.55782

B=56.1°

(b) HAVE (TOC) BD = IBC - 185 = (490 N)(0.557 BZ) or (Tec) By= 273 N €



FIND: (a.) ANGLE & FORMES BY OA AND PC (b) (Tre)OX

FIRST NOTE .. OA = \((12)^2 + (12)^2 + (-6)^2 = 18 IN. THEN .. DON = OA = IB (121+121-68)

= 3(2<u>i+2j-k)</u>

Now OP=6 in. => OP= \$(DA)

.. THE CODRDINATES OF POINT P ARE (4 m, 4 m, -2 m)

PC = (5 m.) i + (11 m) j + (14 m.) k TAHT OC PC = V(5)2+(11)2+(14)2 = (342 m.

(a) HAVE. PC- > on = (PC) cos B

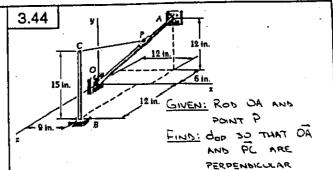
OR (51+111+14 k) - 3(21+21-k) = 1342 cos B

cos 8 = 3/342 [(5)(2)+(11)(2)+(14)(-1)]

= 0.324 44

B = 71.1°

(b) HAVE .. (The) = The · LON = (TAC) PC) · NOA = TPC PC · Zox = TPC COSB = (3 16) (0.324 44)OR (TPC) ON = 0.973 16



FIRST NOTE .. DA = V(12)2+(12)2+(-6)2 = 18 IN THEN - DA = DA = 18 (121-121-6E) = 3(21+21-12)

LET THE COURDINATES OF POINT P BE (XIM, YIM, ZIM.). THEN PZ = [(9-x)m.]: + [(5-7)m.]; + [(12-2)m] } OP = dop 10A = dop (21+21-1) Auso,

JOB = (XIM) + (MIM) = (8 M) = :. X= 3dop 4 3dop_ 2 = -3dop THE REQUIREMENT THAT OA AND PC BE PERPENDICULAR IMPLIES THAT

Fax. bg =0 OR 13(21+21- E). [(9-x) + (15-4)1. (12-2) E) + 0 OR (2)(9-3dop) +(2)(15-3dop) +(-1)[12-(-1 dop)]10 900 = 15 W

3.45 GIVEN: VECTORS P. Q. AND S FIND: VOLUME OF THE PARALLELOGRAM DEFINED BY P.Q. KNDS WHEN

(a) P=41-31+2B <u>Q = -21 - 51 + E</u> Z = JJ + J - F

(P) 5 - 27 - 7 + PF Q = 21 + 31+ k 5 = -3i - 2j + 4 B

AS EXPLAINED IN SEC. 3.10, THE VOLUME V OF THE PARALLELOGRAM IS GIVEN BY N=15-(0x2)

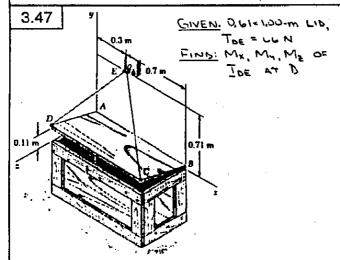
(a) HAVE E- (0-2) = | -5 -2 1 = 20 -21-4+70 +6-4 : N-47

(b) HAVE B. (3x2) = | 5 3 = 60+3-24+54+8+10 :. V= 111

GIVEN: P = 31 - 1+ 1 3.46 Q + 41 + Q41 - 2E 5 = 21 - 25 + 2 E FIND: DY SO THAT P. Q. AND S ARE COPLINAR

IF P. Q. AND & ARE COPLANAR, THEN P MUST BE PERPENDICULAR TO (Q+ 2). ∴ P. (3.5).0 (OR , THE VOLUME OF THE PARALLELOGRAM DEFINER BY P. W. AND & IS BERD). THEN 4 0-4-5 - O -2 2 604 + 4 - B - 204 + B - 12 =0

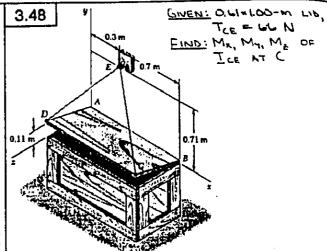
D-4 = 2



FIRST NOTE .. 2 = ((0,41)2-(0.11)2 = 0.60 m

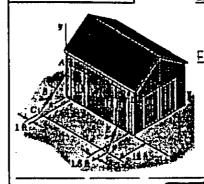
doE = 1(0.3)2 - (06)2+(-0.6)2 = 0.9 m THEN AND TOE = (0N (0.31 + 0.6) - 0.6) = 22 [(1 N) 1 + (2 N) 1 - (2 N)]

Now_ Mx = IDIX x TOE [MY = (0.11 W)] + (0.00 W) F THEN .. MR = 22 =- (31.24 N·m) + (13.20 N·m); - (2.42 N·m) k : Mx =-31.2 N·m, My=13.20 N·m, M3=-2.42 N·m THEN . TAB = TAB (-1-12)+12 k) (16)



FIRST NOTE ... Z = 1(0.61)2 - (0.11)2 = 0.60 m dce = 1(-0,712+(0,6)2+(-0,6)2 = 1.1 m THEN Ice = - (-0.7 1+0.61-0.62) AND = C[-()N) + (6N) - (6N) E] Now--MA = CEIN * TLE WHERE TEIN : (0.3 m) + (0.71 m) THEN .. Mx = 6 0.3 0.71 = 6[-4.261+1.81+(1.8+4.97)5] =- (25.56 N·m); - (1080 N·m); + (40.62 N·m) k

: Mx = -25,6 N·m, My = 10.80 N·m, Mz=40.6 N·m 3.49 and 3.50



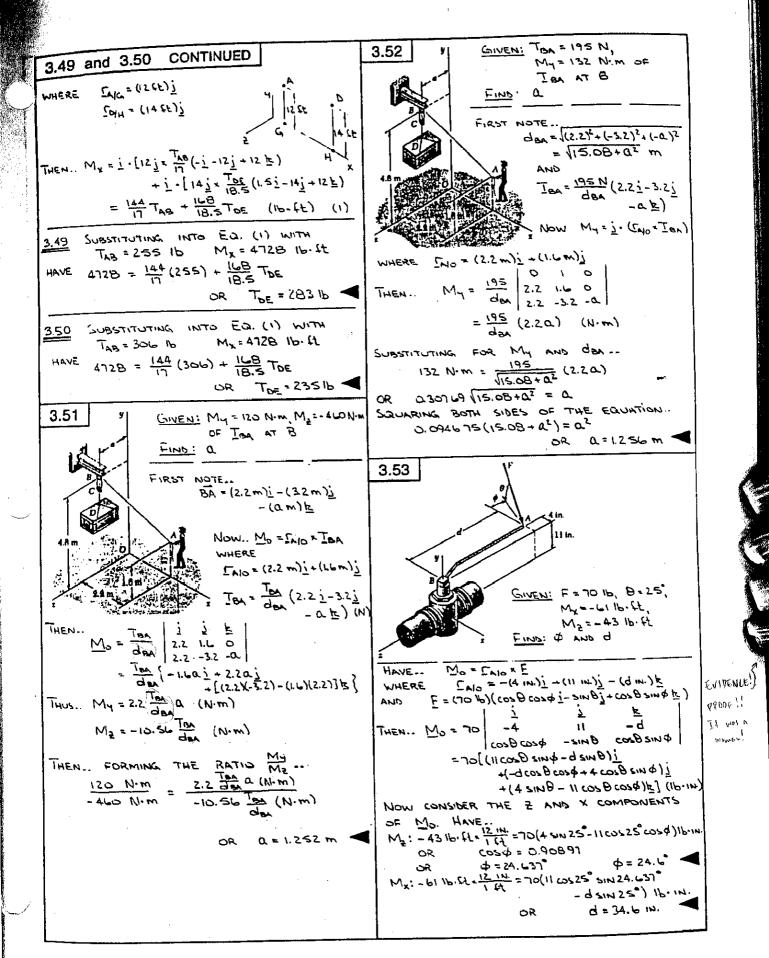
GIVEN: THE, MX OF OHA (A TA) BAT IDE (AT D) = 4728 1b.ft FIND: TDE

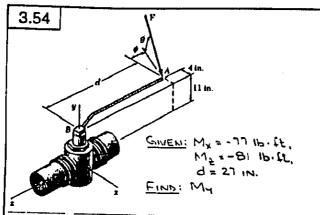
FIRST NOTE .. dAC = \((-1)^2 + (-12)^2 + (12)^2 = 17 ft dDF = V(1.5)2+(-14)2+(12)2 = 18.5 \$1

THEN ..
$$T_{AB} = \frac{1AB}{17} (1.5i - 14i + 12k)$$
 (16)

Now. Mx = ([([No + The) + i · ([Soly * The)

(CONTINUED)





Mo = CAID = E [Alo = - (4 IN.)] + (11 IN)] - (27 IN.)] E = F(cosBcospi-smoj+cosBsmok) AND THEN .. M. = F COSB COSO - SINB COSB SIND = F[(11 cos 8 sin 4 - 27 sin 8); + (-27 cos8 cos4 + 4 cos8 sin4)j + (4 SINB - 11 COSB COS\$)] (15 IN) TAMT OC $M_x = F(11\cos\theta\sin\phi - 27\sin\theta)$ $M_{\gamma} = F(-27\cos\theta\cos\phi + 4\cos\theta\sin\phi)$ (2) $M_2 = F(4 \sin \theta - 11 \cos \theta \cos \phi)$ WHERE Mx. My. AND Mz ARE IN 16.14. Now. ED (1) => COSB SNP = 11 (Mx + 27 SINB)

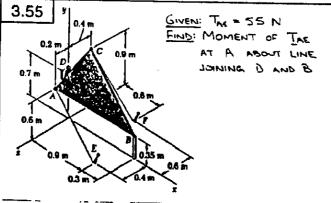
Eq. (3)=> $\cos \theta \cos \phi = \frac{1}{11} \left(4 \sin \theta - \frac{M_2}{F} \right)$ (5) Substituting Eqs. (4) AND (5) into Eq. (2) YIELDS

 $M_{4} = F_{1}^{f} - 27 \left[\frac{1}{11} (4 \sin \theta - \frac{M_{e}}{F}) \right] + 4 \left[\frac{1}{11} (\frac{M_{e}}{F} + 27 \sin \theta) \right]$ $= \frac{1}{11} (27 M_{e} + 4 M_{e})$

Noting that the RATIOS II AND II ARE THE RATIOS OF LENGTHS, HAVE.

 $W^{A} = \frac{11}{5J} (-81 \text{ IP} \cdot tf) + \frac{11}{4} (-JJ \text{ IP} \cdot tf)$

OR My =- 227 16.51



FIRST NOTE.. $d_{NE} = \sqrt{(0.9)^2 + (-0.4)^2 - (0.2)^2} = 1.1 \text{ m}$ THEN.. $T_{NE} = \frac{55 \text{ N}}{1.1} (0.9 \frac{1}{2} - 0.6 \frac{1}{2} + 0.2 \frac{1}{2})$ $= 5[(9 \text{ N}) \frac{1}{2} - (1.1 \text{ N}) \frac{1}{2} + (2 \text{ N}) \frac{1}{2}]$ (CONTINUES)

3.55 CONTINUED

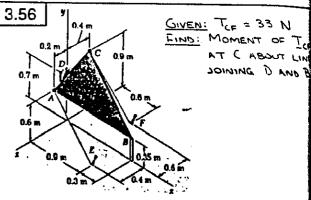
ALSO.
$$DB = \sqrt{(1.2)^2 + (-0.35)^2 - (0)^2} = 1.25 \text{ m}$$

THEN $\Delta DB = \frac{DB}{DB} = \frac{1.25}{1.25}(1.2\underline{i} - 0.35\underline{i})$
 $= \frac{1}{25}(24\underline{i} - 7\underline{i})$

Now.
$$M_{BB} = \frac{1}{2} B \cdot (\frac{1}{14} A \times \frac{1}{14} B)$$

WHERE $\frac{1}{14} B = -(0.1 \text{ m}) \frac{1}{2} + (0.2 \text{ m}) \frac{1}{2}$
THEN. $M_{BB} = \frac{1}{25} (5) \begin{vmatrix} 24 & -7 & 0 \\ 0 & -0.1 & 0.2 \\ 9 & -6 & 2 \end{vmatrix}$
 $= \frac{1}{5} (-4.8 - 12.6 + 28.8)$

OR Mbg = 2.28 N·m



FIRST NOTE..
$$d_{CE} = \sqrt{(0.6)^2 + (-0.9)^2 + (-0.2)^2} = 1.1 \text{ m}$$

THEN. $T_{CE} = \frac{33 \text{ N}}{1.1} (0.6 \frac{1}{2} - 0.9 \frac{1}{2} - 0.2 \frac{1}{2})$
 $= 3[(C N) \frac{1}{2} - (9 N) \frac{1}{2} - (2 N) \frac{1}{2}]$

ALSO.. $DB = \sqrt{(12)^2 + (-0.35)^2 + (0.5)^2} = 1.25 \text{ m}$

ALSO..
$$DB = \sqrt{(12)^2 + (-0.35)^2 + (0.5)^2} = 1.25 \text{ m}$$

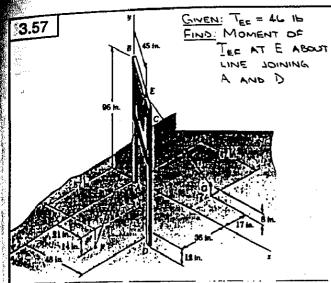
THEN $\Delta DB = \frac{DB}{DB} = \frac{1}{1.25} (12i - 0.35i)$
 $= \frac{1}{25} (24i - 7i)$

WHERE
$$\frac{1}{500} = \frac{(0.2 \text{ m})_{\frac{1}{2}}}{24} - \frac{(0.4 \text{ m})_{\frac{1}{2}}}{0}$$

THEN.. $M_{08} = \frac{1}{25} \frac{(3)}{3} \begin{vmatrix} 24 & -7 & 0 \\ 0 & 0.2 & -0.4 \\ 0 & -9 & -2 \end{vmatrix}$

$$= \frac{3}{25} \left(-9.6 + 16.8 - 86.4\right)$$

OR Mos = -950 N·m



FIRST NOTE THAT $BC = (4B)^2 \cdot (36)^2 = 40$ in and that $BE = \frac{45}{40} = \frac{2}{4}$ The coordinates

OF POINT E ARE THEN (\$48,96, \$136) OR (36 IN, 96 IN, 27 IN.). THEN ..

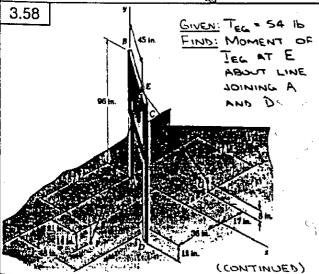
der = ((-15)2+ (-110)2+(30)2 = 115 in.

THEN .. TEE = 46 b (-151-1101 + 30 k)

 $= 2\left[-(3 \ln 1) - (22 \ln 1) + (6 \ln 1)\right]$ ALSO -- AD = $(48)^2 + (-12)^2 + (36)^2 = 12 \cdot (26 \ln 1)$ THEN $\lambda_{AD} = \frac{AD}{AD} = \frac{1}{12\sqrt{2L}} (4B_2 - 12\underline{1} + 36\underline{E})$ = = (4i-j-3k)

NOW -. MAD = XAD . (TELA & TEE) THEN. MAD = 120 (2) 36 96 27 -3 -22 6 = 2 (2304+81-2576-84-216-2576)

OR MAN : 1359 16.14.



3.58 CONTINUED

FIRST NOTE THAT BC = $\sqrt{(4B)^2+(3L)^2}$ = 60 in.

AND THAT BC = $\frac{45}{45}$. THE COORDINATES OF

POINT E ARE THEN (3+48, 96, 3:36) 00 (36 in, 96 in, 27 in). THEN ... $\phi_{\epsilon} = \sqrt{(11)^2 + (-88)^2 + (-44)^2} = 99 in$

THEN .. TEG = 99 (11: 881-44)

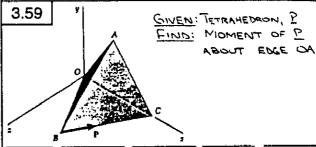
= [(1 1b): - (8 1b): - (4 1b) E]
ALDO. AD = V(4B)2 + (-12)2 + (36)2 = 12 (26 10. THEN LAS = AD = 12(26 (481-121+3612)

= 点 (4<u>i</u> - j + 3<u>k</u>)

NOW -. MAS = LAS · (TEX = TEX) WHERE SEIN = (36 in.) + (96 in.) + (27 in.) k

THEN MAN = 17 (6) 36 96 27 = 126 (-1536-27-864-288-144-864)

OR MAD=-2350 16-1N.



FIRST CONSIDER TRIANGLE OBC. WITH THE LENCTH OF THE SIDES OF THE TRIANGLE EQUAL TO Q, HAVE. BC = a cos boj - a sin to k $\overline{Y} = \frac{5}{5}(\overline{1} - \sqrt{2} \overline{K})$ AND P = P>B = P (i - 13 k)

TO DETERMINE DOW, FIRST OBSERVE THAT KAOC = 60. THE PROJECTION OF DA ON THE X AXIS IS THEN

(DA) = a cos 60 = 2 ALSO, THE PROJECTION OF OA ONTO THE X2 PLANE BISECTS & BOC, WHERE & BOC

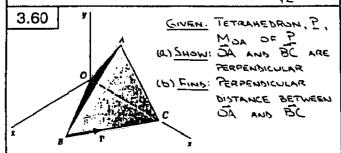
= 60°. THEN, EROM THE EXETCH .. (OA) = (OA) x TAN 30 = 213 $\chi(AO)$ NOW .. (OA)2 = (OA)2 + (OA)2 - (OA)2 (40) $\frac{2}{\alpha^2} = \left(\frac{\alpha}{2}\right)^2 + \left(\frac{\alpha}{2}\right)^2 + \left(\frac{\alpha}{2}\right)^2$

THEN .. OA = 21 + 0131 + 213 1 THAT DOR = \$1 + 12 + 7 E

(CONTINUED)

3.59 CONTINUED

FINALLY.. $M_{OA} = \frac{1}{2}OA \cdot (\frac{1}{2}C_{1O} \cdot \frac{P}{P})$ WHERE $\frac{1}{2}C_{1O} = \frac{1}{2}$ THEN.. $M_{OA} = \frac{1}{2}(\frac{P}{2})$ $\frac{1}{2}\sqrt{3}$ $\frac{1}{2}(\frac{1}{3})$ $\frac{1}{2}\sqrt{3}$ $\frac{1}{2}\sqrt{3}$



To determine \overrightarrow{OA} , first observe that \overrightarrow{AAC} = 60. The projection of \overrightarrow{OA} on the X Axis is then $(\overrightarrow{OA})_X = 0$ (02.60 = $\frac{2}{2}$

ALSO, THE PROJECTION OF OA ONTO THE X2 PLANE BISECTS & BOX, WHERE & BOX = 60. THEN, FROM THE SKETCH.

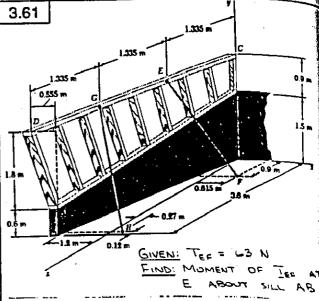
THUS, BC.OA = & (i-13k).[&i.(OA),i.26k] 3.62

: BC · OA = 0 ⇒ BC MO CC ME PERPENDICUM ◀

(b) Since \overrightarrow{OA} is perpendicular to \overrightarrow{BC} , and thus to \overrightarrow{P} , it follows that $M_{OA} = dP$ where d is the perpendicular

WHERE d is the Perpendicular distance between OH and BC and From the Solution to Problem 3.59 $M_{OA} = \frac{1}{12} QP$

THEN.. $\frac{1}{\sqrt{2}} QP = dP$ OR $d = \frac{Q}{\sqrt{2}}$



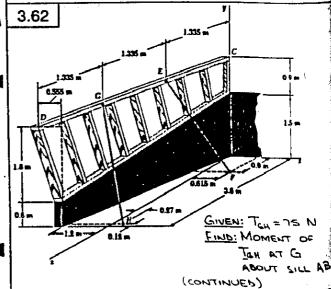
FIRST NOTE THAT $(E = \frac{1}{3}(D))^2$ THEV... $dec = \int \left[\frac{1}{3}(0.555 + 1.2) + 0.615 \right]^2 + (-2.4)^2 + \left[0.9 - \left(\frac{1}{3} \times 3.6 \right) \right]^2 \right]^2 = 0.7 \text{ m.}$ $= \sqrt{(1.2)^2 + (-2.4)^2 + (-0.3)^2} = 2.7 \text{ m.}$ AND $Tec = \frac{63}{2.7} \cdot (1.2 - 2.4 - 0.3 - 2) = 0.3 \text{ m.}$ = 7[(4 N) - (8 N) - (1 N)

NOW... MAB = \(\lambda AB = \left(\frac{\(\Gamma_{FIB} \times \frac{\(\Gamma_{FIB} \)}{\(\Gamma_{FIB} \)} \right) \left(\Gamma_{FIB} \)

WHERE \(\Gamma_{FIB} = \left(\Gamma_{FIB} \) \right) \(\frac{4}{3} \) = 12 \\

1 HEN \(\text{HEN} \). \(MAB = \frac{1}{3} \left(\Gamma_{FIB} \)) \(\frac{4}{4} \) = 8 \\

= \frac{1}{3} \left(\Gamma + \Gamma_{FIB} + \Gamma_{FIB} \) \(\Gamma_{FIB} \) = 18.57 \(\Gamma_{FIB} \)



3.62 CONTINUED

FIRST NOTE THAT (G = 3 CD don = [[2 (0.555+1.2)+0.27] 2+ (-2.4)2 +[(3,6-0.12)-(3,3.4)]2 = \((1.44)2+(-2.4)2+(1.0B)2 - 3 m and ICH = 75N (1.441-2.41+1.08 12) [3 (12 N) - (20 N) + (9 N) E] ALSO. AB = V(1.2)2+(0.9)2+(-3.6)2 = 3.9 M THEN .. \$48 = 3.9 (1.21 + 0.9) - 36 12) = = (4i + 3 i=12 12 12) MAB = ZAB · ([HIN TCH)

WHERE [HA = (1.47 m) - (0.6m) - (0.12 m) h $M_{AB} = \frac{1}{13}(3)$ 1.47 -0.6 -0.12 THEN .. = (3 (-216-4.32+352.8-86.4-39.69-96) MAB = 44.1 N.m

3.63 GIVEN: FORCES F. AND F., F. = F2 = F SHOW: ML OF FZ = MZ, OF E

/ FIRST NOTE THAT

FIRST NOTE THAT

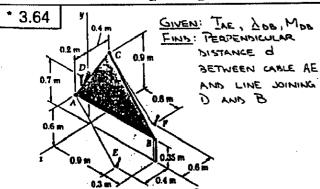
FIRST NOTE THAT ١ž,

Now, by DEFINITION.. $M_{\underline{\lambda}_1} = \underline{\lambda}_1 \cdot (\underline{C} \times \underline{F}_2)F$

 $W_{\overline{Y}^2} = \overline{Y}^3 \cdot (-\overline{L} \times \overline{Y}') E$ $= \overline{Y}^3 \cdot (-\overline{L} \times \overline{E}')$

Using Ea. (3.39) \(\tilde{\chi_2}\cdot\(-\frac{\chi_2}{\chi_2}\) = \(\frac{\chi_1}{\chi_2}\cdot\(-\frac{\chi_2}{\chi_2}\)) Mx = 7. (C = 72)E TAHT CZ

: Mx . Mx2



FROM THE SOLUTION TO PRUBLEM 3.55 .. The = 55 N, The = 5[(9 N): - (L N) + (2 N) +] Mog= 2.28 N·m > DB = 25 (241-71) BASES ON THE DISCUSSION OF SEC 3.11, IT (CONTINUES)

CONTINUED 3.64

COLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF THE WILL CONTRIBUTE TO THE MOMENT OF THE ABOUT LINE DB. NOW (TAE) PARALLEL = TAE · 108 = 5(91-61+2k). 25 (241-71)

= = [(9)(24) + (-6)(-7)]

ALSO. THE = (THE) PARKLLEL + (THE) DERR SO THAT (TAE) PERP = V(SS)2- (SIL)2 = 19.0379 N

SINCE LOB AND (TAE) PERP. ARE PERPENDICULAR, IT FOLLOWS THAT

MOB = d(TAE) PERP. 02 2.28 N·m = d · 19.0379 N

d=0.1198 m -

ALTERNATIVE SOLUTION

LET THE PERPENDICULAR LINE, DRAWN FROM LINE DB TO THE LINE OF ACTION OF TAE. BE REPRESENTED BY

d = xi + 4) + 2 k X,4,2 in m Now .. d I The = d. The = D OR (x1+71+21). 5(91-61+21) =0 9x-64-22.0

可下了PB → 可·ブDB * 0 AND OR (xi-4j-2k). 25 (24j-7j)=0

OR 24x-74=0 => 4= 24x (2) 9x-6(24x)-22=0 => 2= 81x (3)

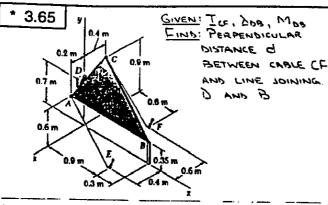
NOW - Mas = JOB . (dx TAE) -7 O 24 = = = (4By -632+14x+1442) = = (4B4 + 14x + B1 2)

SUBSTITUTING FOR MAS AND USING EQL (2)

AND (3) YIELDS ... 2.28 = = = [48(24x)+14x+81(4x)] OR X= 0.017 614 M

M 182 0000 = 4 (2) AND THEN (3) => 2 -0.10199 W

FINALLY, d= (x2+42+22 =[(0,017614)2+(0,060391)2+(0,101909)2]2 or d=aligem



FROM THE SOLUTION TO PROBLEM 3 56 .. Ter = 33 N Ter = 3[(6N)= (9N); - (2N) k] IMOBI= 9.50 N·m 208 = = = (241-72)

BASED ON THE DISCUSSION OF SEC. 3.11 IT FULLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF ICE WILL CONTRIBUTE TO THE MOMENT OF ICE ABOUT LINE DB. NOW.. (ICE) PARALLEL = ICE . Y DB

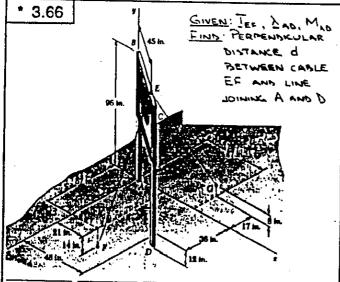
= 3(6 - 9 - 2 k) - 2 < (24 - 7) $=\frac{2}{2} \left[(-1)(24) + (-9)(-1) \right]$ = 24.84 N

ALSO. ICF = (ICF) PARALLEL - (ICF) DERP. SO THAT (TLE) PERP = 1(33)2-(24.84)2

= 21.725 N SINCE LOB AND (TCF) PERP. ARE PERPENDICULAR, IT FULLOWS THAT

IMDEL = d(TCF) PERP 9.50 N·m = d + 21.725 N

OR 0 = 0 437 m FOR A SECOND METHOD OF SOLUTION, SEE THE SOLUTION TO PROPLEM 3.64.



FROM THE SOLUTION TO PROBLEM 3.57 .. TEE = 46 16 TEE = 2[-(316)i-(2216)j+(616)k] THUS, (TEG) PERP = TEG = 54 16 (CONTINUES)

CONTINUED 3.66

MAD = 1359 16.14. DAD = (20 (4)-1-3+3E)

BASED ON THE BISCUSSION OF SEC. 3.11, IT FOLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF TEE WILL CONTRIBUTE TO THE MOMENT OF IEE ABOUT LINE AB. NOW (TEF) PARALLEL = IEF. ZAD

= 2(-31-221-61). 126(41-143) = (26/6-3)(4)+(-22)(-1)-(6)(3)] = 10.9825 1b

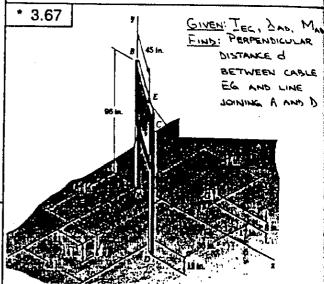
ALSO. TEC = (TEF) PARALLEL + (TEC) PERP 50 THAT (TEF) PERR = 1 (46)2- (10.9825)2

= 44, 470 16

SINCE LAD AND (TEF) PERP. ARE PERPENDICUL IT FOLLOWS THAT

MAN = d(TEF)PERP. 1359 16.1M. = d = 44.670 16

OR "3 = 304 IN FOR A SECOND METHOD OF SOLUTION, SEE THE SOLUTION TO PROBLEM 3.64.

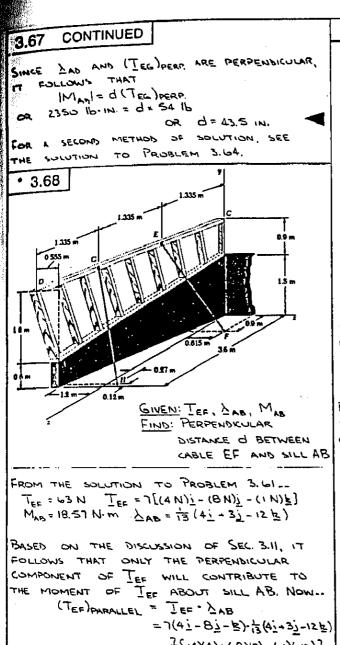


FROM THE SOLUTION TO PROBLEM 3.58 ... TEG = 54 16 TEG = 6[(1 16): - (8 16); - (4 16) 1] IMAN = 2350 16. IN. DAS = (41-1-3+35)

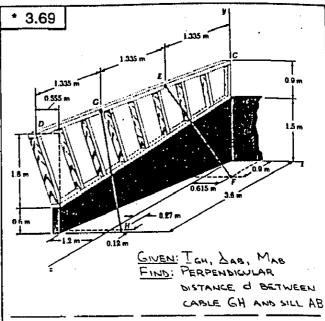
BASED ON THE BISCUSSION OF SEC. 3.11, IT FOLLOWS THAT DALY THE PERPENDICULAR COMPONENT OF TEG WILL CONTRIBUTE TO THE MOMENT OF TEC ABOUT LINE AD. NOW (TEG) PARALLEL = TEG . LAD

= 6(1-81-4k). (21(41-1-3k) = (=[(1)(4)+(-8)(-1)+(-4)(3)]

(CONTINUED)



 $= \frac{1}{3} (4)(4) + (-8)(3) + (-1)(-12)$ = 2.1538 N ALSO. TEF = (TEF) PARALLEL + (TEF) PERR SO THAT (TEF) PERO = V(63)2-(2.1538)2 = 62,963 N SINCE JAB AND (TEF) PERR ARE DERIENDICULAR, IT FOLLOWS THAT MAD = d(TEF) PERP OR 18.57 N·m = d = 62.963 N OR d=0.295 m FOR A SECOND METHOD OF SOLUTION, SEE THE SULUTION TO PRUBLEM 3.64.



FROM THE SOLUTION TO PROBLEM 3.62 .. TGH = 75 N TGH = 3[(12 N)1- (20 N)1+(9 N)]

BASED ON THE DISCUSSION OF SEC. 3.11, IT FOLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF IGH WILL CONTRIBUTE TO THE MOMENT OF ICH ABOUT SILL AB. NOW .. (TGH) PARALLEL = TGH . YAB

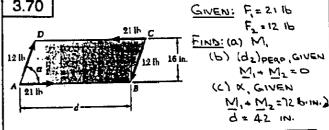
= 3(121-50]+0F). 17(4;+31-15F) = 13 ((12)(A)+(-2)(3)+(P)(-12)] =-27.492 N

ALSO. IGH = (IGH) PARALLEL - (IGH) PERP. SO THAT .. (TOH) DERP. = V(75)2-(-27.692)2 = 49.700 N

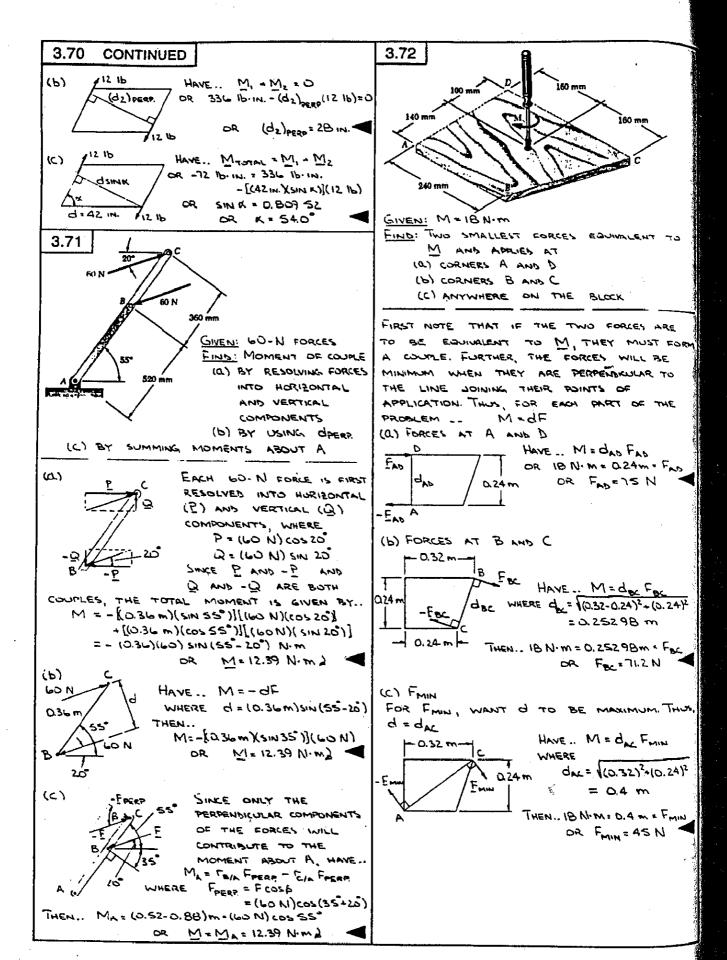
SINCE LAB AND (TGH) PERP. ARE PERPENDICULAR, IT FOLLOWS THAT MAB = d(TGH) DERD.

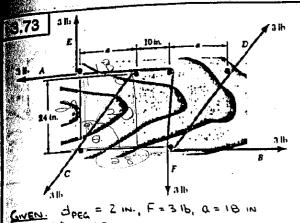
> 44.1 N·m - d. 69.700 N OR d=0,633 m

FOR A SECOND METHOD OF SOLUTION SEE THE SOLUTION TO PROBLEM 3.64.



(a) HAVE W' = 9'E' WHERE d, = 16 IN. = (16 m. X21 16) M, = 336 16.14.) (CONTINUED)





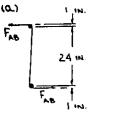
GWEN: DPEC = 2 IN., F = 3 Ib, Q = 18 IN

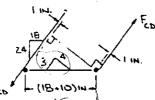
FIND: M FOR

(Q) WIRES AB AND CD

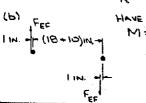
(B) WIRES AB, CD, AND EF

In General, $M = \sum dF$, where d is the perpendicular distance between the lines of action of the two forces acting on a given wire.

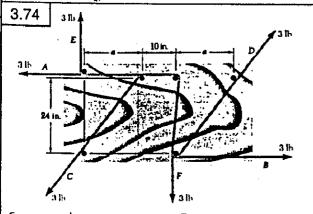




HAVE .. M = drafab + dcafcb = (2+24)m. = 3 1b + (2+1)+28)m. = 31b 18 OR M=151.2 1b.1N.)



M=[das Fas + desFes] + der Fee = 151.2 16.11. - 28 10.2316 DR M= 67.2 16.11.3



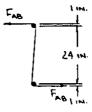
GIVEN: OPEG = 2 m., FAB = FOD = 3 lb., M = 159.6 lb.m.)

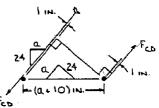
FIND: amin

HAVE.. M = das Fas + do Fco (CONTINUED)

3.74 CONTINUED

WHERE day and do are the perfeudicular distances between the lines of action of the forces action on wires AB and CD, respectively.





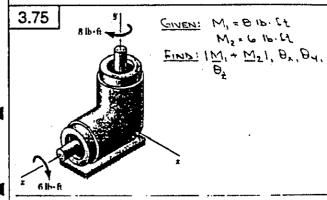
THEN. 159.6 16.1N. = $(2 \cdot 24) \text{ in. * 3 lb}$ + $\left[2 + \frac{24}{(24^2 + \Omega^2)} (0 + 10)\right] \text{ in. * 3 lb}$

or 25.2 =
$$\frac{24(0+10)}{\sqrt{576+02}}$$

OR (25.2)2(576+02) = (576)(0+10)2 OR 59.0402-11 5200+308183=0

OR $Q = \frac{11520 \pm \sqrt{(-11520)^2 - 4(59.04)(308.183)}}{2(59.04)}$

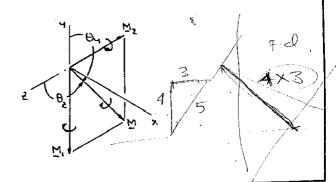
SOLVING YIELDS. Q=32.0 IN. Q=163.1 IN. TAKING THE SMALLER ROST. Q=32.0 IN.

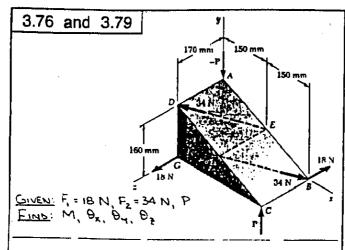


HAVE - M = M, = M2 = - (B 16. FU) - (6 16- FE) K

THEN .. M = \((0)^2 + (-8)^2 + (-6)^2\)
OR M = 10 16. Ft

AND $\cos \theta_{x} = 0$ $\cos \theta_{y} = -\frac{\theta}{10}$ $\cos \theta_{z} = -\frac{b}{10}$ or $\theta_{x} = 90$ $\theta_{y} = 1431$ $\theta_{z} = 126.9$





HAVE. $M = M_1 - M_2 - M_3$ WHERE $M_1 = \Gamma_{C|C} \times F_1 = (0.3 \text{ m})_1 \times [-(18 \text{ N}) \text{ K}]$ $= (5.4 \text{ N·m})_2$ WHERE $\Gamma_{F|E} = (0.17 \text{ m}) \text{ K}$ AND $G_{EB} = \sqrt{(0.15)^2 + (-0.08)^2 + (-0.17)^2}$ = 0.17(2 m)THEN $F_2 = \frac{34 \text{ N}}{0.17(2)}(0.15\frac{1}{2} - 0.08\frac{1}{2} - 0.17 \text{ K})$ $= \{2[(15 \text{ N})_2 - (8 \text{ N})_2 - (17 \text{ N}) \text{ K}]\}$ so that $M_2 = 0.17 \text{ K} \times \{2(15\frac{1}{2} - 8\frac{1}{2} - 17 \text{ K})\}$ $= \{2[(1.3 \text{ N·m})_2 + (2.55 \text{ N·m})_2]\}$ $M_3 = \Gamma_{C} \times P = [(0.3 \text{ m})_2 + (2.17 \text{ m}) \text{ K}] \times P_2$ $= P(-0.17\frac{1}{2} + 0.3 \text{ K}) \quad (N \text{ m})$

3.76 P=0 : $M = M_1 + M_2$ OR $M = (5.4) + \sqrt{2}(1.36i + 2.55)$ = (1.923.33 N - m) + (9.0062 N - m)Then. $M = \sqrt{(1.925.33)^2 + (9.0062)^2 + (0.0)^2} = 9.2093 N - m$ OR M = 9.21 N - mAnn. $\Delta_{M/2} = M = 0.208 BS_1 + 0.97795$

THEN.. (050, 0.208 85 COS By = 2977 95 COS B_ = 90 4

3.14 P=20 N : M= M,+ M, + M,

OR M= (1.923 33 i+ 9.0062 j) + 20(-0.17 i+0.3 k)

=-(1.47667 N·m)i+(9.0062 N·m)j+(6.44m)k

THEN. M= ((-147667)2 + (9.0062)2 + (6)2 = 10.9221 N·m

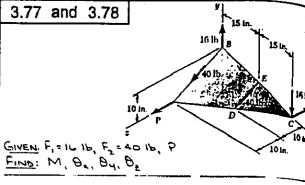
OR M=10.92 N·m

AND DAKE M=-0.1352001+082459j+0.54934k

THEN...

COS Ox = -0.135200 COSOy=082459 COSO2:0.54934

SO THAT Ox + 97.8° Dy=34.5° O2:567° ◀



HAVE.. $M = M_1 + M_2 - M_3$ WHERE $M_1 = C_1 \times F_1 = (30 \text{ m.}) \cdot \times [-(16 \text{ lb}) \cdot j]$ $= -(480 \text{ lb·m.}) \cdot k$ $M_2 = C_{EIB} = F_2$ WHERE $C_{EIB} = (15 \text{ m.}) \cdot (-(5 \text{ m.}) \cdot j)$ AND $C_{DE} = \sqrt{(5)^2 + (-5)^2 + (-10)^2} = 5(5 \text{ m.})$ THEN.. $F_2 = \frac{40 \text{ lb}}{5(5)} (5j - 10 \cdot k)$ $= 8(5(1 \text{ lb}) \cdot j - m(2 \text{ lb}) \cdot k)$

$$= (305)^{\frac{7}{2}} \qquad (10 \cdot 10)$$

$$= (205)^{\frac{7}{2}} \qquad (10 \cdot 10)^{\frac{7}{2}} \times (-5)^{\frac{7}{7}}$$

THEN. M = V(178.885)2+(536.66)2+(-211.67)2
= 603.99 16.10.

AND DANG = M = 0.296 171 + 0.888 521 - 0.350 45 B THEN.

 $\cos \theta_{x} = 0.29617$ $\cos \theta_{y} = 0.898 \le 2$ $\cos \theta_{z} = 0.3504$ $\cos \theta_{x} = 0.29617$ $\cos \theta_{y} = 27.3$ $\cos \theta_{z} = 10.5$

3.78 P= 20 16 : M = M, + M2 + M3

OR M = - (480) & + 8 & (10 i + 20 i + 15 &)

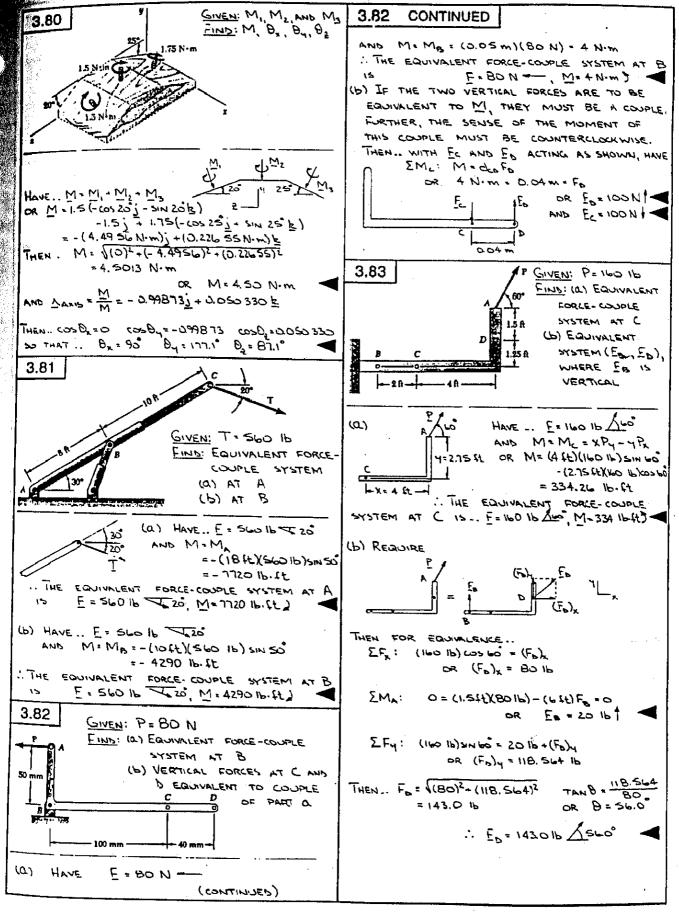
+ (30 = 20) i

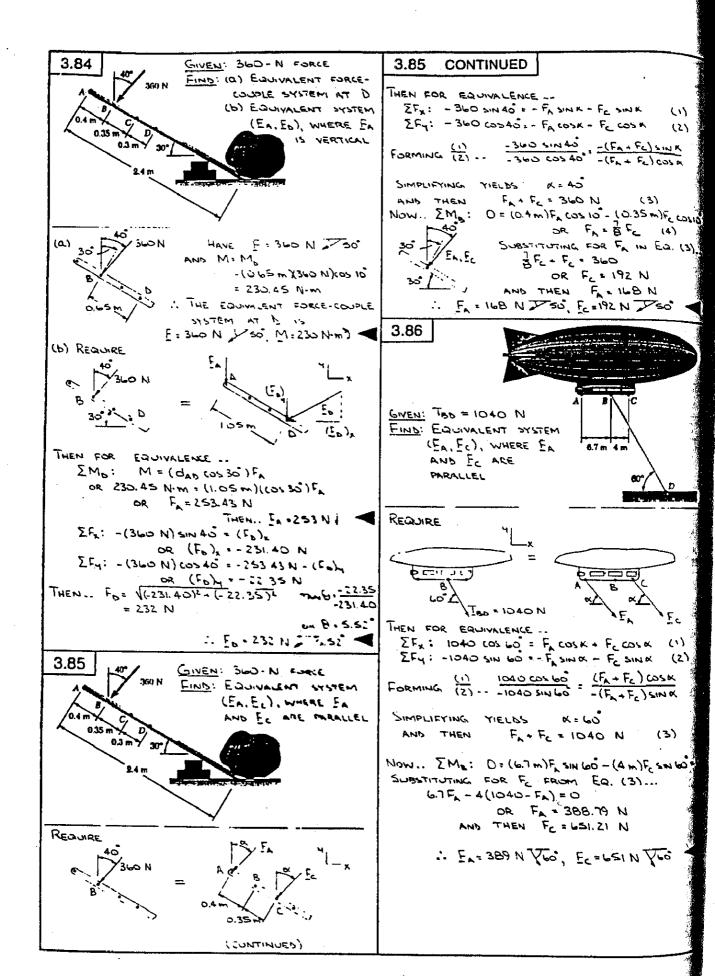
= (178.88 & 16 + 11 + (1136.66 16 + 16))

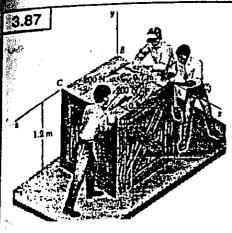
- (211.67 16.16.) b THEN. M: \((178.885)^2 + (1136.66)^2 + (-211.67)^2 = 1169.96 16.16.

OR M = 1170 lb.m.
AND \(\frac{\text{N}}{M} = 0.152 \text{ 898 i + 0.971 54j - 0.180 921 \text{ }}

THEN ... COSBX = 0.152 B9B COSBY = 0.971 SA COSBX = -0.18012 SO THAT BX = B1.2 BY = 15.70 BZ = 100.4







(GIVEN: 1-1-1.2-M CRATE

FIND: (A) EQUIVALENT FORCE-COUPLE SYSTEM

AT A 1F P= 240 N

(b) SINGLE EQUIVALENT FORCE AND

POINT OF APPLICATION ON SIDE AB

(C) P IF THREE FORCES ARE

(a) Since the two 200-N forces form a couple. The three forces are equivalent to a force E and a couple vector 11, where F = (240 N) &

EQUIVALENT TO A SINGLE FORCE AT B

AND M = (0.7-0.2)m = 200 N = 100 N·m

THE EQUIVALENT FORCE-COUPLE SYSTEM AT

A 15- E = (240 N)E, M=(00 N·m);

(b) THE SINGLE EQUIVALENT FORCE F IS EQUAL TO (240 N) & AND IS APPLIED ALLOW AB

SO THAT ITS MOMENT ABOUT A IS

EQUAL TO MI. THUS:

M=dF'

OR 100 N·m = d(240 N)

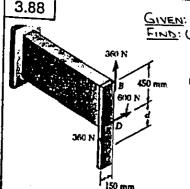
OR d=0.417 m

F'=(240 N) k

■

(C) FOR THIS CASE, d: 1 m. THEN...

M=dP OR 100 N·m=(1 m)P OR P=100 N ◀



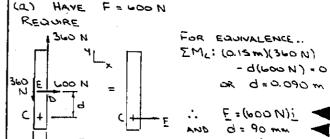
GIVEN: FORCE-COURLE SYSTEM FIND: (a) SINGLE EQUIVALENT FORCE E AT C,

DISTANCE d.

(b) F AND d IF THE DIRECTIONS OF THE TWO 3LO-N
FORCES ARE
REVERCED

(CONTINUED)

3.88 CONTINUED



HOUSEN BELOW POINTS D AND E

(b) THE DULY EFFECT OF REVERSING THE

DIRECTIONS OF THE TWO 360-N FORCES

WILL BE TO CHANGE THE SENSE OF THE

MOMENT OF THE COUPLE, THUS

E=(600 N); AND EMc:-(0.15m)(360 N)-d(600 N)=0 OR d=-0.090 m ... d=90 mm ABOVE POINTS D AND E

3.89

GIVEN: FORCE-COUPLE

SYSTEM

FIND: (a) EQUIVALENT

FORCE-COUPLE

SYSTEM AT B

SO SILL

(b) SINGLE

EQUIVALENT

FORCE, POINT

OF APPLICATION

(a) First Note that the two 20-16 forces FORM A COUPLE. THEN $F = 48 \text{ lb } \triangle 9$

F= 48 16 19 WHERE 0= 180-(60+55")

55° AND M = ΣMB

= (30 m.)(48 lb) cos 55° - (70 m.)(20 lb) cos 20° = - 489.62 lb.m

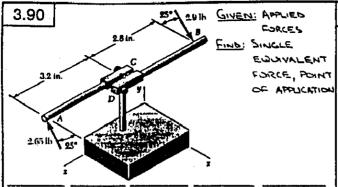
THE EQUIVALENT FORCE-COUPLE SYSTEM AT B

(b) THE SINGLE EQUIVALENT FORCE E' IS EQUAL TO E. FURTHER, SINCE THE SENSE OF M IS CLOCKWINE, E' MUST BE APPLIED BETWEEN A AND B. FOR EQUIVALENCE...

EMB! M = - QF'COS SS'
WHERE & IS THE DISTANCE FROM B TO THE
POINT OF APPLICATION OF E'. THEN...
- 489.42 16.14 = - Q (48 16) COS SS'

or 0 = 17.78 m. ∴ F' = 48 lb ∠65 °

AND 13 APPLIED TO THE LEVER 17.78 IN. TO THE LEFT OF PIN B



FIRST TRANSFER THE 2.65-16 FORCE AT A TO B. THE RESULTING FORCE-COUPLE SYSTEM (F,M) AT B 15 THEN ...

F = (2.9. 2.65)16 = 0.2516

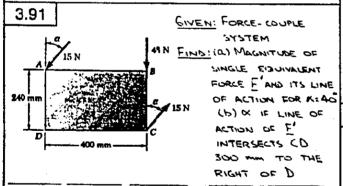
AND M=MB=(6m.X2.6516X0325° OR M=-(14.410316.11) j

THE SINGLE EQUIVALENT FORCE F' IS EQUAL TO F. FURTHER, FUR EQUIVALENCE

 ΣM_B : $M = Q F' \cos 25^\circ$ WHERE Q is the distance from B to the POINT OF APPLICATION OF F'. SINCE M ACTS IN THE -1 DIRECTION, E' WOULD HAVE TO BE APPLIED TO THE RIGHT OF B. THEN...

- 14,4103 lb·m. =-a(0.25 lb) cos 25°

.. $E' = (0.25 \text{ lb})(\cos 25) + \sin 25 \text{ b})$ And is applied on an extension of handle BD at a distance of 63.6 in. to the right of B.



(a) THE GIVEN FORCE. COUPLE SYSTEM (F,M) AT $B : V_{A} = E + B N$ AND $M = EM_{B}$ $= (0.4 m)(15 N)\cos + 0 + (0.24 m)(15 N)\sin 40$

DR M = 6.9103 N.m)
THE SINGLE EQUIVALENT FORCE E' IS EQUIL TO

E. FURTHER, FOR EQUIVALENCE..

E' EMB: MI = dF'

OR 6.9103 N·m = d + 48 N

OR d = 4.14396 m

F' = 48 N

AND THE LINE OF ACTION OF E' INTERSECTS

LINE AB 144 mm TO THE RIGHT OF A.

(CONTINUED)

3.91 CONTINUED

Single

(b) Following the solution to PART Q BU

EQUIVALENT

FORCE, POINT

CMB: (04m)(15N) cosk + (0.24 m)(15N) sink

OF APPLICATION

(b) Following the solution to PART Q BU

LINTH d=0.1 m AND & UNKNOWN, HAVE

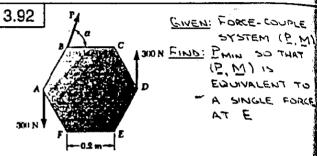
(0.4m)(15N) cosk + (0.24 m)(15N) sink

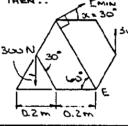
(0.4m)(15N) cosk + (0.24 m)(15N)

OR $5\cos x + 3\sin x = 4$ REARRANGING AND SQUARING... $25\cos^2 x = (4-3\sin x)^2$ Using $\cos^2 x = 1-\sin^2 x$ AND EXPANDING... $25(1-\sin^2 x) = 16-24\sin x + 9\sin^2 x$ OR $34\sin^2 x - 24\sin x - 9 = 0$

THEN SINK = 24 + V(-24)2-4(34)(-9)

DR SINK = 0.97686 SINK = - 0.27098
DR R = 77.7° X = -15.72°





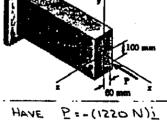
DUN EME: (0.2 sin30+0.2)m·300 +(0.2 m)sin30 · 300 -(0.4 m)Pmin = 0 OR Pmin = 300 N : Pmin = 300 N

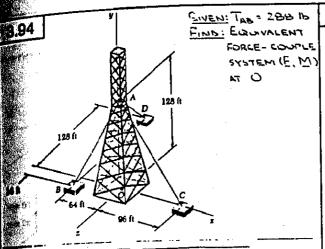
GIVEN: P= 1220 N

FIND: EQUIVALENT FOR

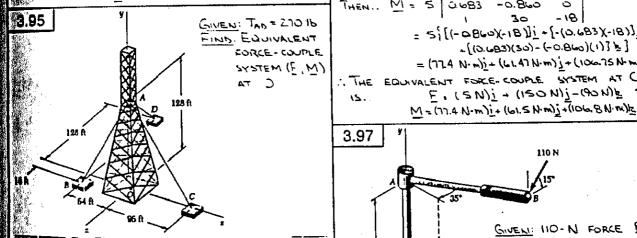
COUPLE SYSTEM

(E,M) AT G





CLAB = 1(-64)2+(-128)2+(16)2 = 144 ft TAB = 28816 (-641-1281-168) THEN = (32 16)(-41-Bj- Bj- B) M = Mo = [1/0 x] AB = 128 j = 32(-41-8j-1) = (4000 16.8E) + (16,384 16.8E) } THE EUNVALENT FORCE-COUPLE SYSTEM AT = = (12B1b) i - (256 16) j + (32 16) k D 15. M = (4.10 kp. ft) = (16.38 kp. ft) =

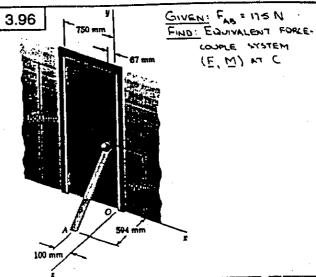


HAVE .. dan = 1(-64)2+(-128)2+(-128)2 = 192 ft

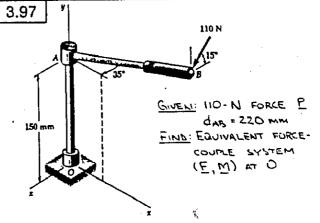
THEN .. IAD = 192 (- 64 - 128) - 128 E) = (90 16)(-<u>i</u>-2j-2<u>E</u>)

Now. = 158] = 80(-j-5j-5F) =-(23,040 16.ft) +(11,520 16.ft) 12

THE EQUIVALENT FURCE-COUPLE SYSTEM AT E = - (90 IP) = (180 IP) = (180 IP) = $M = -(23.0 \text{ Eig. (4)}\underline{i} + (11.52 \text{ Eig. (4)}\underline{k})$



das = \((33)2+(990)2+(-594)2 = 1155 mm FAB = 175 N (331 - 990 j - 594 k) THEN = (5 N)(1+30j-185) NOW .. M = Mc = IBK * FAB [0 = (0 087 m) - (0.800 m)] MHERE THEN .. M = 5 0.083 -0.860 = 5 [(- a B 6 a) X - 1 B] i + [- (0.683 X - 18)] i ~ [(0.683)(30) - (-0.860)(1)] \ \ \] = (774 N·m)j+ (6647 N·m)j+ (100075 N·m) E



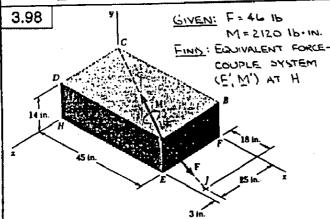
E. (SN) - (ISON) - (90N) E M=(77.4 N-m)i+(61.5 N-m)j+(106.8 N-m)k=

HAVE .. P = (110 N)(-SN 151+ COS 15 E) Now .. M = Mo = [2/0 +] WHERE [PAO = (0.22 m) (0.35 35 1 - (0.15 m) - (0.22 m) SIN 35° k D.15 -0.225m 35° THEN .. M = 110 0.22 cos35 - SIN 15 COS 15

(CONTINUED)

3.97 CONTINUED

OR M = 110{[(0.15)((0515")-(-0.2251035")(-51015")] +[-(022 cos35°)(cos 15°)]; +[(0.22 cos 35)(-sin 15) 12] = (12.345 N·m) = - (19.148 N·m) = - (5.131 H·m) E THE EQUIVALENT FORCE-COUPLE SYSTEM AT E = (110 N) (- SIN 15] + cos 15 E) = - (28.5 N) 1- (106.3 N) E M = (12.35 N·m) = (19.15 N·m) = -(5.13 N·m)E



HAVE -- das= (18)2+(-14)2+(-3)2= 23 in.

THEN. F = \frac{46 \lb \chi}{23} \left(18\frac{1}{2} - 14\frac{1}{2} - 3\frac{1}{2} \right) \frac{1}{2} - (6 \lb) \frac{1}{2}

ALSO. de = V(-45)2+(0)2+(-28)2 = 53 m.

M = 2120 16.14 (-45i - 28 E)

=-(1800 lb.in.) - (1120 lb.in.) E

NOW. M' = M + TAIN x E WHERE TAIN = (45 IN.) 1 + (14 IN.) 1

THEN. M'=(-1800]-1120 E) + 45 14 0

= (-1800)-1120 12)+/[(14)(-6)]1 + [-(45)(-6)]j

~[(45)(-2B)-(14)(3L)]E]

= (-1800 - 84)i + (270)j+ (-1120-1764) k

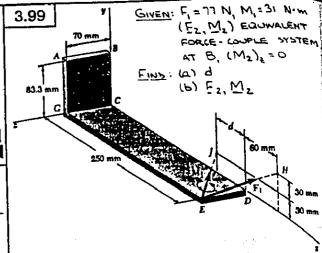
=-(1884 Ib. 11) + (270 Ib-11) }

-(1884 Ib·111) <u>k</u>

=-(157 16.54) =+(22.5 16.54) }

- (240 16.4t)E

.. THE EQUIVALENT FURCE- COUNTE SYSTEM AT E, = (30 19) = (58 19) = (0 19) F M'=-(157 16. ft) i+(22.5 Tb.ft) j-(240 16.6t) t



HAVE .. den = V(60)2+(00)2+(-70)2 = 110 mm

 $E_{1} = \frac{110}{110} (601 + 601 - 10E)$ = (42 N)1 + (42 N)2 - (49 N)E

ALSO. des = V(-d)2+(30)2+(-70)2 mm

W' = GE7 [-(9)] + (30 mm)]-(30 mm)]

(a) HAVE. $M_2 = M_1 + C_{H/B} \times F_1$ (1) WHERE $C_{H/B} = (0.31 \text{ m})_1 - (0.0233 \text{ m})_2$

0.31 - 0.0233 THEN . . IND . F. = - 49

= [(-00233X-49)] i+[-(031)(-49)] +[(0.31)(42)-(-0.0233)(42)] = = (1.1417 N·m) + (15.19 N·m) j

+(13.99B6 N·m) 12

EQ. (1) CAN THEN BE EXPRESSED AS (M₂)_x i + (M₂)_y i = 31 N·m [-(d)i + (30 mm) i (M₂)_x i + (M₂)_y i = 31 N·m [-(d)i + (30 mm) i -(10 mm)jī]

> + (1.1417 Now) + (15.19 Now)] + (13.508C N.m/F)

EQUATING THE E COEFFICIENTS..

THEN. dej = (13.9786 70 mm)2=[(-d)2+(30)2+(-70)] d - 135.0 mm OR 0 = 135.018 mm

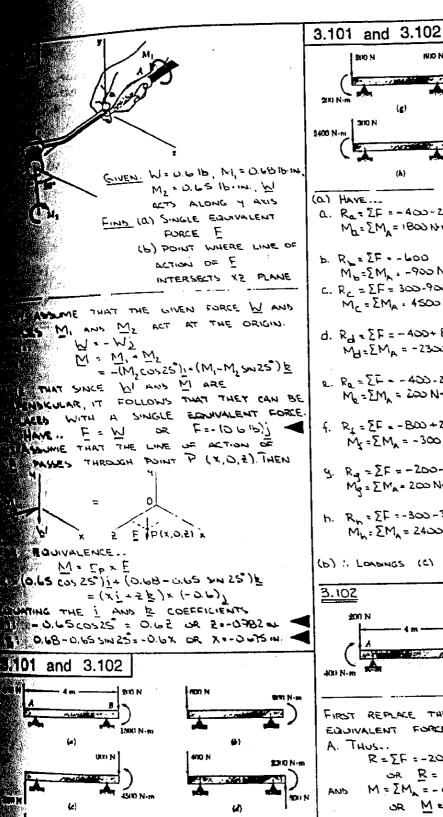
(b) FIRST NOTE dE1 = V(-135.018)2+(30)2+(-70)1 155,016 mm

Using Eq. (2), M_2 is THEN... $M_2 = \left(-\frac{31 \times 135.018}{155.016} + 1.1417\right)_1^2$

+ (31x 30 + 15A)j

= -(25.859 N·W) + (21.189 N·m);

Ez = (42 N) + (42 N) = (49 N) = M. =- (25.9 N·m) = (21.2 N·m)



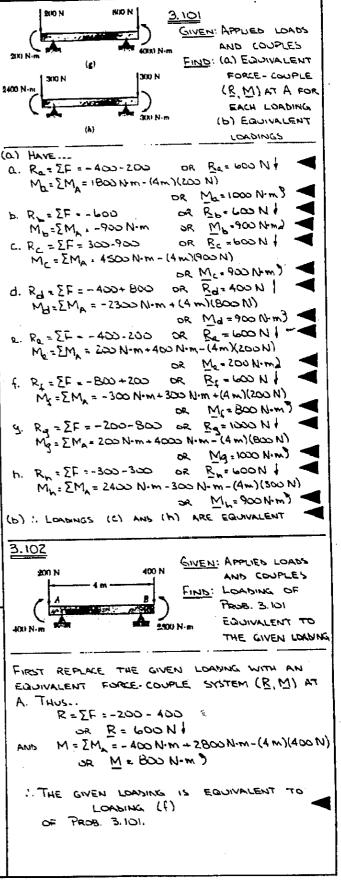
800 N

(f)

(CONTINUED)

300 N-n

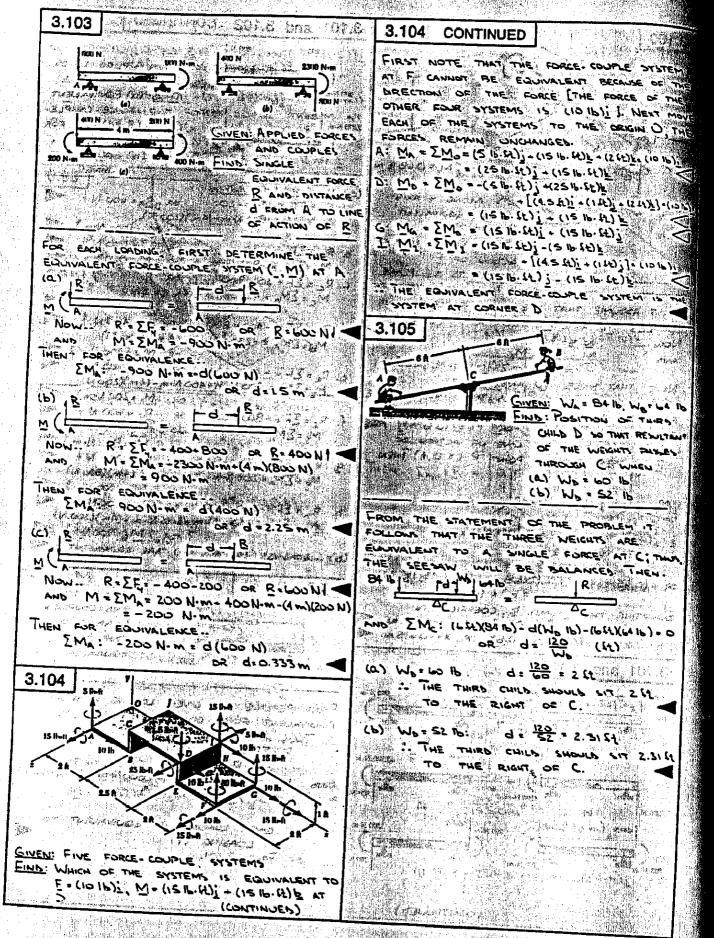
400 N-m

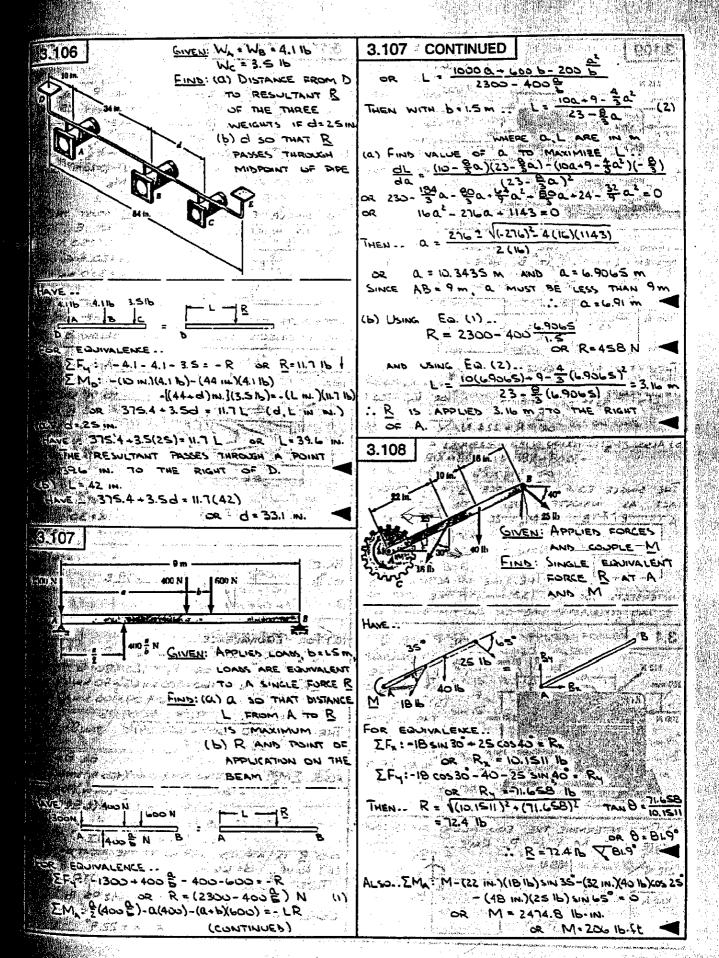


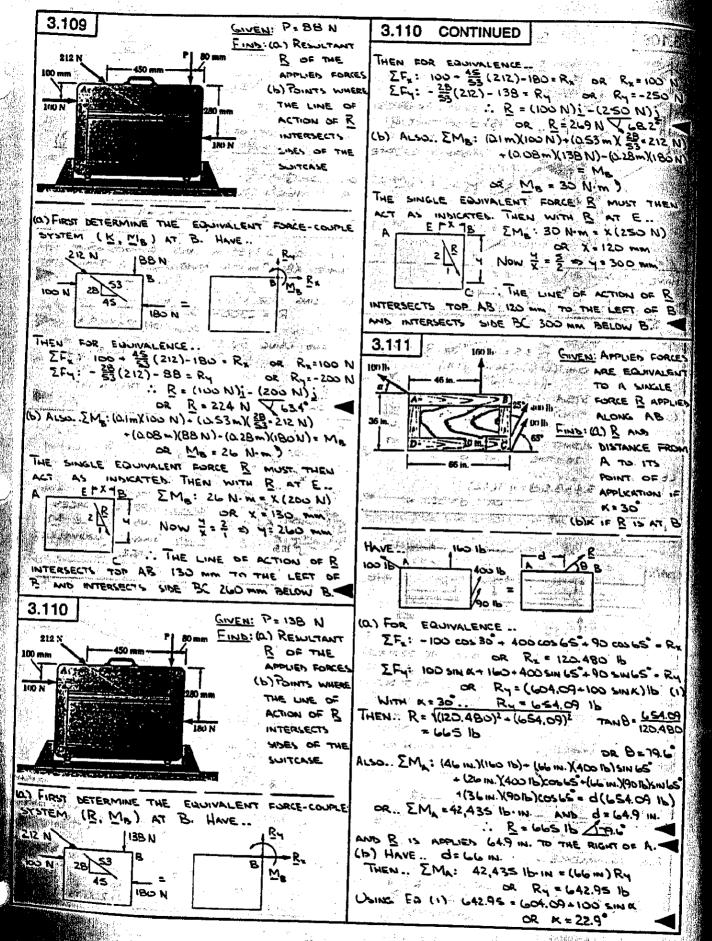
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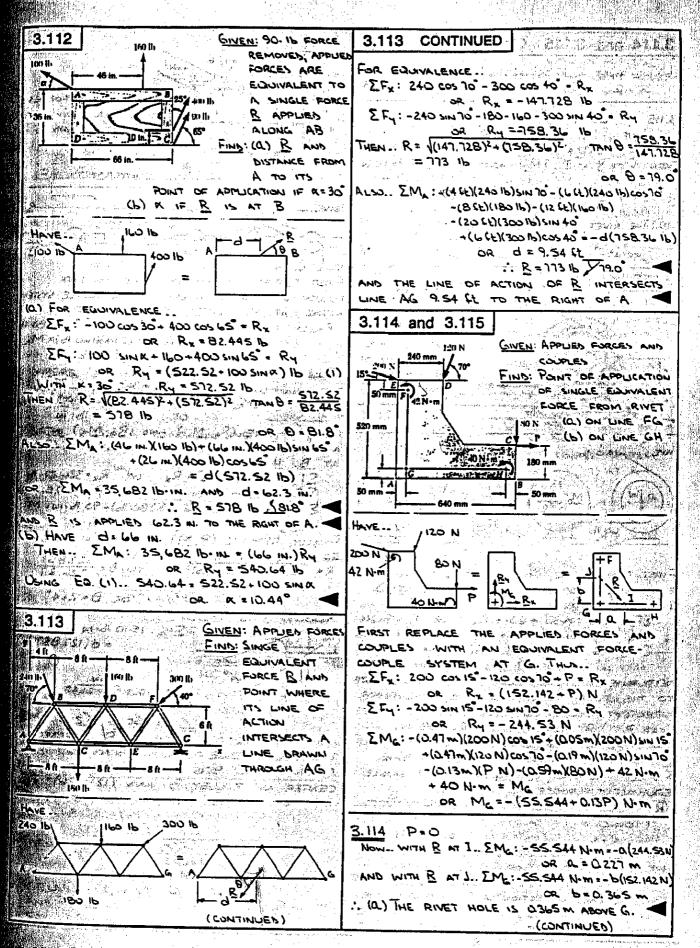
300 N·m

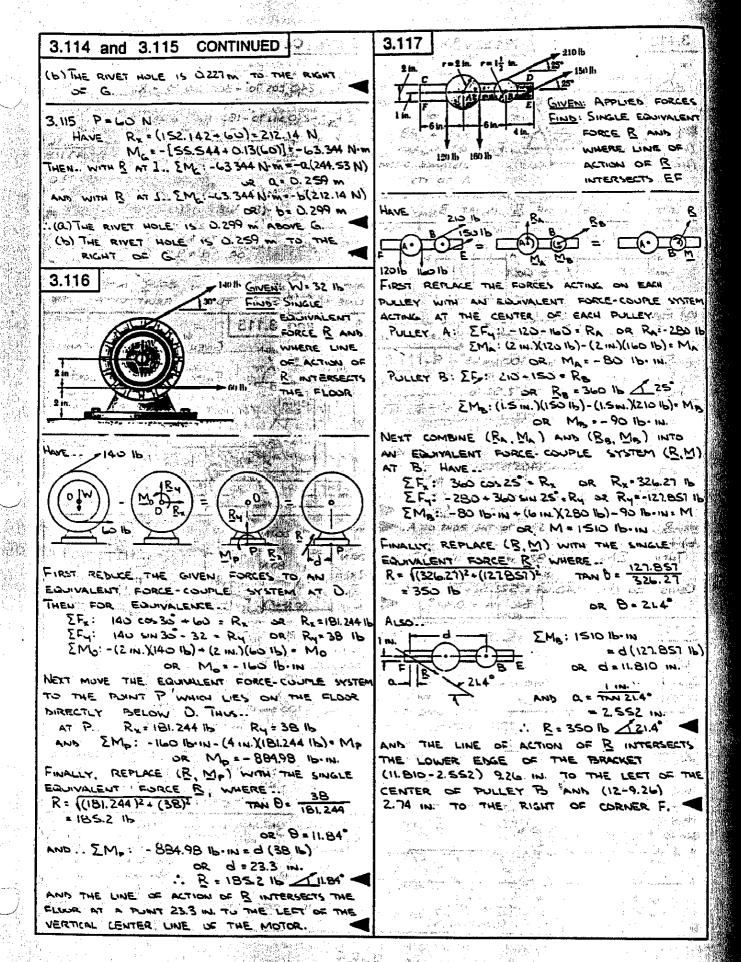
200 N

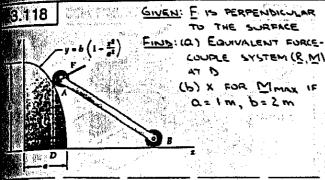












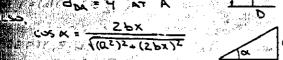
THE SLOPE AT ANY POINT ON THE SURFACE OF MEMBER C 15.

DINCE E IS PERPENDICULAR TO THE SURFACE, IT FOLLOWS THAT

TAN $K = \frac{QL}{2L} \frac{1}{V}$

WHERE K IS THE ANGLE THAT F FORMS IDITH THE HORIZOUTAL THEN FOR ELOUVALENCE

SE F R SMb Idda F cos a = M JACE A 15 A POINT ON THE D SAFACE HAVE A TA PENDEN



 $M = [b(1 - \frac{x^2}{\Omega^2})] \cdot F = \frac{2bx}{\sqrt{\Omega^4 + 4b^2x^2}}$

THE EQUIVALENT FORCE-COURLE SYSTEM R=FJTNI(能)

 $M = \frac{2Eb^{2}(X - \frac{X^{2}}{4E^{2}})}{\sqrt{Q^{2} + 4b^{2}X^{2}}}$

STATING Q=1 M, b= 2 M M THE EXPRESSION FOR MYIELDS ..

M = BE(X-X3) 1-8E (1-3x5)1+1Px5-(x-x3)(\$(35x)(1+1Px5).5) というとはない。(1+10メ2)

BE (1-3x2)(1+16x2)-16x(x-x3) = 0 32 x4 + 3x2 - 1 = 0

Y2 = -3 ± 1(3)2-4(32)(-1) 2(32) AKING THE POSITIVE ROUT SINCE X2 >0

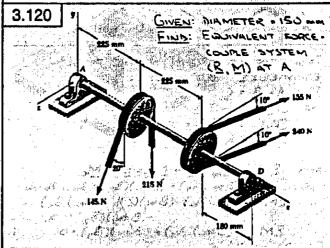
VELDS X2 = 0.136011 M2 AND THEN x = 0.369 m

FOR MMX

GWEN! DIAMETER - 60 MM 3.119 APPLIED FORKES 20 mm $= \left\{ \begin{array}{ll} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \left(\frac{1}{2} \right) \\ \frac{1}{2} & \frac{1}{2} \left(\frac{1}{2} \right) & \frac{1}{2} \left(\frac{1}{2} \right) \end{array} \right\}$ FIND: EQUIVALENT FORCE-17 N 12 N COUPLE SYSTEM (R.M) AT C FOR EQUIVALENCE ... - 117 - 15? Fig - 102 - 211 = (21 N);-(29 N); EM: M = CAK = EX + Laye = Fa

+ Tole + Fo OR M = (0.11m) - (0.03m) &] + [- (17 N)] + [(0.05m)j+(0.11m)j-(0.03m)]z]-[-(12N)j +[(QU3m)i+(QO3m)j-(Q.O3m)k]=[-(21N)]i =-(0.51 N. m) + [-(0.24 N.m)]x-(0.36 N.m) i] 1 +[(0.63 N-m)k+(0.63 N-m)]]

. THE ECHNICLENT FORCE-COUPLE SYSTEM AT R = -(21N); - (29N); - (16N)& W =-(0.87 N-m) +(0.63 N-m) = (0.39 N-m)



FIRST REPLACE THE BELT FORCES ON EACH PULLEY WITH AN EQUIVALENT FORCE-COURLE SYSTEM AT THE CENTER OF THE PULLEY THIS ELIMINATES THE NEED TO DETERMINE WHERE THE BELTS CONTACT THE PULLEY'S POLLEY B: EE: BB = -2151+145(-c0320j-31420) = -(351.26 N); -(49.593 N)} EM : M = [(0.075 m X 145 N) - (0.075 m)(215 N)] PULLEY C: Ef: Rc = (155+240X-51410 1-60510 E)

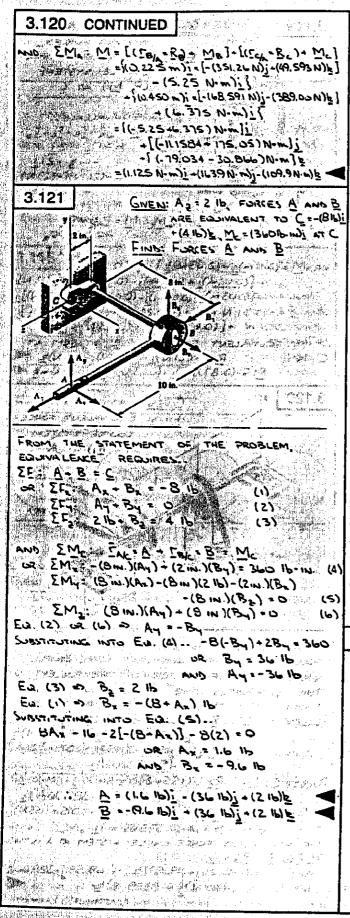
J(N 20. 1885) = (N 182.84) = == ΣMc: Mc = [(0.075m / 240N)-(0.075m / 155N)]

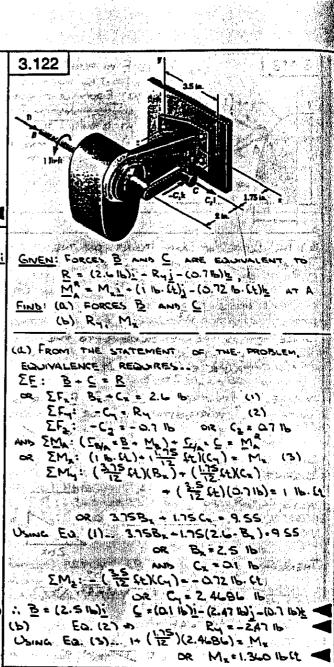
= (6.375 N·m)i

THE EQUIVALENT FORCE-COURLE SYSTEM AT A IN THEU EF: R = Ra - Rc

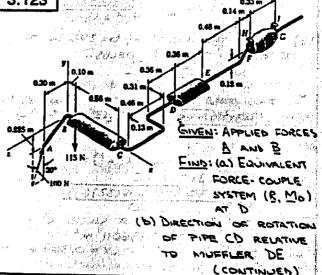
= (-35126)+49.593 k)+(-68.591)-389.00k = - (420 N); - (339 N)E (CONTINUED)

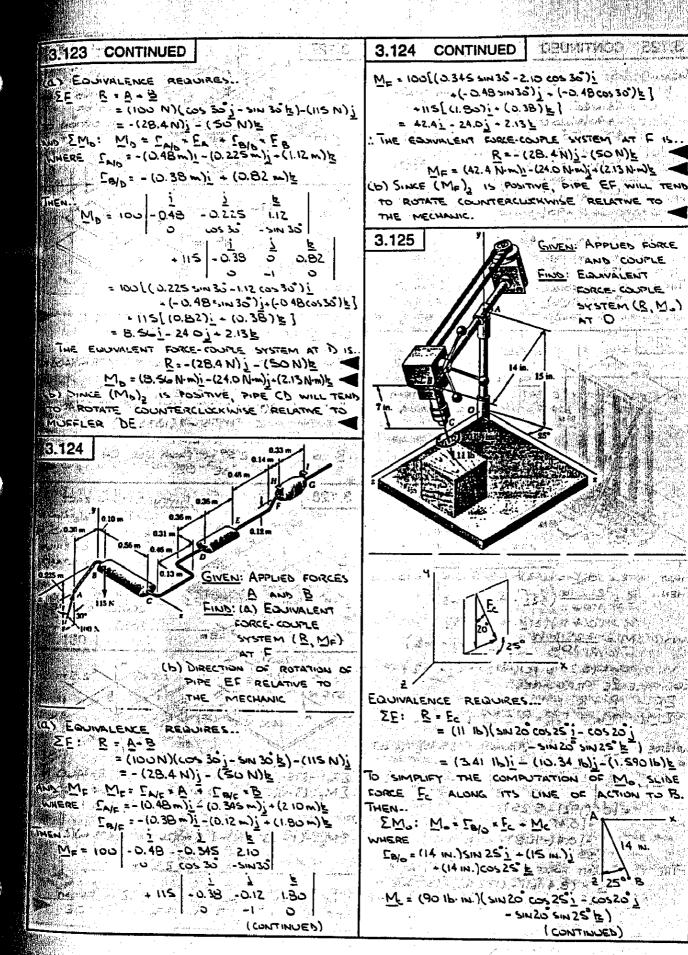
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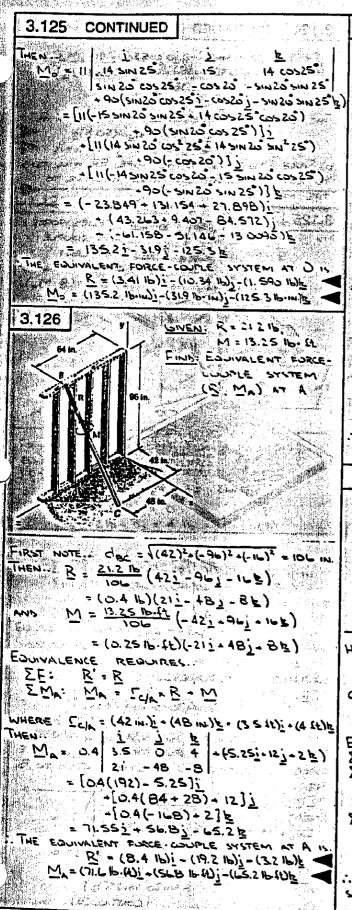


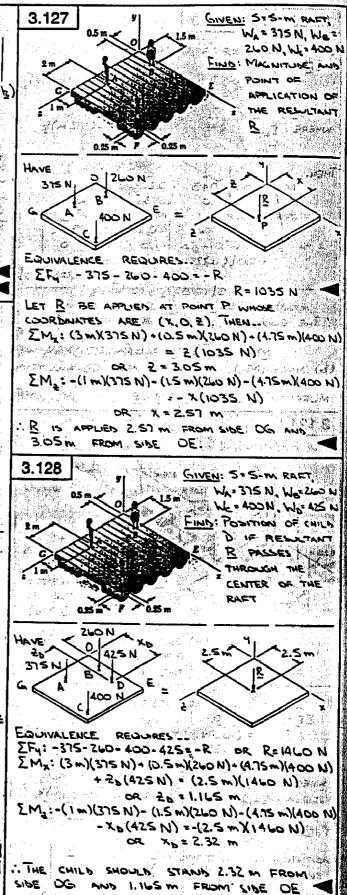


3.123

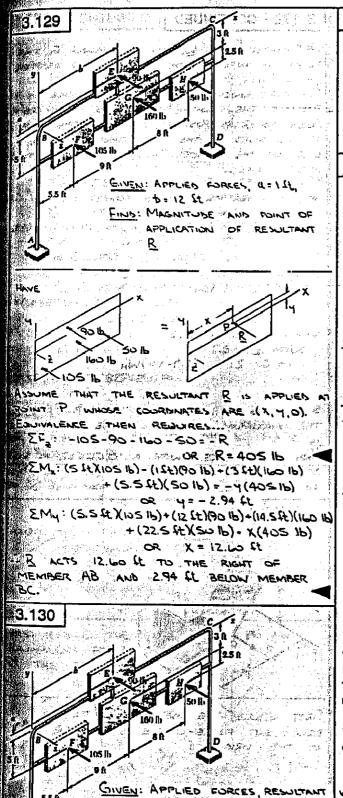








30000 Prog. 安起數學



R OF THE FOUR FORCES

(CONTINUED)

FIND DISTANCES Q AND b

SINCE BOACTS AT G. EQUIVALENCE THEN

REQUIRES THAT EM OF THE APPLIES

3.130 CONTINUED

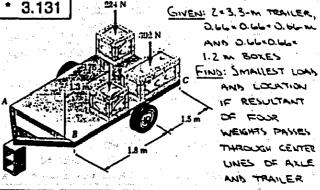
萨斯内特斯 医乳球病 化排泄管管理 医二甲基

SYSTEM OF FORCES ILLSO BE BERO. THEN...
AT G: $\sum M_x := (0.3) \text{ ft.} (90 \text{ lb.}) + (2 \text{ ft.}) (105 \text{ lb.})$ + (2.5 ft.) (50 lb.) = 0

OR Q=0.722 \$2

 $EM_{ij}:=(9 \text{ i.e.})(105 \text{ i.e.}) - (14.5-16) \text{ i.e.}$

OR 6=20.681 -



FIRST REPLACE THE THREE KNOWN LOADS WITH A SINGLE EDUIVALENT FORCE RK APPLIED AT POINT K WHISE COORDINATES ARE (12,021)



EQUIVALENCE REQUIRES ...

THE RESERVE OF THE WAR WITH THE WAY

EF4: - 224-392-176=-RK OR RK=792 N

EMx: (0.33 m)(224 N)+ (0 6 m)(392 N)

+ (2 m)(17L N) = ZK (792 N)

EM2: - (0.33 m)(224 N) - (1.67 m) (392 N)

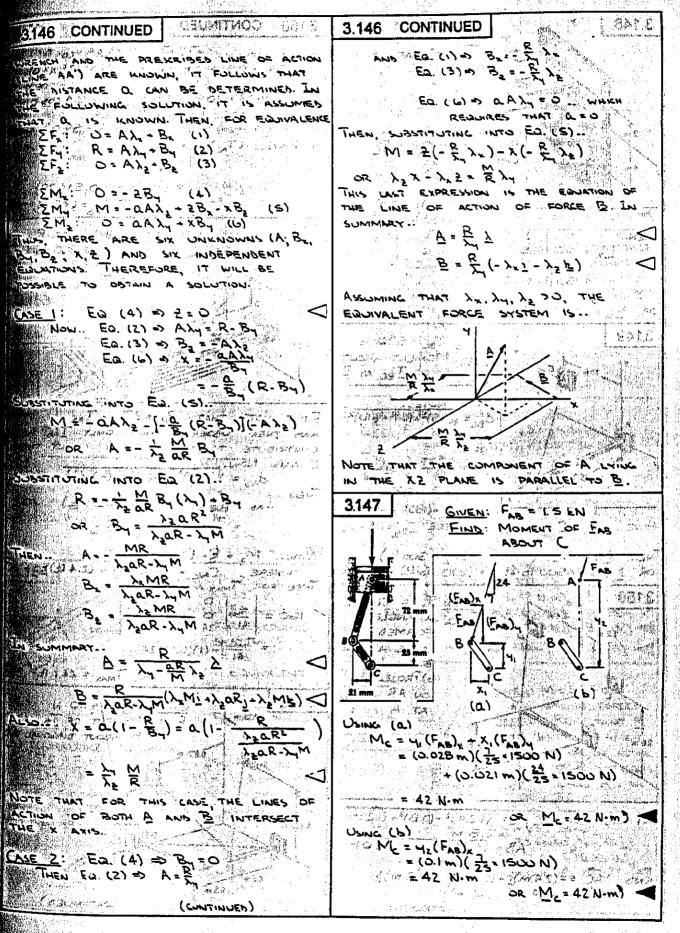
- (1.67 m)(176 N) = - xx(792 N)

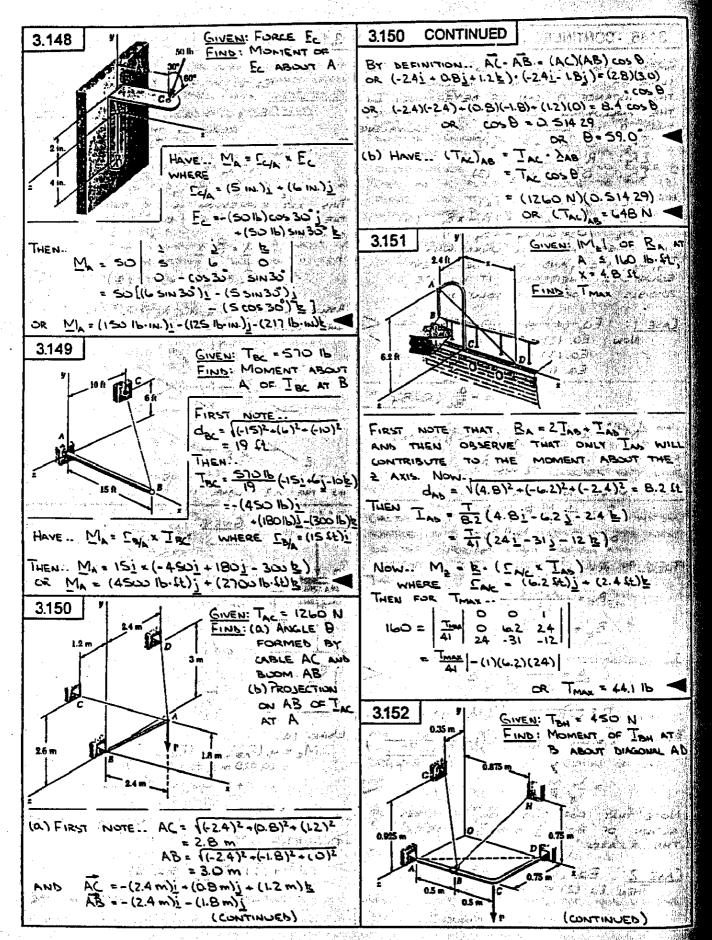
FROM THE STATEMENT OF THE PROBLEM IT IS KNOWN THAT THE REGILTANT OF BY AND THE LIGHTEST LOAD WE PHOSES THROUGH G, THE POINT OF INTERSECTION OF THE TWO CENTER

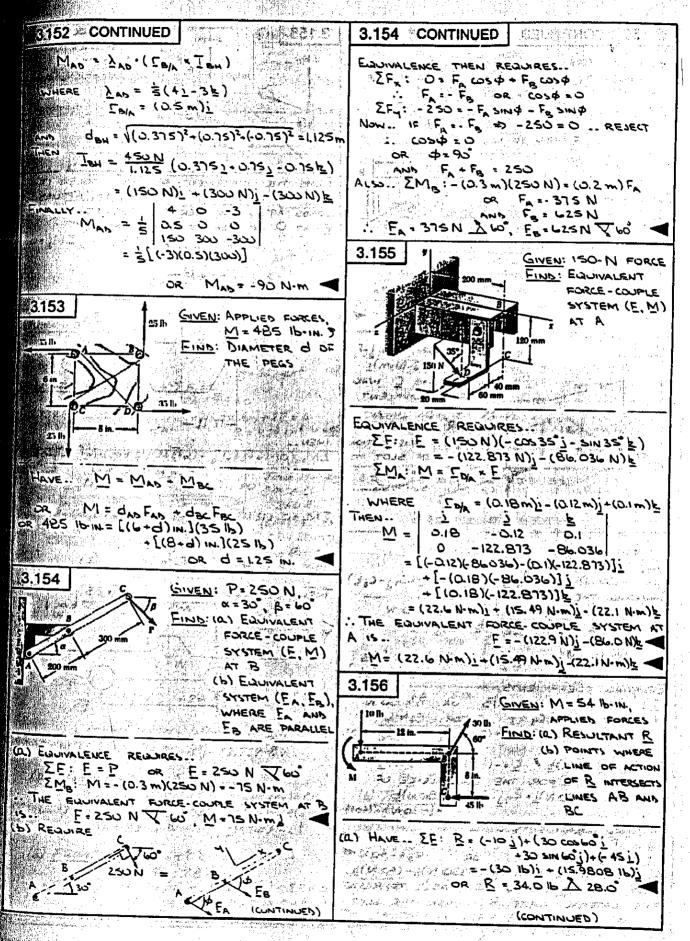
LINES THUS, $\Sigma M_{G} = 0$ FURTHER, SINCE W_{L} 15 TO BE AS SMALL AS POSSIBLE, THE FOURTH BOX SHOULD BE PLACED AS FAR FROM G AS POSSIBLE. THESE TWO REQUIREMENTS IMPLY.

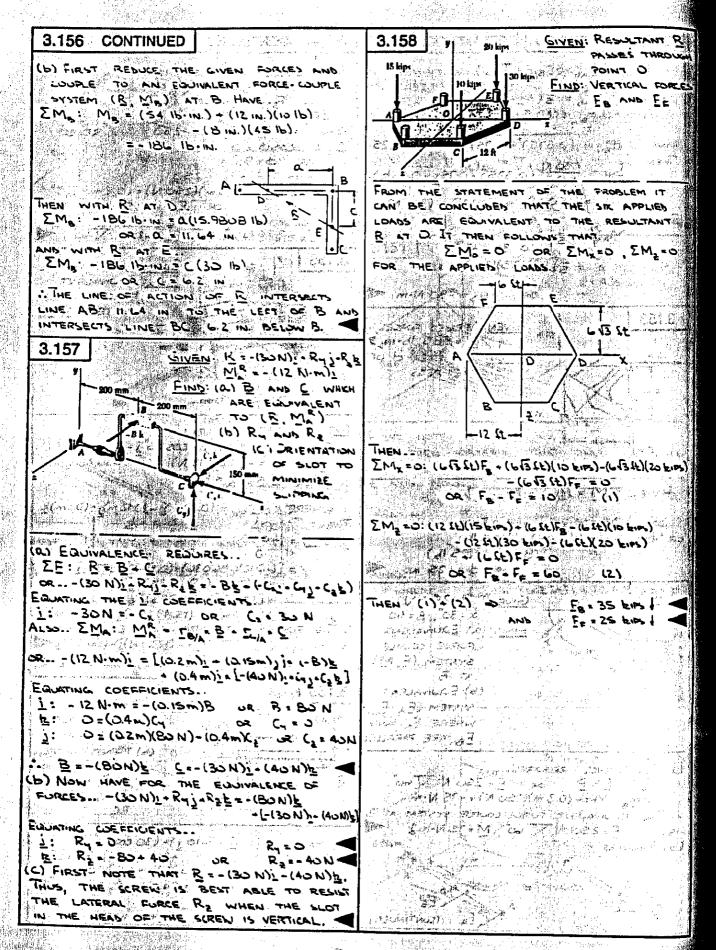
O 33 m & X & 1.0 m AND 1.5 m & 2 & 2.97 m where the Lower bound on X and the upper bound on X and the upper bound on A ARE IMPOSED SO THAT THE BOX DOES NOT OVERHAND THE TRAILER. SINKE THE BOX IS TO BE AS FAR FROM G AS POSSIBLE CONSIDER FIRST IF THESE BOUNDS ARE PHYSKALLY POSSIBLE.

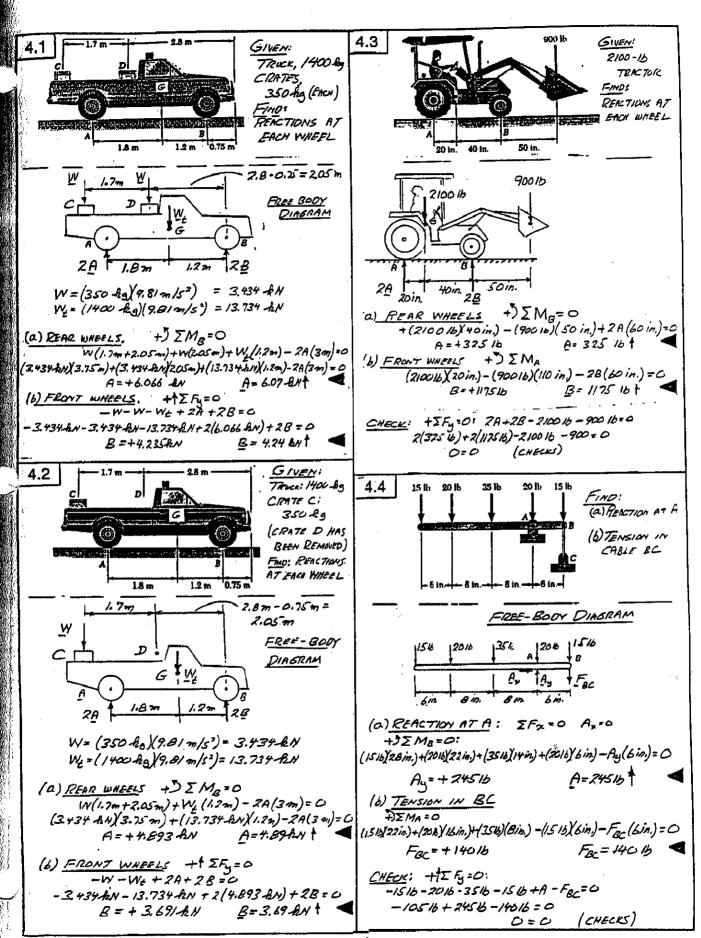
(CUNTINUES)

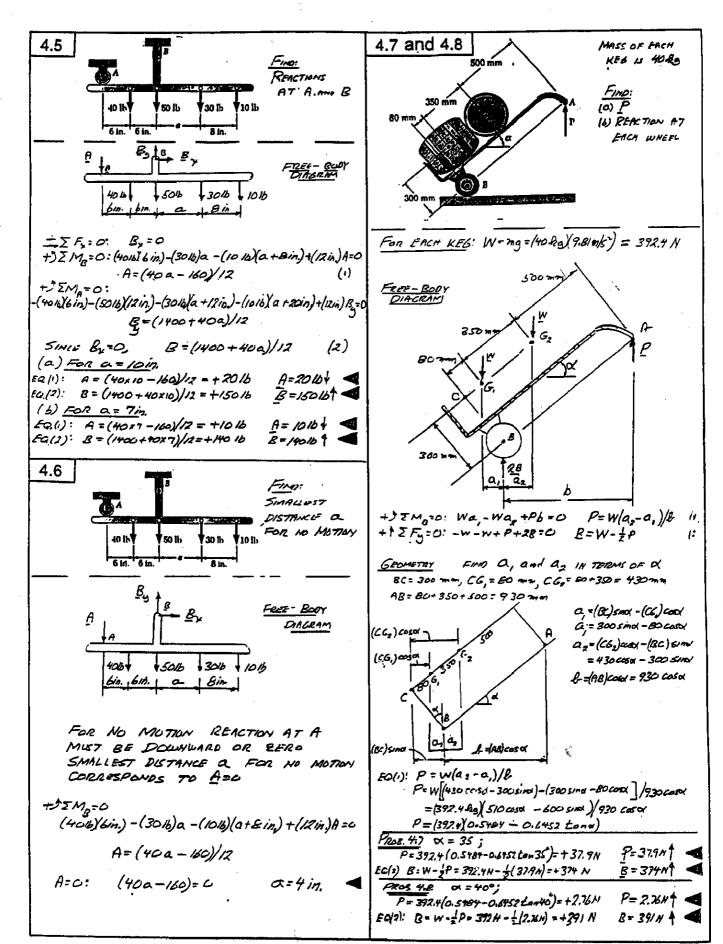


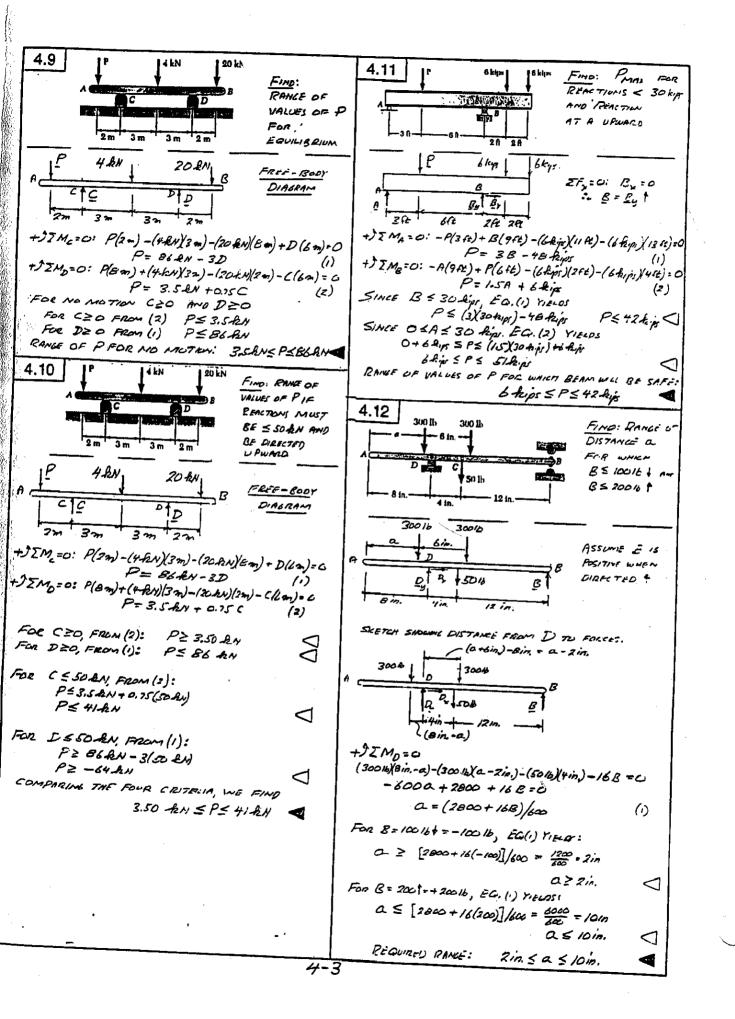


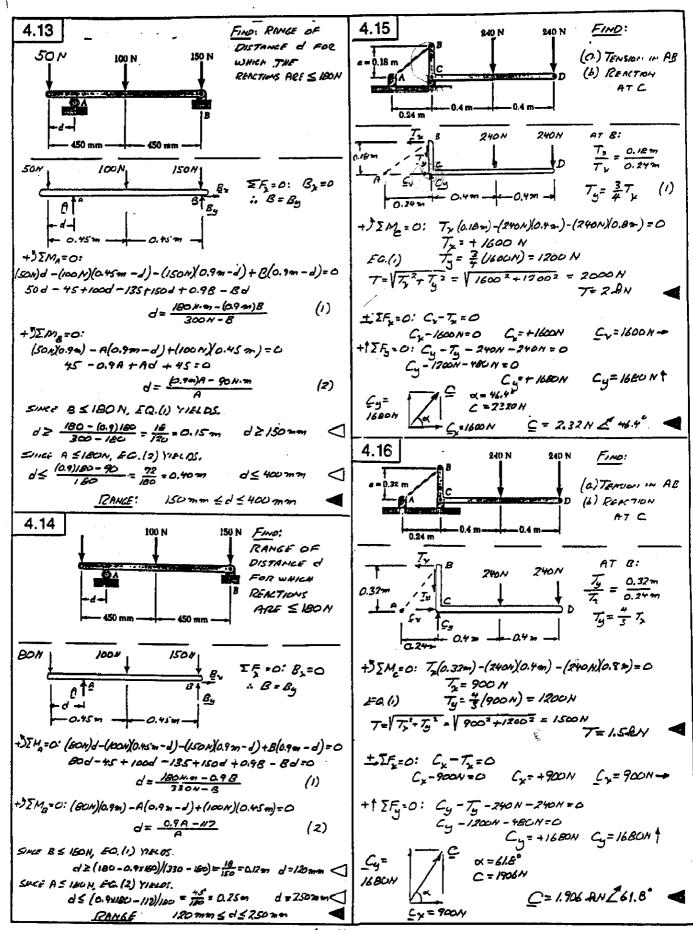


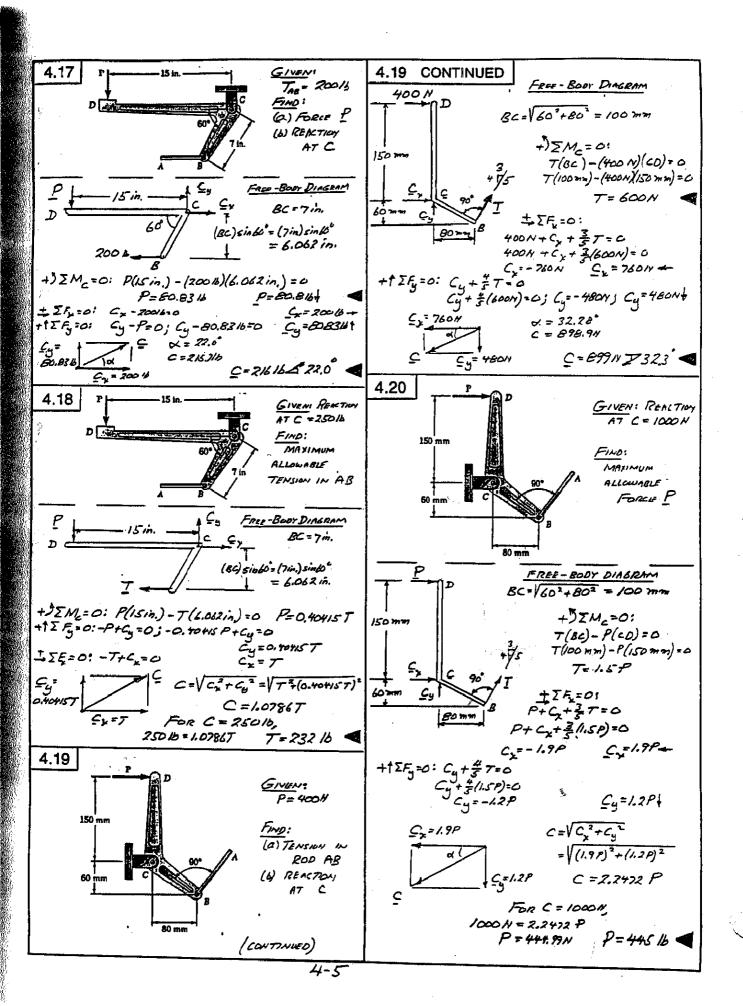


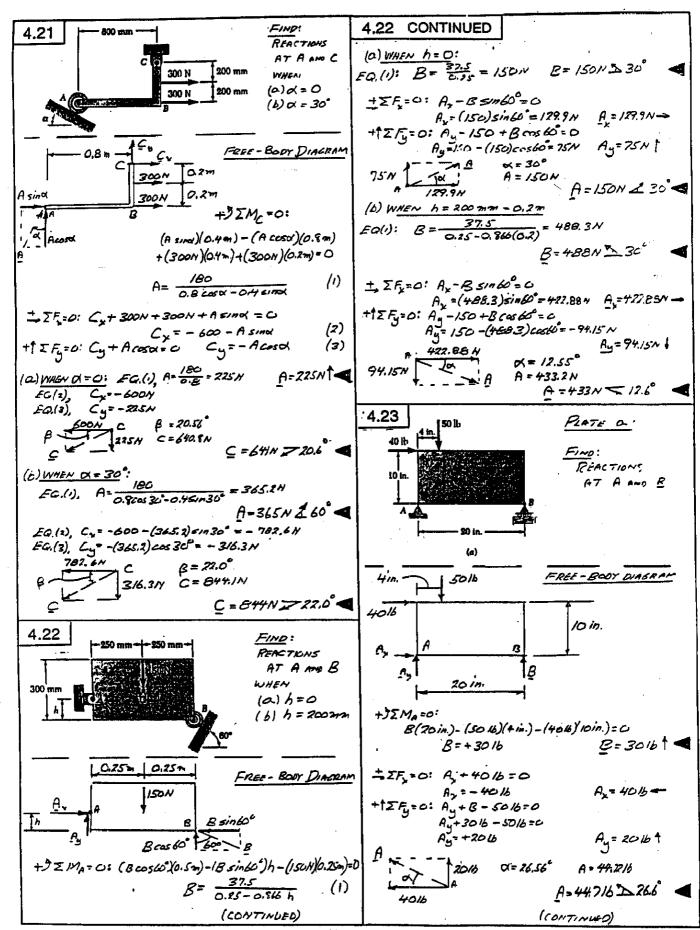


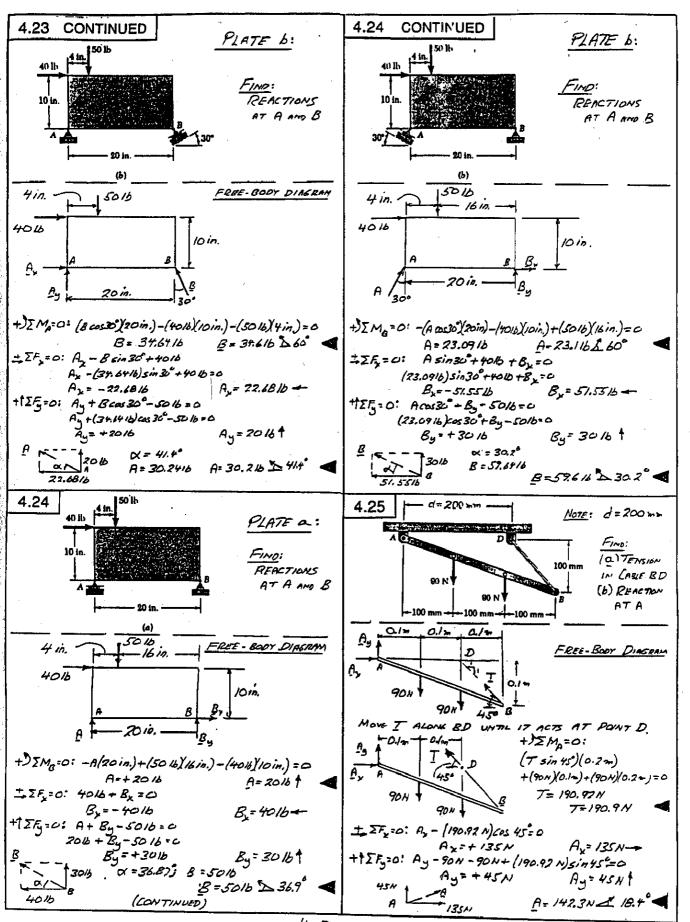


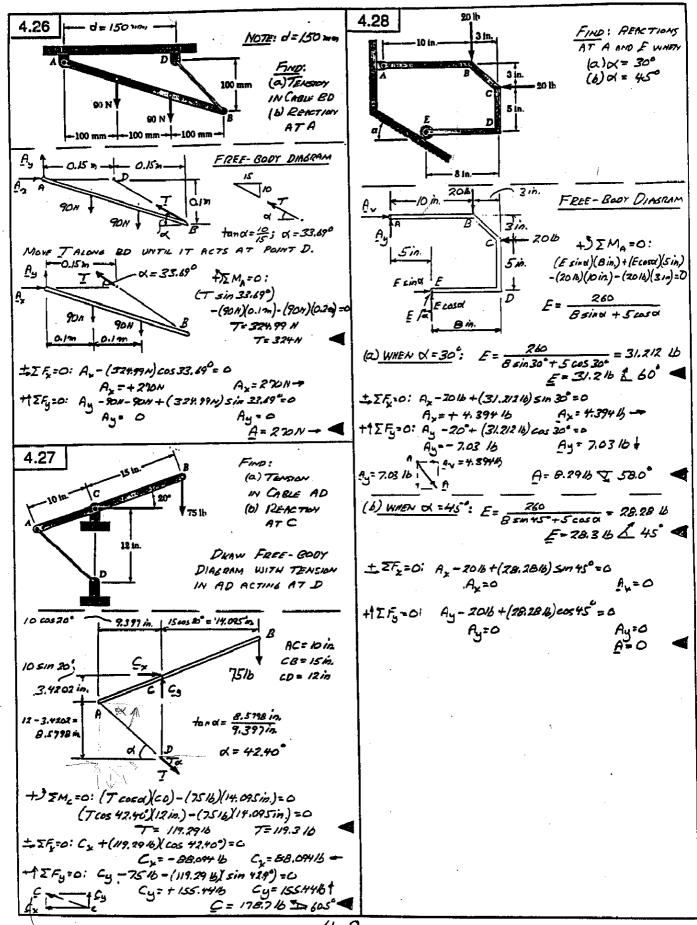




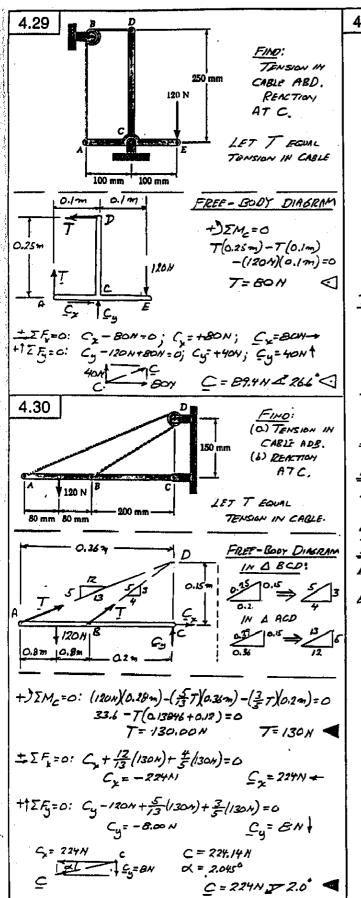


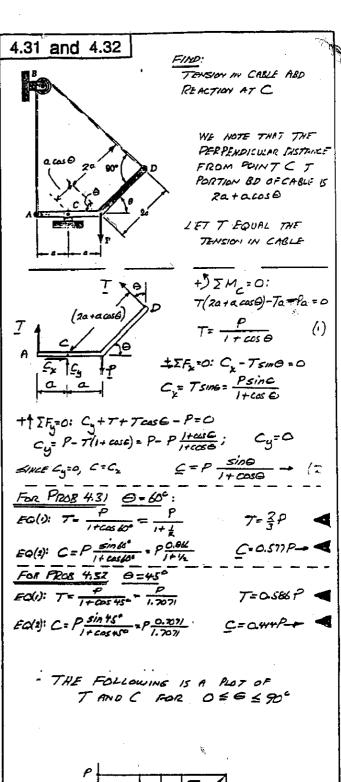




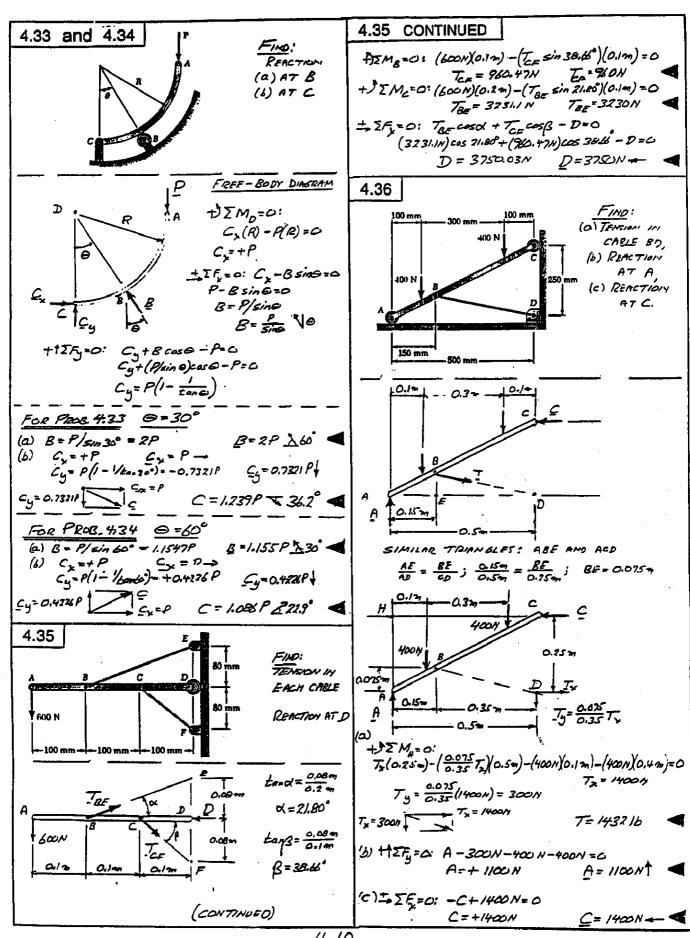


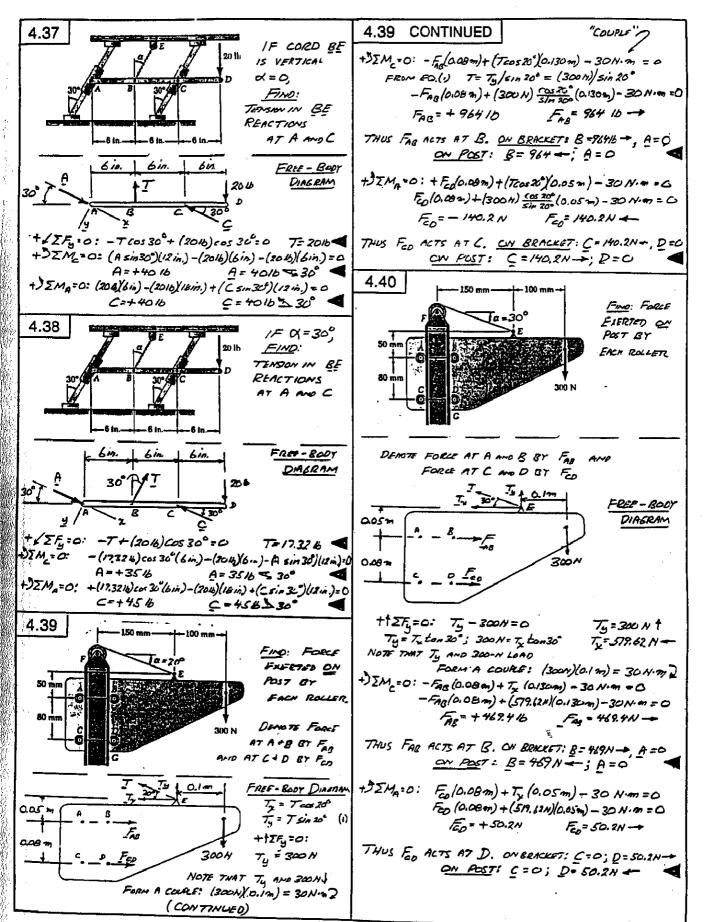
4-8

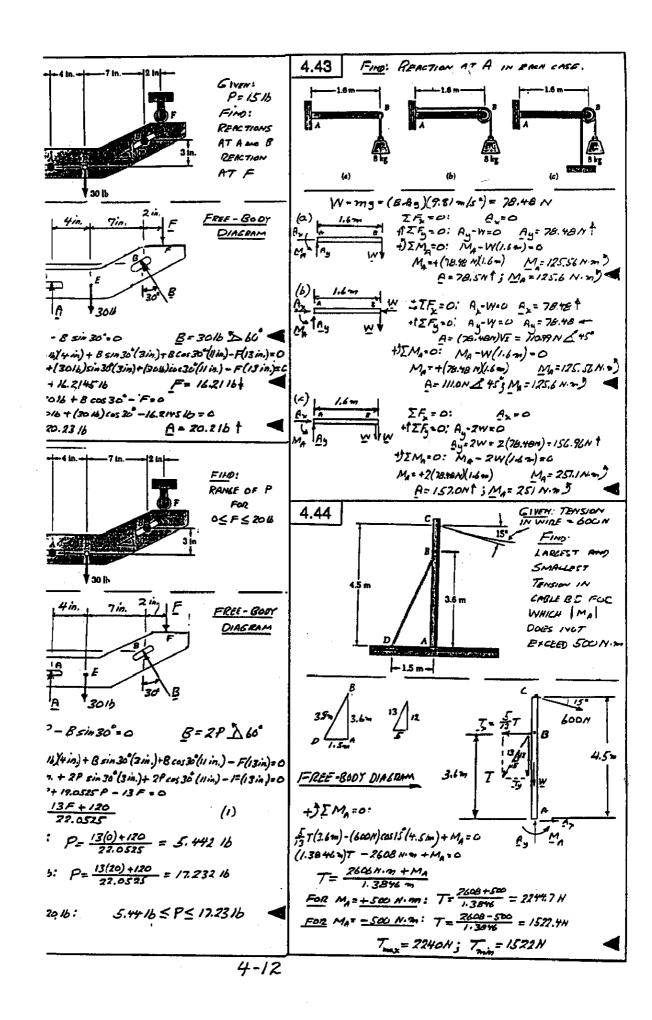


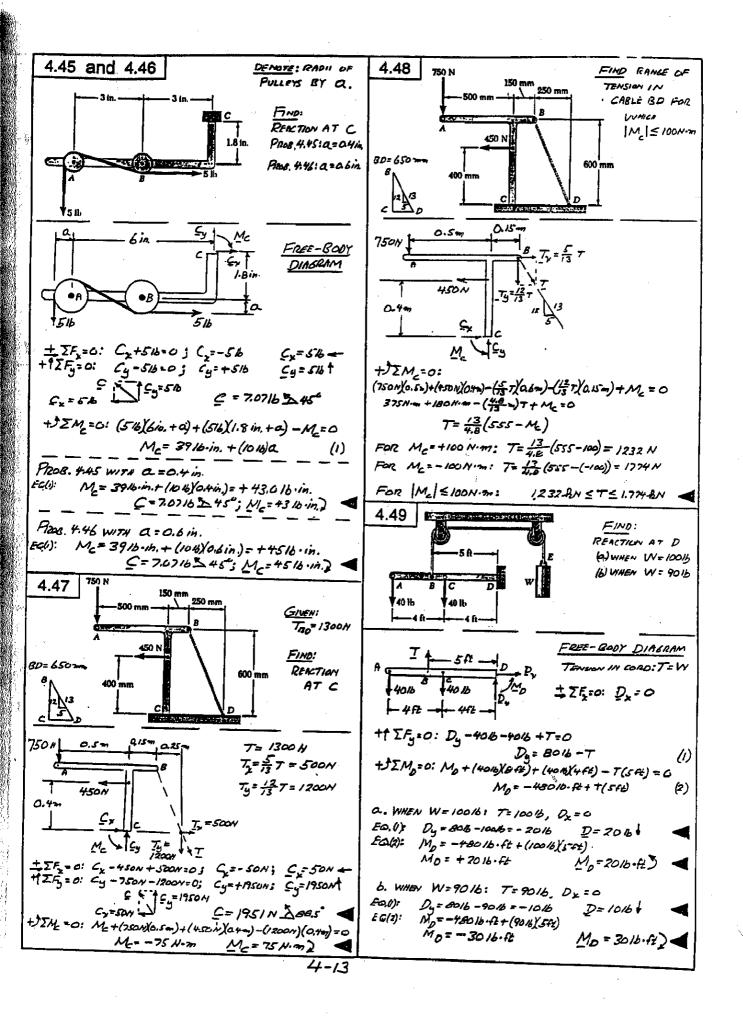


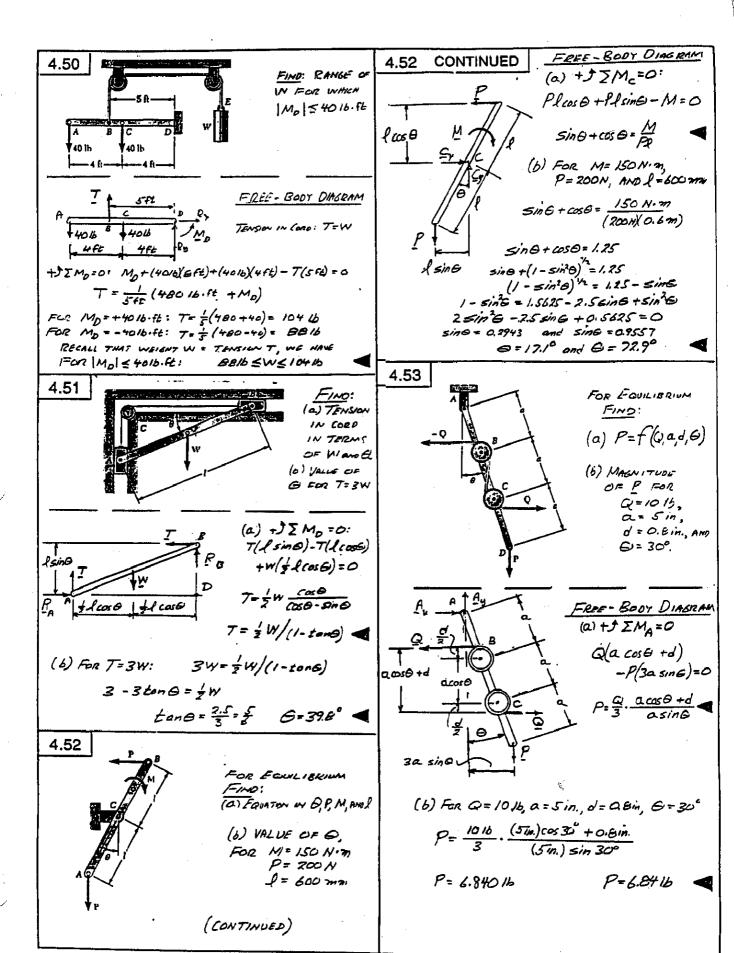
0.6P 0.4P 0.2P 0.2P

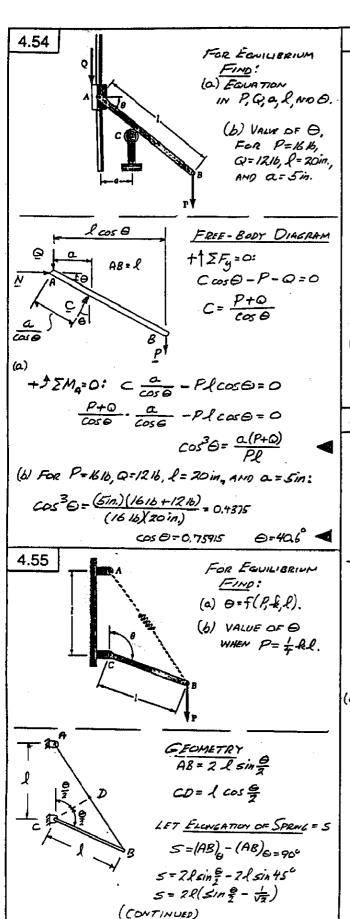


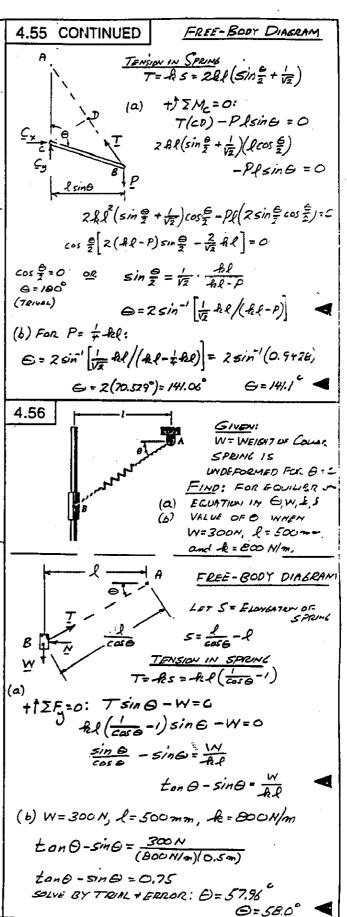


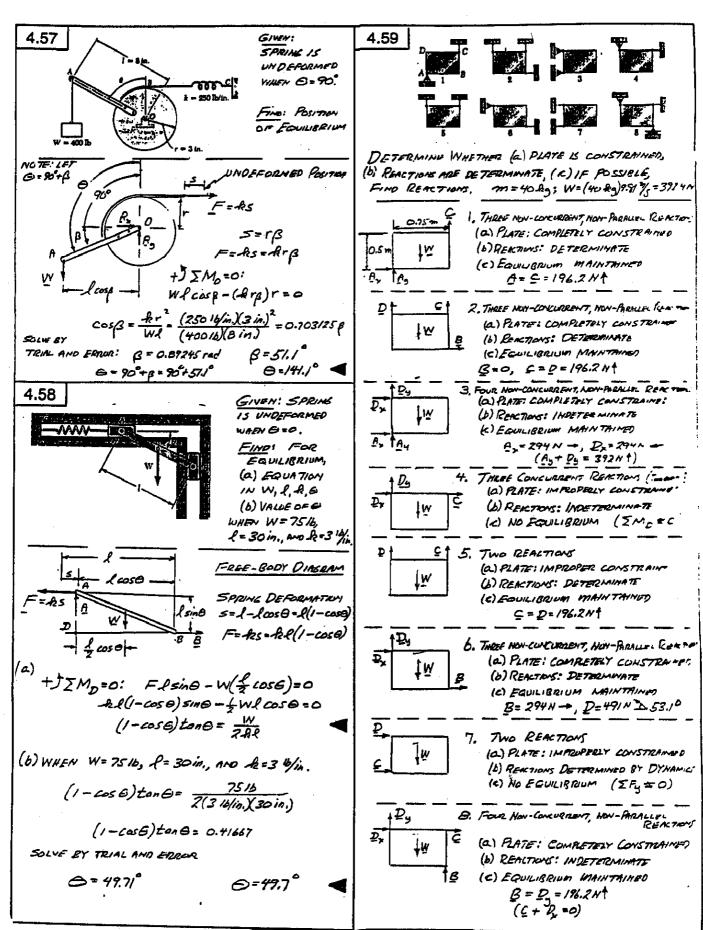


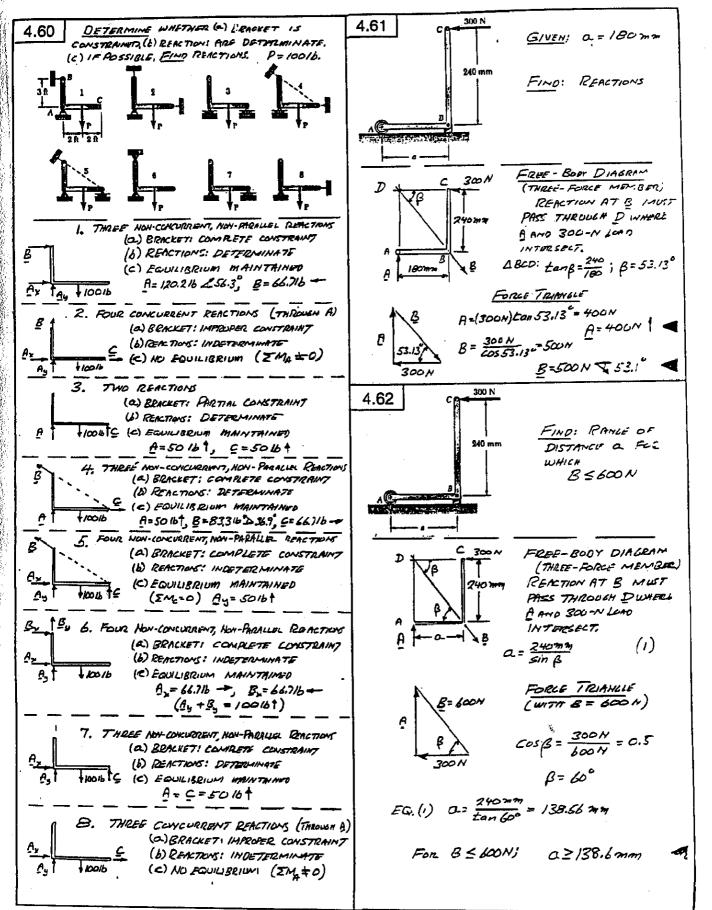


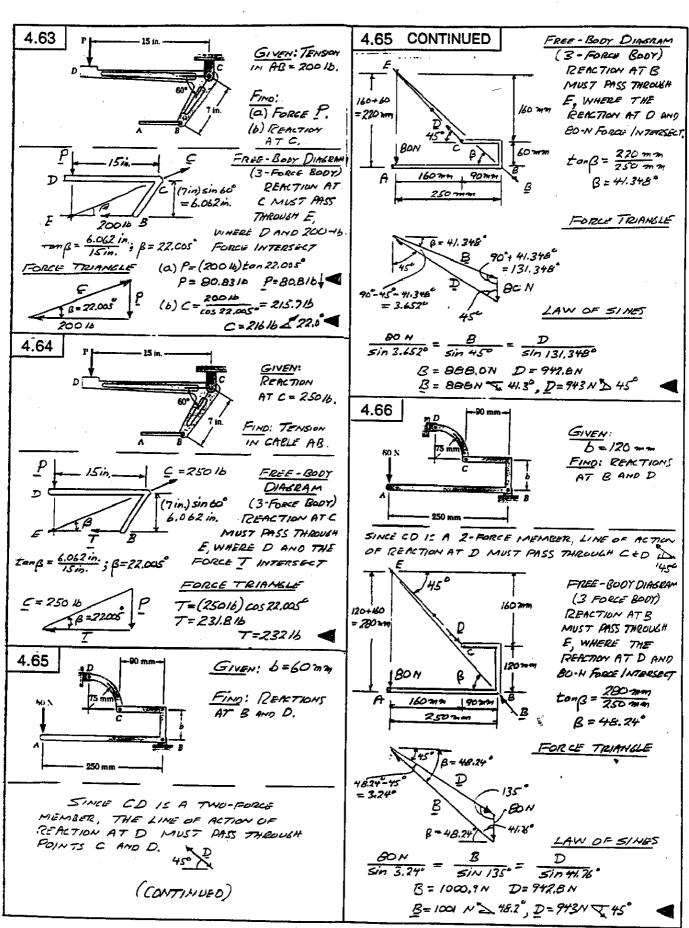


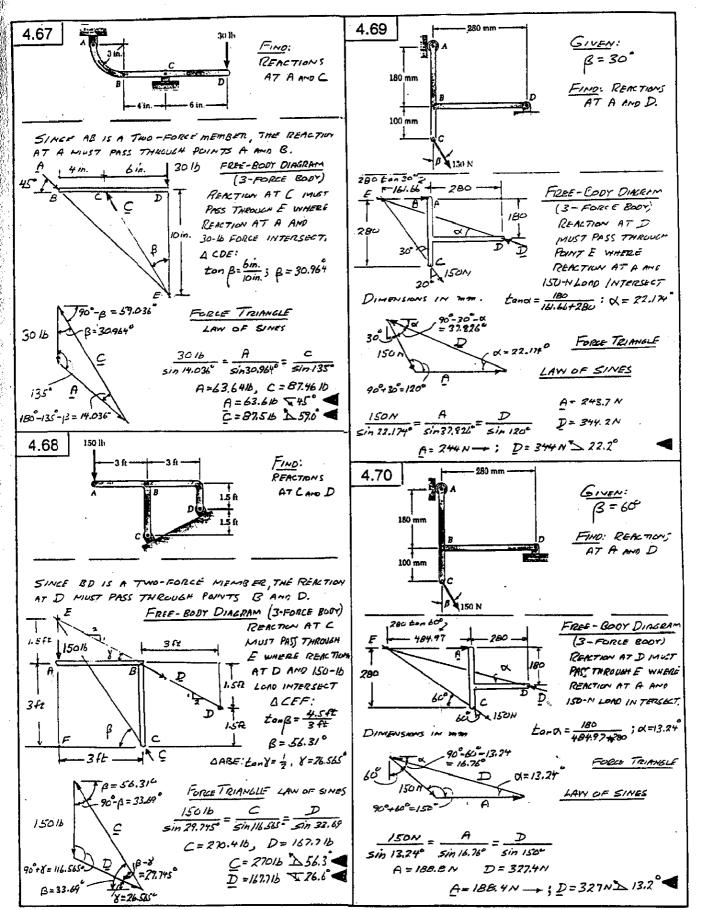


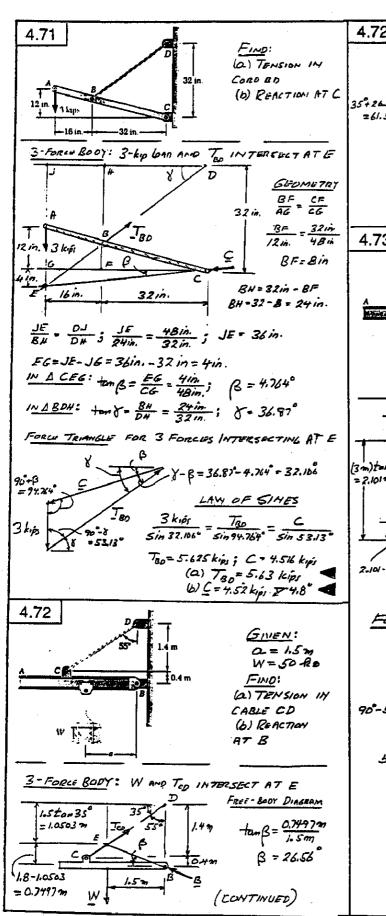


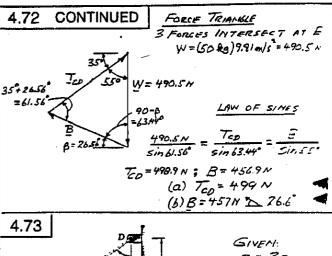


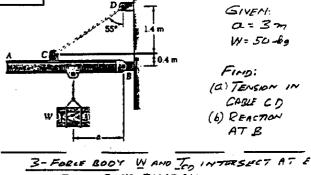


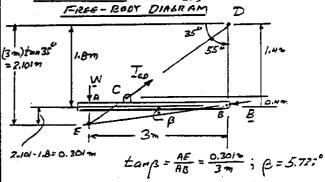




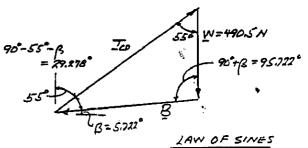






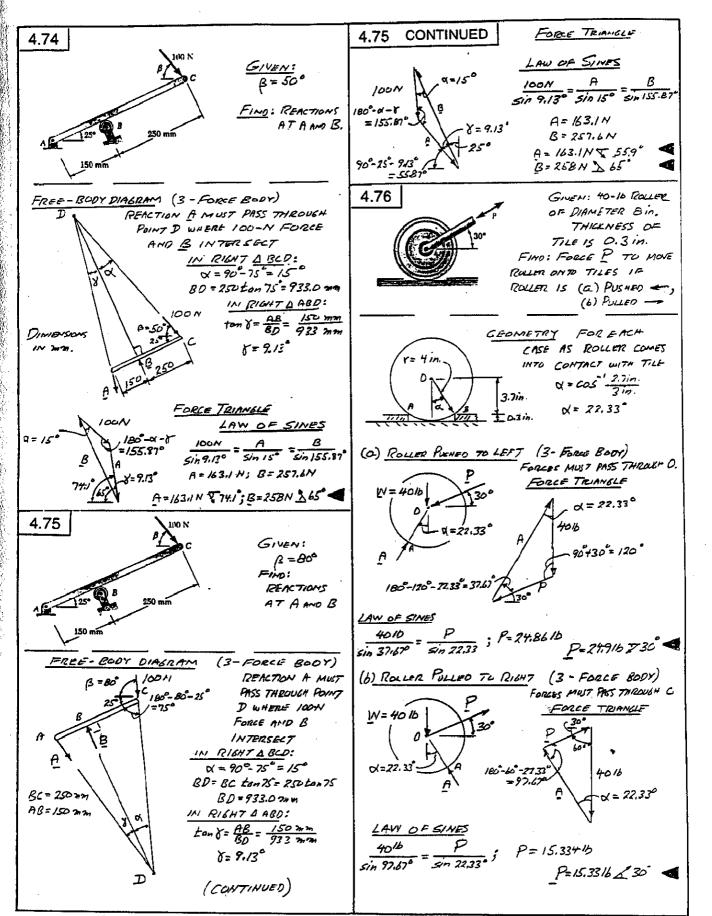


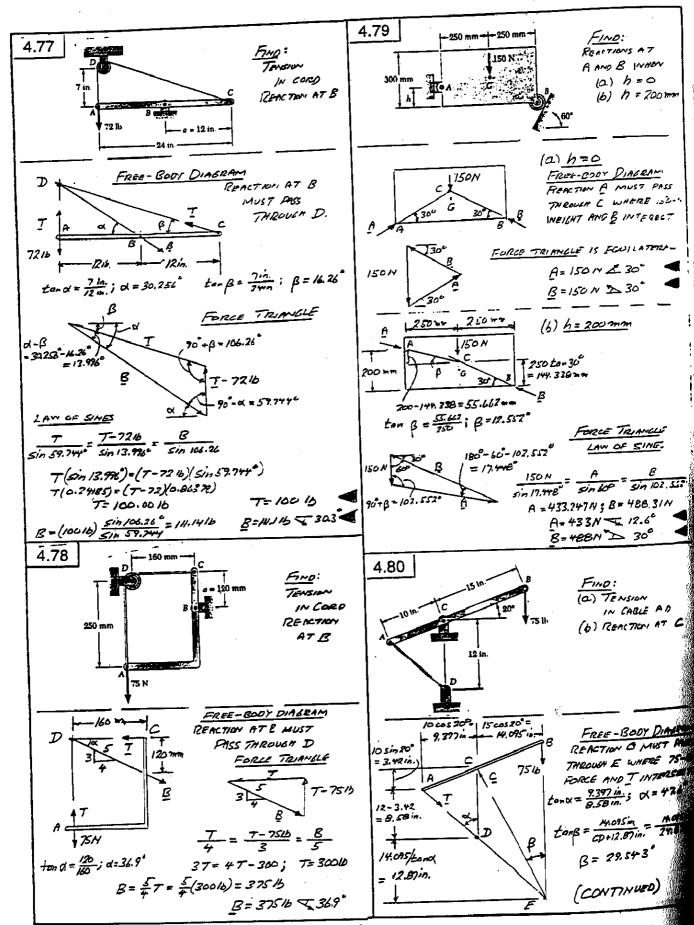
FORCE TRIANGLE (3 FUNCE INTERSECT AT E) W=(50 ftg)9.81m/s2=490.5N

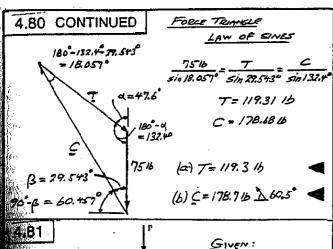


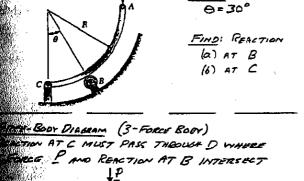
$$\frac{490.5N}{\sin 29.278^{\circ}} = \frac{T_{co}}{\sin 95.722^{\circ}} = \frac{B}{\sin 55^{\circ}}$$

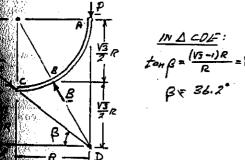
$$T_{co} = 992.99N ; B = 521.59N$$
(a) $T_{co} = 99BN$
(b) $B = 872N = 5.7^{\circ}$



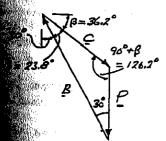


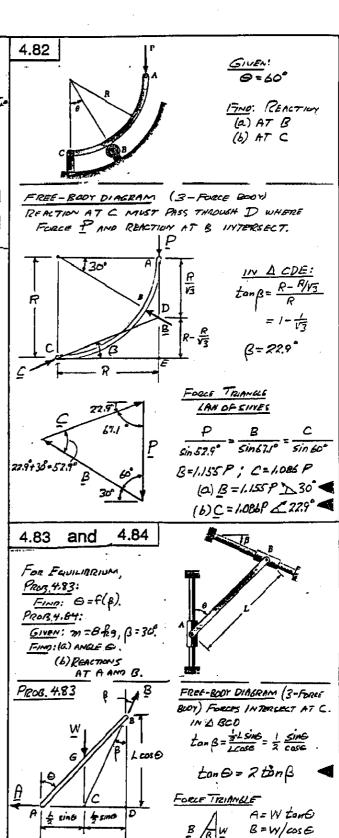






TRANCLE





m = 8Ag; W=(8Ag) 9.81 7952 = 78.48N, B = 30

G=49.1°

B= 90.6N & 60°

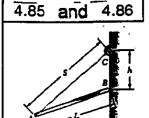
A= 45.3N-

Pros. 4.84

GIVEN:

(a) ton0 = 2ton 30° = 1.1547

(b) A= W tonβ = (78.48N)tan 30° B=W/cosβ = (78.48N)/cos 30°



PROB. 4.85:

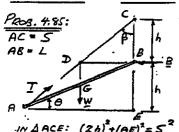
Fing: EXPRESSION FOR h IN TERMS OF SAMOL

Pros 4.86:

GIVEN: L=20in., S=30in., AND W=1015

FIND: (a) DISTANCE h (b) TENSION IN AC

(4) REACTION AT B



FREE-BODY DIAGRAM (3-FORCE BOOT) THE FORCES WI AM B MUST INTERSECT AT D

ON LINE OF ACTION OF T.

IN A ACE: (26) + (AE) = 52 n2+(A2) = L IN A ABES

(2)

(i)

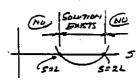
362=52-62 EG(1)-EG(2):

(3) $h = \sqrt{(5^2 - L^2)/3}$

AS LENGTH S INCREASES RELATIVE TO L, ANGLE @ INCORNSES UNTIL ROD AB IS VERTICAL AND



h≥5-L V(5-19/2 2 5-L $5^2 - L^2 \ge 3(5^2 - 25L + L^2)$ 0 2 25 2-651+4L2 02 Z(5-L)(5-2L)

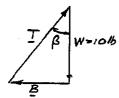


: NO SOLUTION FOR 5>2L

Pros 4.86 L=20 in., S= 30 in., W=1016 $h = \sqrt{(S^2 - L^2)/3} = \sqrt{(30^2 - 20^2)/3} = \sqrt{500/3}$ h=12.91 in.

IN A ACE: cosp = 2h = 2(12.9/in) = 0.8607 B = 30.609

FORCE TRIANGLE

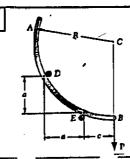


$$T = \frac{W}{\cos \beta} = \frac{10.15}{\cos 30.609}$$

(b) T= 11.6216

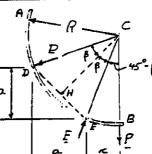
B = W tan B = (1016) ton 30,609

(c) B=5.9216 -



GIVEN: a= 20 mm P=100mm

FIND: DISTANCE C CORRESPONDING TO EQUILIBRIUM



: SLUPE OF CH 15 & 45° DE = VZ a

SLUPE OF DE 15 A5

DH=HE= IDE= VZ a

IN A DHC AND IN ACEN: $\sin\beta = \frac{\sqrt{2}a}{R} = \frac{a}{\sqrt{2}R}$ C = R sin(45 -β)

FOR a=20mm, R=100mm

C= (100 mm) sin (45°-18:13)

rc = 60.0 m

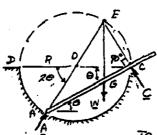


4.87



GIVEN: RADIUS OF BOWL IS R.

FINO: ANGE 6 FOR ECUILIBRIUM



FREE-BOOT DIAGRAM (3- FORCE BODY)

POINT E IS POINT OF INTER SECTION OF A AND E.

SINCE A PASES THROUGH O AND SINCE C IS PERPENDICULAR

TO ROD, TRIANGLE ACE IS A RIGHT TRIANGLE INSCRIBED IN THE CIRCLE. THUS E IS A PONT ON THE CIRCLE.

NOTE THAT LOOK IS THE CENTRAL ANGLE CORRESPONDING TO THE INSCRIBED ANGLE DCA. THUS Z DOA = 20

HORIZONTAL PROJECTIONS OF AF AND AS ARE EQUAL. (AF) COS 26 = (AG) COS 6

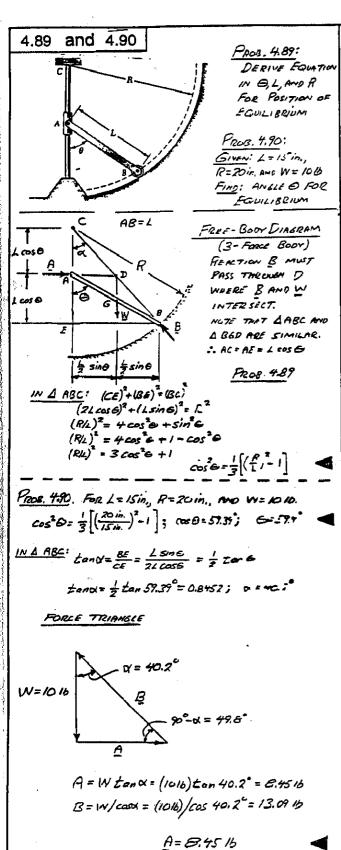
(2R)cos 20 = (R)cos @ 567: cos 20 = 2 cas 20 -12 4 cos 0 - 2 = cos 0 4 605 6 - 0056 - 2 = 0

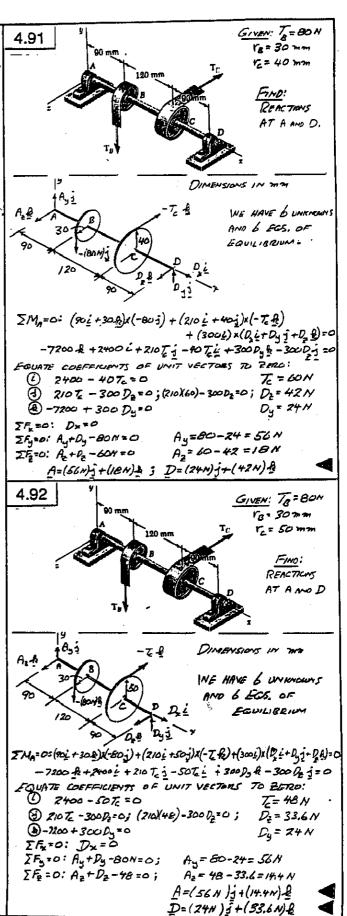
COS 6 = 0.84307

&= 32,5°

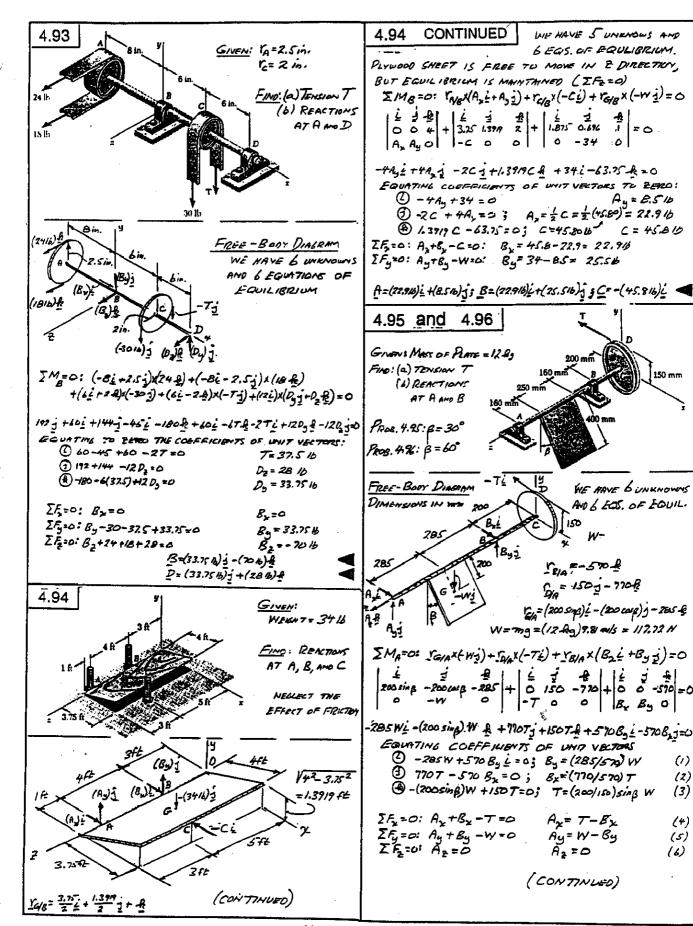
COSG =-0.59307

6= 126.4" (DISCARD)





B=13.0916 1 49.8°



150 mm

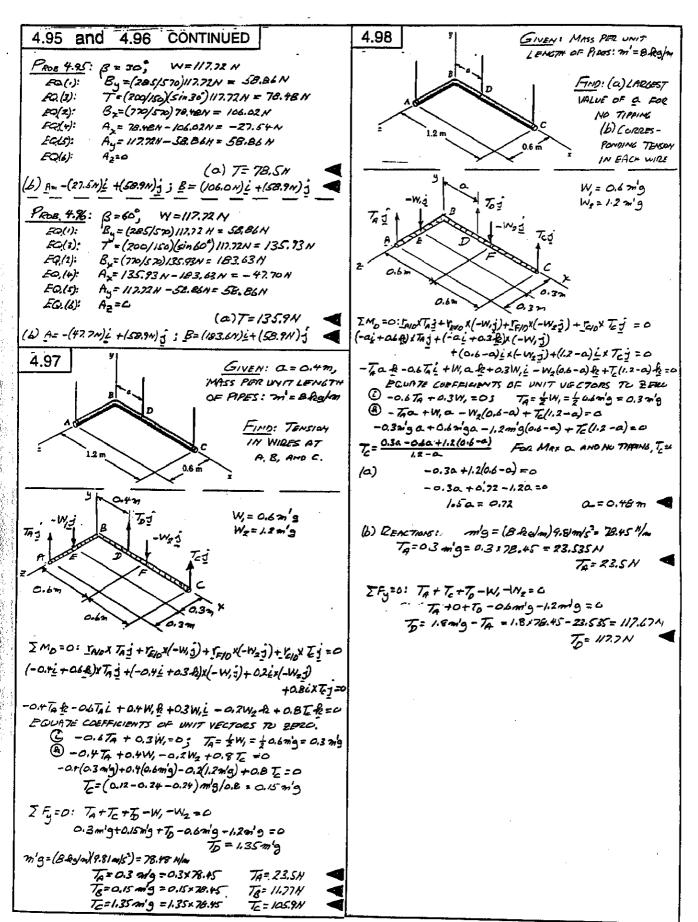
(1)

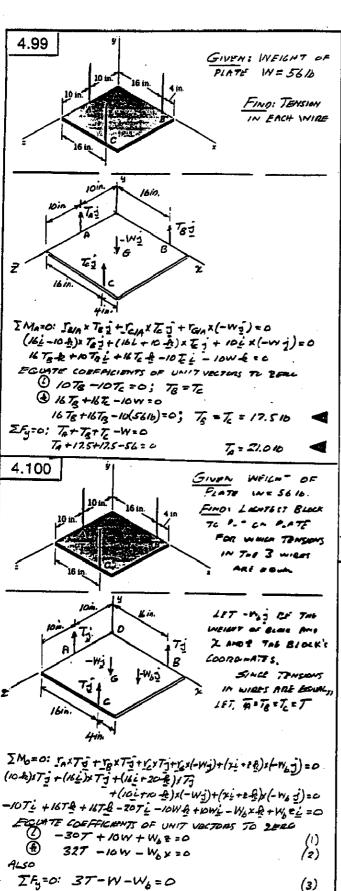
(z)

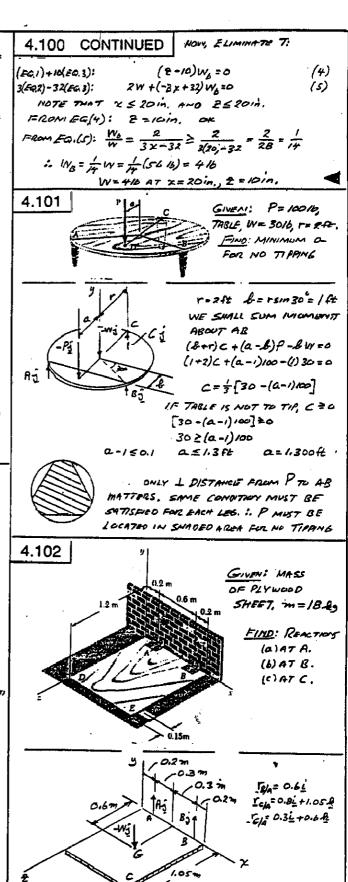
(3)

(4)

(5) (6)







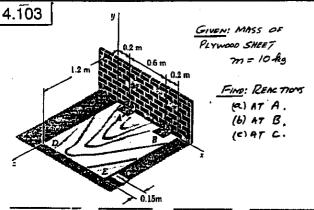
W=mg=18Ag)9.81 W=176.58 N

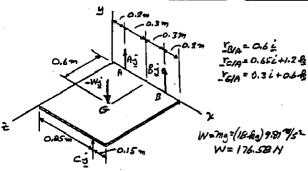
(CONTINUED)

(CONTINUED)

4.102 CONTINUED

∑MA=0: _V&A × B j + YA × C j + YA × (-VV j) = C (C, 6 f) × B j + (O £ i + 1, O S £) × C j + (O 3 £ + O 6 €) × (-W j) = 0 0.6 B £ f 0.8 C £ - 1.0 S C £ - D .3 W £ + 0.6 W £ = C £CLATE CCEFACIENTS OF UNIT VECTORS TO \$ERD. ① -1.0 S C + O 6 W = 0 ; C = (O .6 / 1.0 S) 176.58 N = 100.90 N ② 0.6 B + 0.8 C = 0.3 W = 0 0.6 B + 0.8 (D .0 M) - 0.3 (176.58 N) = 0, B = -46.24 N 1 ∑Fy=0: A + B + C - W = 0 A - 46.24 N + 100.90 N + 176.58 N = 0, A = 121.92 N (Q) A = 121.9 N (b) B = -46.2 N . (c) C = 100.9 N





IM4=0: IBH × Bj + Ych × Cj + Gh × (-Vyj)=0

0.6 i × Bj + (0.65 i + 1.2 f) × Cj + (0.3 i + 0.6 f) × (-Wj)=0

0.6 Bf + 0.65 Cf - 1.2 Ci - 0.3 Wf + 0.6 Wi = 0

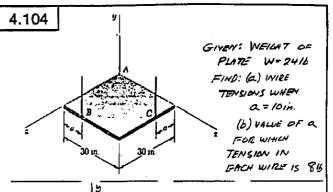
EQUATE COEFFICIENTS OF UNIT VECTORS TO ZERO.

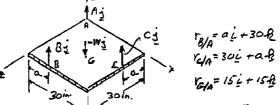
- (-1.2C +0.6W=0; C=(0.6/1.2)176.68N= 88.29N
- (4) 0.68 + 0.65C -0.3W =0 0.68 + 0.65(88,89N)-0.3(18,58N) =0

B = -7.36 N $\sum F_{n} = 0: A + B + C - W = 0$

A-7.36N+88.29N-176.88N=0 A=95.648N

(a) A = 95.6 N. (b) - 7.36 N. (c) 88.3 N





BY SYMMETRY: B = C \[\begin{align*} & \mathbb{L} & \mat

$$B = \frac{15W}{30+\alpha} \qquad C \neq B = \frac{15W}{30+\alpha} \qquad (1)$$

$$IF_y=0$$
: $A+B+C-W=0$
 $A+2\left[\frac{15W}{30+a}\right]-W=0$; $A=\frac{aW}{30+a}$ (2)

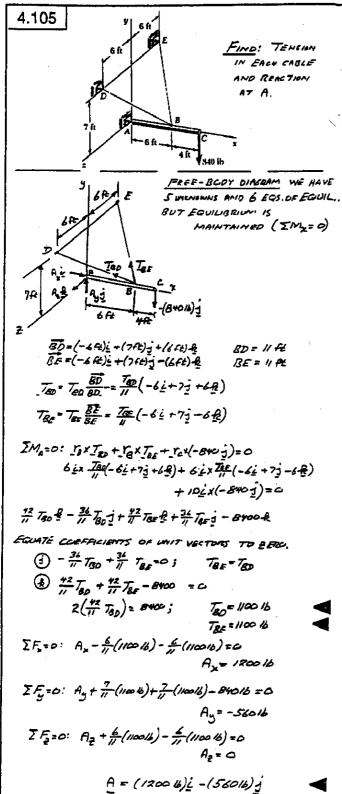
(a) For
$$\alpha = 10 in$$
.
EQ.(1) $C = B = \frac{15(2416)}{30+10} = 916$

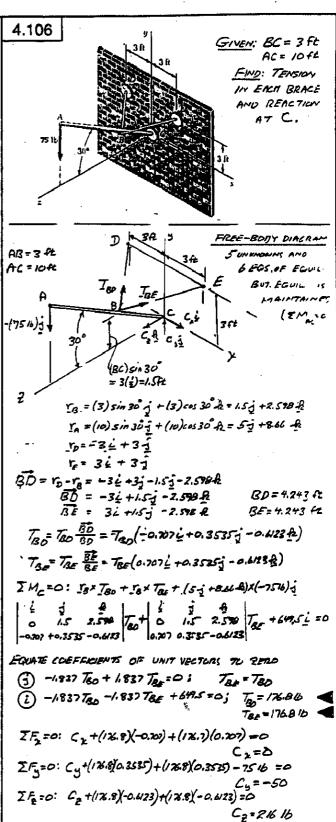
$$EG_{1}(z)$$
 $A = \frac{10(2416)}{30+10} = 616$

(b) FOR TENSION IN EACH WIRE - 816

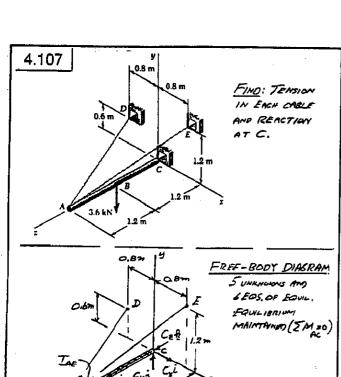
$$30in.+a = 45$$

 $a = 15 in.$





C=-(5016)j+(21616)&



rg= 1.2 de To = 2.+-6

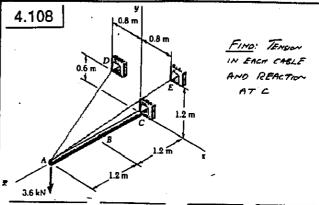
$$\begin{split} & \sum M_{e} = 0: \ \, \underbrace{Y_{A} \times T_{AD} + Y_{A} \times T_{AE}}_{T_{AE}} + \underbrace{f_{B} \times (-3 - RN)}_{J} = 0 \\ & | \underbrace{i}_{J} \quad \underbrace{f_{B}}_{J} \\ & | \underbrace{f_{AD}}_{J} + \underbrace{f_{AD}}_{J} + \underbrace{f_{B} \times (-3 - RN)}_{J} = 0 \\ & | \underbrace{f_{AD}}_{J} + \underbrace{f_$$

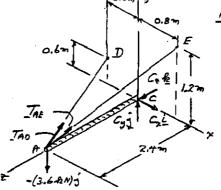
$$T_{A0} = 0.92857 T_{AE}$$

$$EO(1): -0.553850.92857) T_{A} = 1.02857 T_{A} + 4.22 - 0.000$$

$$\sum F_{\chi} = 0$$
: $C_{\chi} = \frac{0.8}{2.6} (2.6 \text{ km}) + \frac{0.6}{2.6} (2.8 \text{ km}) = 0$; $C_{\chi} = 0$

$$\Sigma F_g = 0$$
: $C_g + \frac{0.6}{2.6} (2.64n) + \frac{1.2}{2.8} (2.84n) - (3.64n) = 0$





FREE-BODY DINGEAM 5 UNKNOWNS AND 6 Eas. of Eau-EQU. LIBRIUM. MAINTHINED (IMAC= 0)

$$T_{AD} = \frac{\overline{AD}}{AB} = \frac{T_{AB}}{2.6} (-0.8 \pm +0.6 \pm -2.4 \pm)$$

$$\frac{C_{OFFF, OF L}: -\frac{7_{AD}}{2.6}(0.8) + \frac{7_{AF}}{2.8}(0.8) = C}{7_{AD} = \frac{7.6}{2.8} 7_{AF}}$$
 (1)

COEFF OF
$$j = \frac{T_{AD}}{2.4}(0.6) + \frac{T_{AE}}{2.8}(1.2) - 3.6 - 2N = 0$$

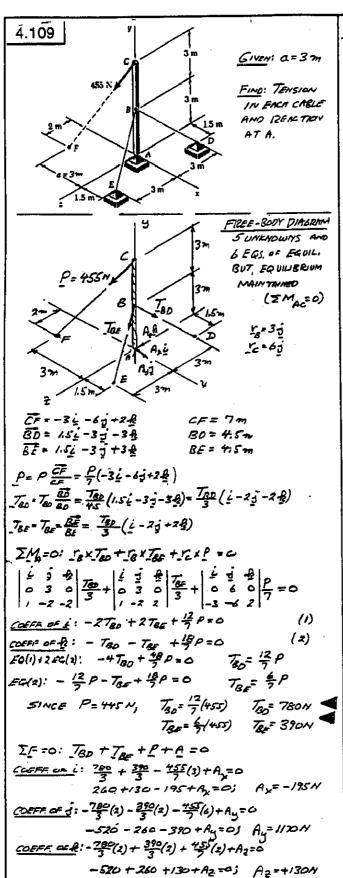
$$\frac{2.6}{2.8}T_{AF}(\frac{0.6}{2.4}) + \frac{1.2}{2.8}T_{AF} - 3.6 - 2N = 0$$

$$T_{AF}(\frac{0.6 + 1.2}{2.8}) = 3.6 - 2N$$

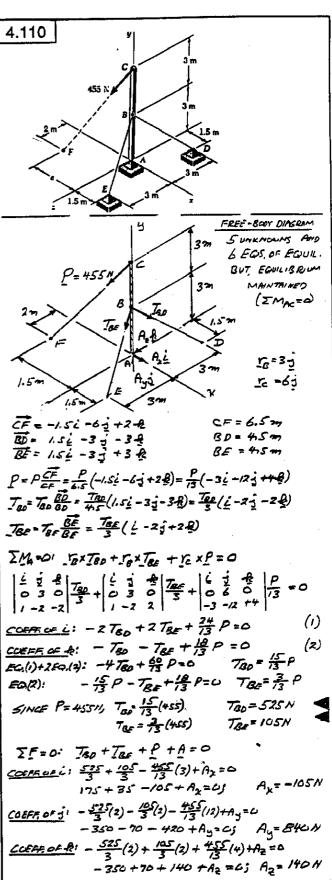
Ify=0:
$$C_y + \frac{C_16}{2.6}(5.2RN) + \frac{1.2}{2.8}(5.6RN) - 3.6RN = C$$

$$\Sigma F_2 = ci$$
 $C_2 = \frac{2.4}{2.6} (5.2 \text{ AN}) - \frac{2.4}{2.8} (5.6 \text{ AN}) = c$ $C_2 = 9.6 \text{ BN}$

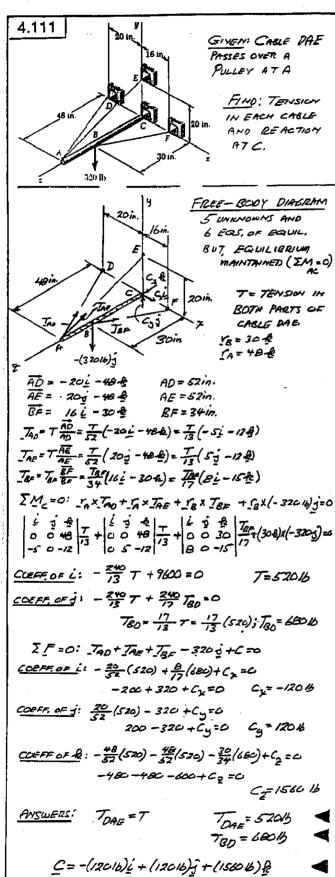
C=(9.6-BN) A MOTE: SINCE FORCES + REACTION ARE CONCURRENT AT A, WE COULD HAVE USED THE METALOS OF CHAPTER 2

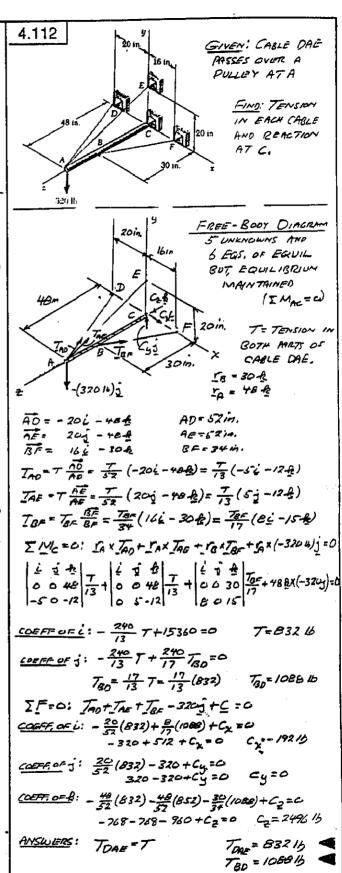


A=-(195N) + (1170N) + (130N) &

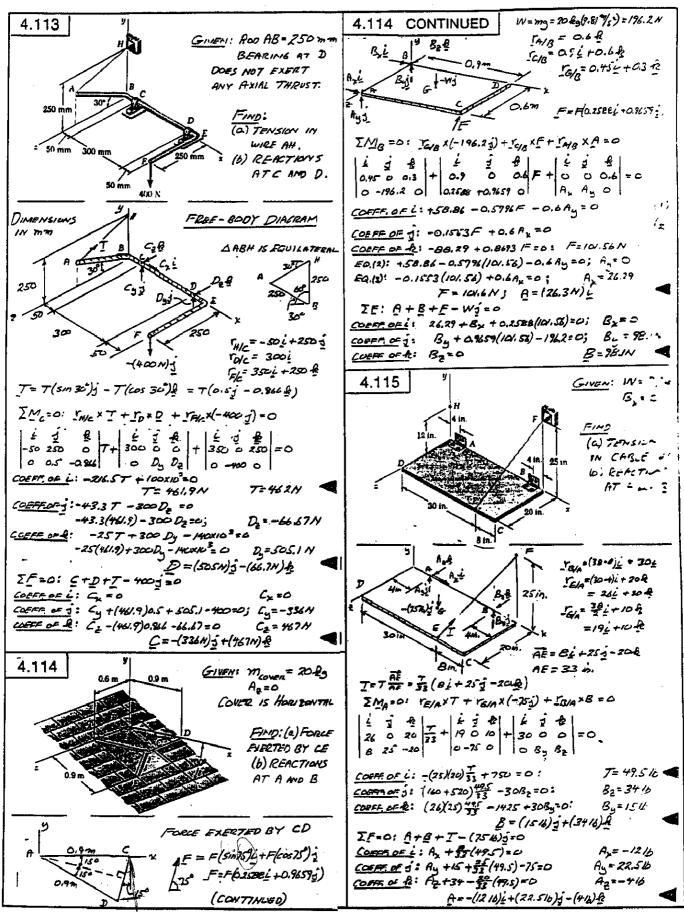


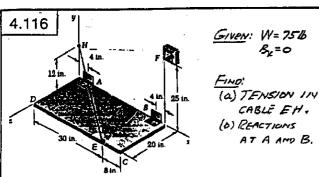
A=-(105N)+(840N) + (140N)&

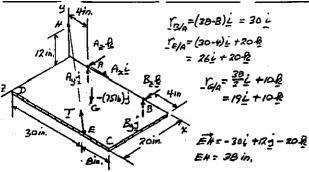




C = - (19216) + (2496 16)-12







$$T = T = \frac{T}{E^{H}} = \frac{T}{3B} \left(-30 + 12 - 20 \frac{R}{2} \right)$$

$$\Sigma M_{A} = 0: \quad \Sigma E_{/A} \times T + \Sigma M_{A} \times (-75 \frac{1}{0}) + \Sigma M_{A} \times B = 0$$

$$\begin{vmatrix} i & j & \frac{1}{2} \\ 26 & 0 & 20 \end{vmatrix} = \frac{T}{3B} + \begin{vmatrix} i & j & \frac{1}{2} \\ 19 & 0 & 10 \end{vmatrix} + \begin{vmatrix} i & j & \frac{1}{2} \\ 30 & 0 & 0 \end{vmatrix} = 0$$

$$\begin{vmatrix} -30 & 12 & -20 \\ -30 & 12 & -20 \end{vmatrix} = 0 -25 c \quad \begin{vmatrix} 0 & 8y & 8z \\ 0 & 8y & 8z \end{vmatrix}$$

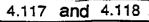
COSEF. OF 1: -(12)(20) T +750=0; T=118.25; T=118.816 ◀ coeffe of j: (-600 +520) 118.75 -3082=0; B2=-8.336

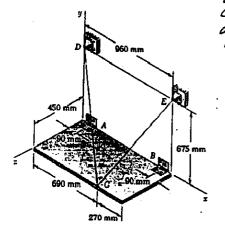
COFFF. OF A: (26)(12) 118.75 -1425+308,=0; By=15.00 B B= (1516) + (8,3316) &

IF=0: A+B+T-(756) ==0

COFFF. OF 1: Ay - 10 (118.75) =C Ax=93.7516 CUEFF. OF 3: Ay +15 + 12 (18.75) - 75=0 Ay= 22.5 16 CCAFE. OF A: A= -8.33 - 30 (18.75) + 0 Az=70.1313

A = (93.816) £ + (22.516) + (20.816) &

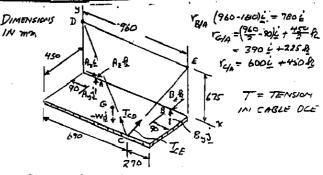




GILLEN: mplate = 100 ftg B2=0 CABLE DOE PASSES OVER PULLEY AT C.

FIND: (a) TENSON IN CARLE DEF. 16) REACTIONS AT A AND B.

4.117 and 4.118 CONTINUED



CD = - 690/ +675-j - 450-f CD = 1065 mm CE = 2701+6753-450-2 CE = B55 mm T= T (-6901+675) -450-A) Top = T (2702 +675 j -450 - 12) W=-mgi--(100 &g)(9.81 m/s2) = -(981 N) 5 PROB. 4.117

IMA = 0: ICIAX TED + ICIA ITEE + ICIAX (-WS)+IBIAX B = 0 600 0 450 1065+ 600 0 450 055+

+ 300 0 225 + 780 0 0 = 0 0-781 0 0 B₃ B₂

CONFF. OF L: - (450)(675) T - (450)(675) T + 220.725 x103 = 0

T= 344.6 N T= 345N

COFFF OF J: (-6706450+600x450) 344.6 +(R708450+6008450) 3446 B= 185.49 N -780/S=0 CORPE, OF A: (600)(675) 3446 + (600)(675) 3446

- 382.592103 + 780B45 By=//3.2N

IF=0: A+B+ To+To+W=0 = (1/3.2N) + (185.5N) & COST. OF L: Az - 600 (3446) + 270 (2446) =0; COFFE OF 1: Ay + 13.2 + 105(244.4) + 25(3414) - 20 = 0; Ay = 377 N COFFE OF 1: Ay + 18.5 - 1045 (344.4) - 25 (344.4) = 0; Ay = 377 N

A=(144N)++1377N)+(14.5N).A PROB. 4.118

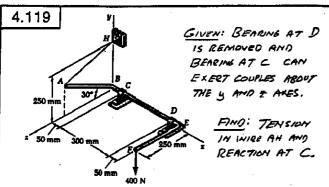
EMA=0: TOUXE + TOUX(-W3)+YOUXB=0 \(\frac{1}{2} \) \(\frac{1} \) \(\frac{1}{2} \) \(\frac{1}{2} \) \(\frac{1}{2} \) \(\frac{ 0-181 0 0 By 82

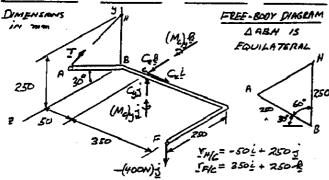
<u>COFFF OF L</u>: -(450) 675) T T=621,3N T=621N 🗲 <u>CORFE OF</u> 1= (270×450 +600×450) 621.3 - 780B2+0; B2-364.7 N CORP. OF A: (600)(675) 6713 - 382,5910 + 780850; B= 113.2N B=(113.2N) 5+(365 N) fe

IF=0: A+B+ TestW=0

COEFF OF L: Ay + 270 (6213)=0 Az=-1962N COFFF. OF 9: Ay + 1/3.2 + 675 (621.3) -981=0; Ay= 377.3N COFFF. OF A: A2 + 364.7 - 450 (621.3)=0

A=-(196.2N)+(377N)-3-(37.7N)A





T= T(sin 30) j-T(cos 30) k = T(0.5 j - 0.84 k) IMC=0: _ TE/EX (-400 j) + YA/EXT + (Me) j f+ (Me) & = 0 -20 520 0 T+(ME) 3+(ME)= =0 350 0 250 0 0.5 -0.866

COEFF. OF. L: + 100x103-216.5 T=0; T=469N; T=462N

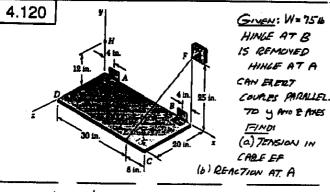
(Mc) = 20×0 Nom; (Mc) = 20×0 Nom;

(Mc) = 151.57x10 Nomm; (Ma)=157.5 Nom IF=0:C+T-4001-0-5

Me= (20 Nom) 1+(151, 5Nom) 4 COFFE. OF E: Cy EO Cx = 0

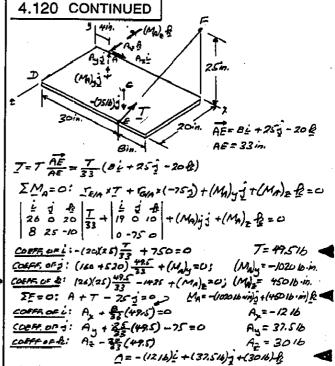
COPFF. OF 1: Cy + 0,5(461,9) =400=0
COPFF. OF &: C2 -0,866(461,9)=0 C.F 169,1N

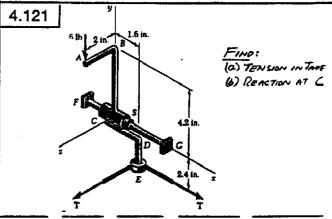
= 400 N C= (169.1N) + (400N) &

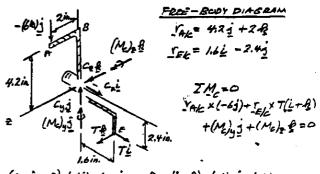


YEM= (30-4) + +204 = 26 + 20 & 16/A = (0.5×38) i +10-12 = 19 i + 10-12

(CONTINUED)





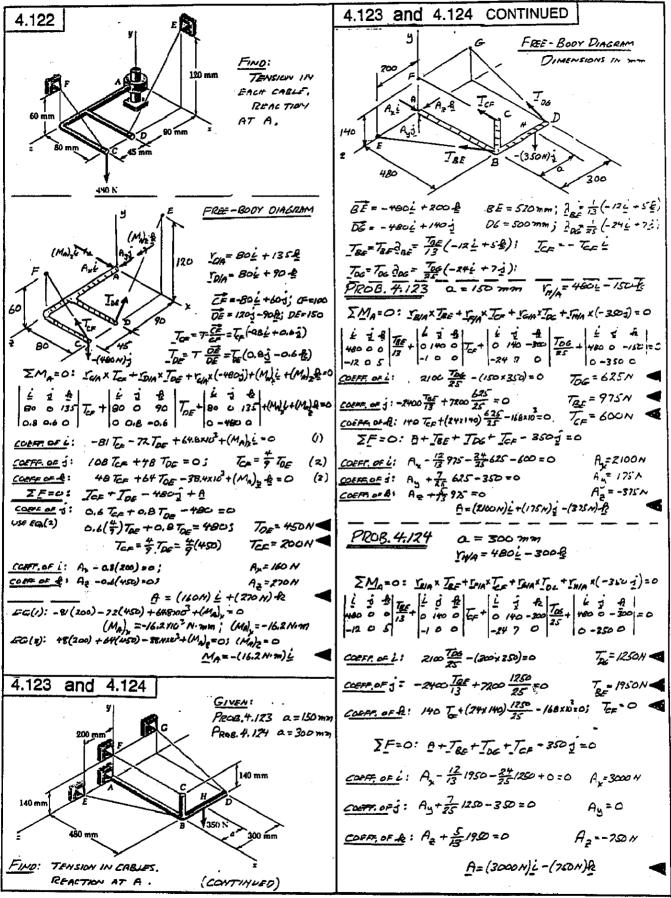


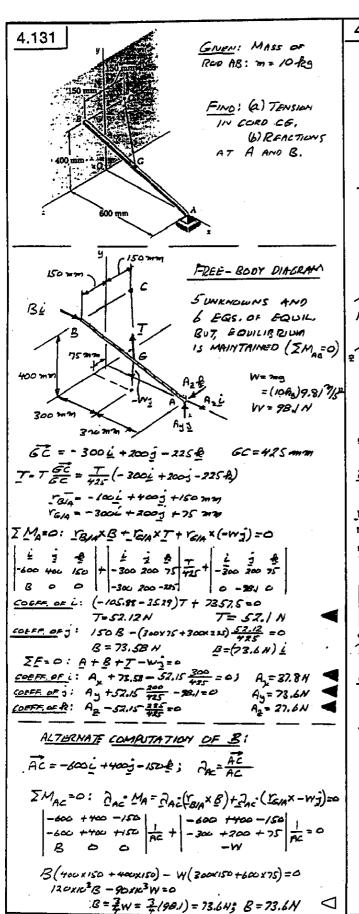
(42=+2=)x(-6=)+(16=-2.4=)xT(=+=)+(M),=+(Mc)==== 12-2.47=01 CORFF. OF L アニダル -1.6(54)+(Me)y =0 (Ma) = B 16 · in. (Ma) = -1216 · in. COPPE OF S: 2.4(54) + (Me) = 0 cceff.of &:

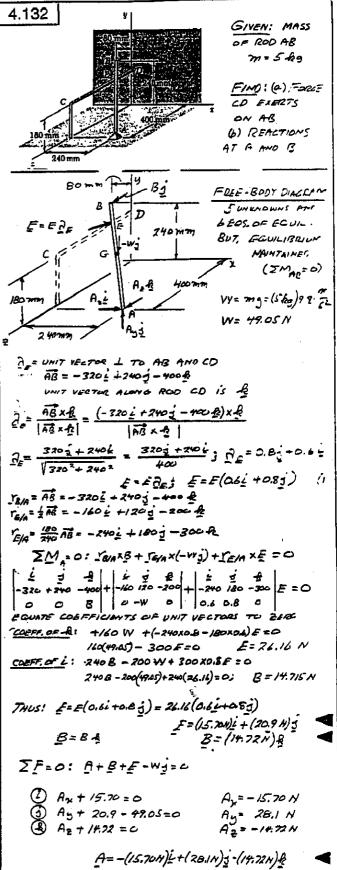
M=(810-10) f-(1210-10) &

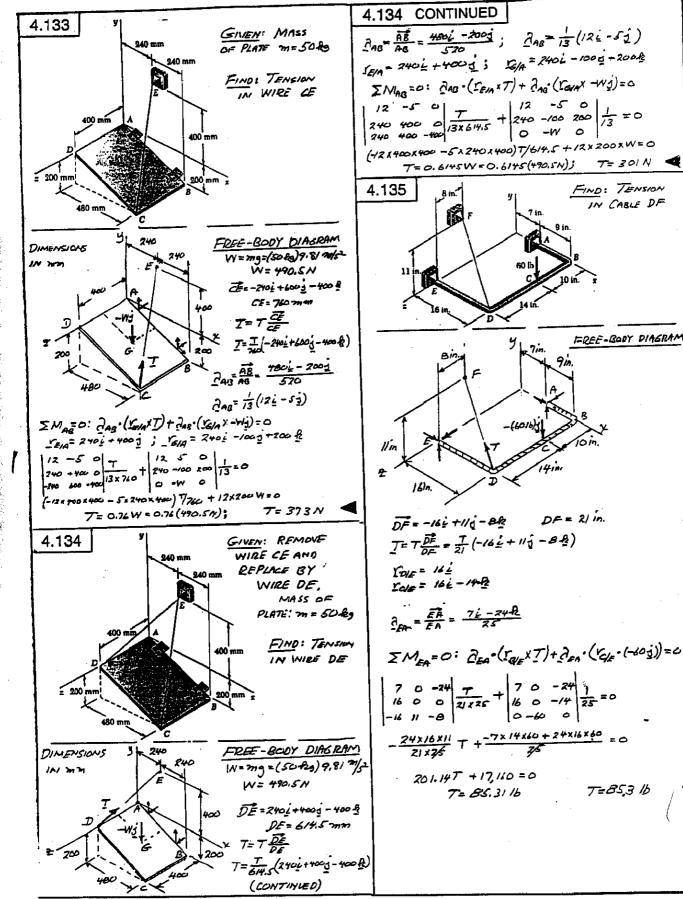
EF=0: C, i+Cy i+C=E-(614) j+(514) i+(614) f=0

EGUATE COFFFICIENTS OF UNIT VELTORS TO 2012 Cy = 616 Cz = -54 C=-(516)+(616)-j-(516)-B Cx=-516







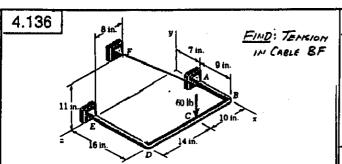


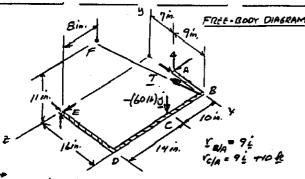
FIND: TENSION

IN CABLE DE

FREE-BODY DIAGRAM

T=853 B



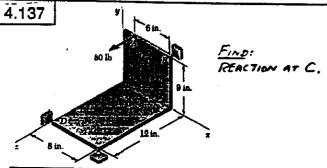


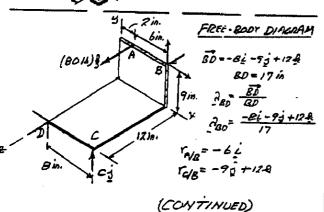
$$\overrightarrow{BF} = -16\underline{i} + 1/\underline{j} + 1/\underline{k} \qquad BF = 25.16 i_{\text{m}}.$$

$$T = T \frac{\overrightarrow{BF}}{\overrightarrow{BF}} = \frac{T}{26.16} \left(-16\underline{i} + 1/\underline{j} + 1/\underline{k} \right)$$

$$R_{AE} = \frac{R_{E}^{2}}{R_{E}} = \frac{7L - 244}{25}$$

T= 18/.716

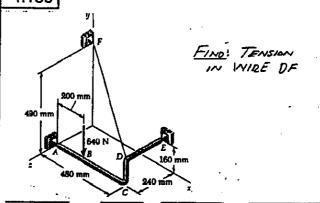


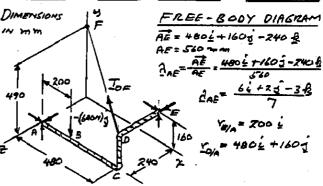


4.137 CONTINUED

$$\begin{split} & = M_{BD} = 0: \quad \frac{\partial}{\partial s_{0}} = \left(\sum_{l,k} - \frac{c}{c} \right) + \frac{\partial}{\partial s_{0}} = \left(\sum_{l,k} - \left(\frac{c}{b} \right) + \frac{c}{b} \right) = 0 \\ & = \frac{c}{c} - \frac{c}{c} \cdot \frac{c}{l} + \frac{c}{c} = \frac{c}{c} - \frac{c}{l} \cdot \frac{c}{l} = 0 \\ & = \frac{c}{l} \cdot \frac{c}{l} + \frac{c}{c} \cdot \frac{c}{l}$$

4.138





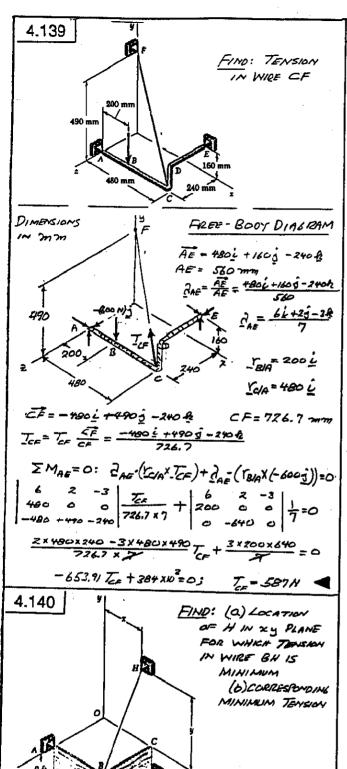
DF = -480 1 + 3301 - 240 k; DF = 680 --
TOF = TOF OF = TOF -4801 + 3303 - 240 k = TOF - 161 + 1/3 - 8 k

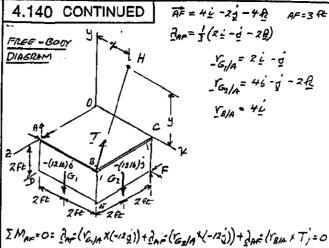
$$\sum_{AE} M_{AE} = \sum_{AE} (Y_{MA} Y_{DE}) + \sum_{AE} (Y_{G/A} \times (-600\frac{1}{2})) = 0$$

$$\begin{vmatrix} 6 & 2 & -3 \\ +60 & 160 & 0 \end{vmatrix} \frac{7ac}{21 \times 7} + \begin{vmatrix} 6 & 2 & -3 \\ 200 & 0 & 0 \end{vmatrix} \frac{1}{7} = 0$$

$$\frac{-6x \text{ Hox} 8 + 2x \text{ HeBO} \times 8 - 3x \text{ HeBO} \times 111 - 3x \text{ Hox} 16}{21 \times 7} + \frac{3x \text{ 200 x 6 to}}{27} = 0$$

· Toz = 343N





 $\begin{vmatrix} 2 & -1 & -2 \\ 2 & -1 & 0 \end{vmatrix} \frac{1}{3} + \frac{1}{4} - 1 & -2 \end{vmatrix} \frac{1}{3} + \frac{1}{1} A F^{*}(fB/A \times T) = 0$ $(2 \times 2 \times 12) \frac{1}{3} + (-2 \times 2 \times 12 + 2 \times + 112) \frac{1}{3} + \frac{1}{1} A F^{*}(fB/A \times T) = 0$ $A_{AF^{*}}(fB/A \times T) = -32 \quad OR, \quad T^{*}(fA_{AF^{*}} \times f_{B/A}) = -32 \quad (1)$ $PROJECTION OF \quad T \quad ON \quad (\frac{1}{1} A_{AF^{*}} \times f_{B/A}) \text{ is constaint. Thus, }$ $T_{min} \quad 1S \quad PARALLER \quad TO$ $A_{AF^{*}} \times f_{B/A} = \frac{1}{3}(2 \cdot - \frac{1}{2} - 2 \cdot \frac{1}{2}) \times 4 \cdot \frac{1}{3}(-0 \cdot \frac{1}{2} + 4 \cdot \frac{1}{2})$ $CORRESPONENC \quad UNIT \quad VECTOR IS \quad \frac{1}{\sqrt{5}}(-2 \cdot \frac{1}{2} + \frac{1}{4}) \cdot \frac{1}{\sqrt{5}}$ $EQ(1): \quad T_{S^{*}}(-2 \cdot \frac{1}{2} + \frac{1}{4}) \cdot \left[\frac{1}{3}(2 \cdot \frac{1}{2} - 2 \cdot \frac{1}{4}) \times 4 \cdot \frac{1}{2} \right] = -32$ $T_{VS^{*}}(-2 \cdot \frac{1}{2} + \frac{1}{4}) \cdot \frac{1}{3}(-6 \cdot \frac{1}{2} + 4 \cdot \frac{1}{4}) = -32$

$$\frac{T}{3VS}(16+4) = -3Z; \quad T = -\frac{3VS(32)}{20} = 4.8 VS$$

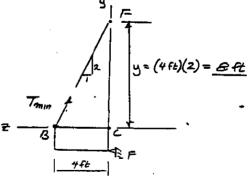
$$T = 10.733 \text{ 16}$$

$$EG.(2) \quad T_{min} = T(-2\underline{1} + \underline{1})\frac{1}{VS}$$

$$= 4.8VS(-2\underline{1} + \underline{1})\frac{1}{VS}$$

$$T_{min} = -(9.616)\underline{1} + (4.816\underline{1})$$

SINCE Tom HAS NO L' COMPONENT, WIRE BH
15 PARALLEL TO THE 48 PLANS, AND X=4FE

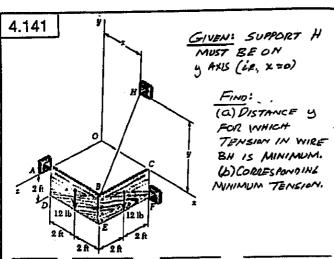


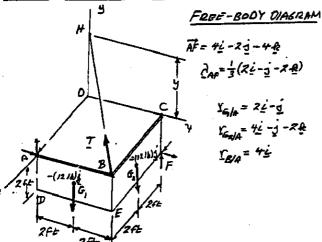
4-43

(CONTINUED)

PLATE! m = 50 kg

 $\hat{A}_{SN} = \frac{ER}{EA} = \frac{7E - 27}{25}$





IM = 0: dai((-12) + dai(() () + dai () () + dai () + dai () () + dai () + $\begin{vmatrix} z & -1 & z \\ 2 & -1 & 0 \end{vmatrix} \frac{1}{3} + \begin{vmatrix} z & -1 & z \\ + & -1 & -2 \end{vmatrix} \frac{1}{3} + \frac{1}{2} \frac{1}{4} + \frac{1}{2} \frac{1}{4} \times \frac{1}{4} = 0$ 0-120 0-120 (222x12) = + (-2x2x12+2x4x12) = + dag ((21x X T) = 6 2Ap. (YBIAXT)=-32 (1)

BN = -41+43-4-B BH = (32+7) 1/2 T= T 84 = T -46+41-4R (32+42)12

 $\hat{C}_{Ac}(r_{BH} \times 7) = \begin{vmatrix} 2 & -1 & -2 & T \\ 4 & c & c \\ -4 & 4 & -4 \end{vmatrix} = \frac{7}{3(3z+4^2)} \cdot 2^{-3} - 32$

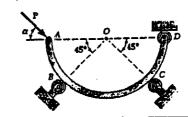
 $(-16-8y)T = -3x32(32+y)^{1/2}$ $T = % \frac{(32+y)^{-1}}{8y+16}$

 $\frac{dT}{dy} = 0: \% \frac{(8y+4) \frac{1}{2}(32+y^2)^{-1/2}(2y) + (32+y^2)^{1/2}(6)}{(8y+46)^2}$

NUMBERATURED: (89+16) y = (32+9²) 8 842+169 = 32x8+84 y=16ft €

FG.(2): 7= % (32+162)1/2 = 11.31316 T= 11.3116

4.142 and 4.143



PRUB. 4.141: FOR X = 45, FIND REALTIONS AT B, C, AND D.

PROB. 4.142: FIND RANGE OF CX FOR EQUILIBRIUM.

FREE-BOOY DIAGRAM Psina PCOSON BNE

+5 IM0=0: (Psina)R-D(R)=0

(2) \$IF=0: PCOSX +B/VI-C/VI=0

+ 1 IF = 0: - Psina + B/VZ + C/VZ - Psina = 0 (3) -28sind +B/V2 +C/V2 =0

(2)+(3): P(cosx -2 sina) + 2B/VZ =0

 $B = \frac{\sqrt{2}}{2} (2 \sin \alpha - \cos \alpha) P$ (m

/2)-(3): P(cosx + 2 sma) - 2C/VZ = 0

C= \$ (2 sind + cosd)P

PROB 4142 FOR X = 45°; SINN = COSK = 1/2 EQ(4): B=VE(是-1/2)P=P; B=PA45°

EG(5): C = \frac{\frac{1}{2}}{2}(\frac{1}{12} + \frac{1}{12})P=\frac{3}{2}P; C=\frac{3}{2}P\delta 45^c \\

D= 9/3 1 EQUI D=PNZ

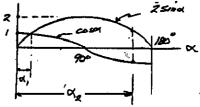
PROB. 4.143 RANGE OF & FOR EQUILIBRIUM

FOR .830:

FROM EG. (4): ZEING -COSK >O

FOR CZO:

From Fa(s): 25ma + cosa 20

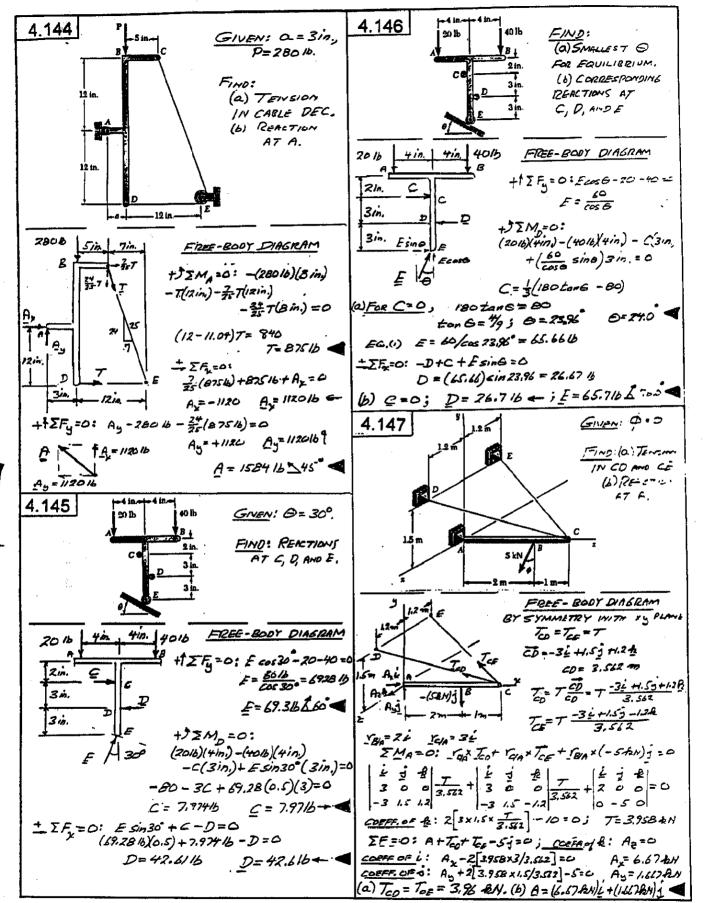


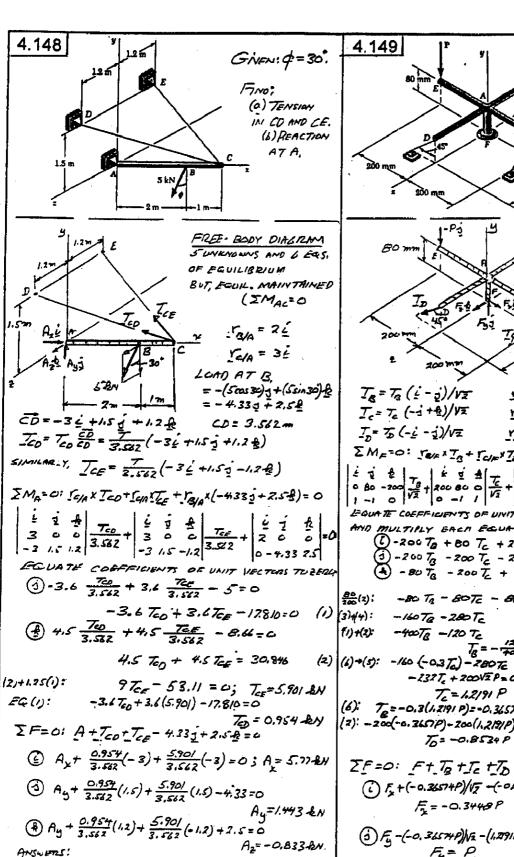
2 SING & COSO, tand, 2 0.5 cx ≥ 26.6°

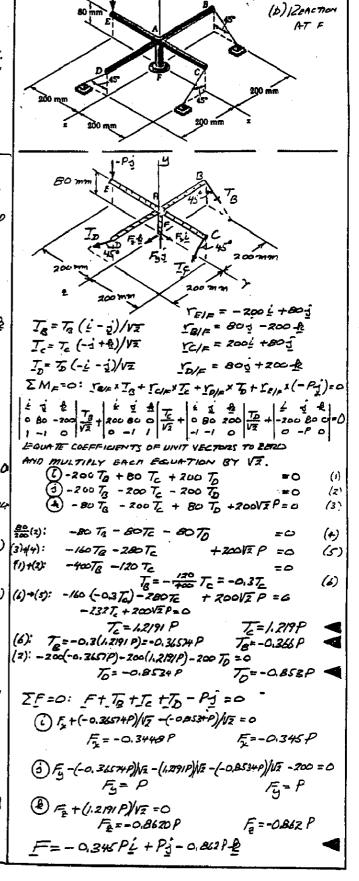
25140 2 - COSX 2 tand2> -0.5 d≥ 153.4°

26.6°≤ × ≤153.4

FOR THIS RANGE SING O, THUS EC(1) YIELDS D>0, OK





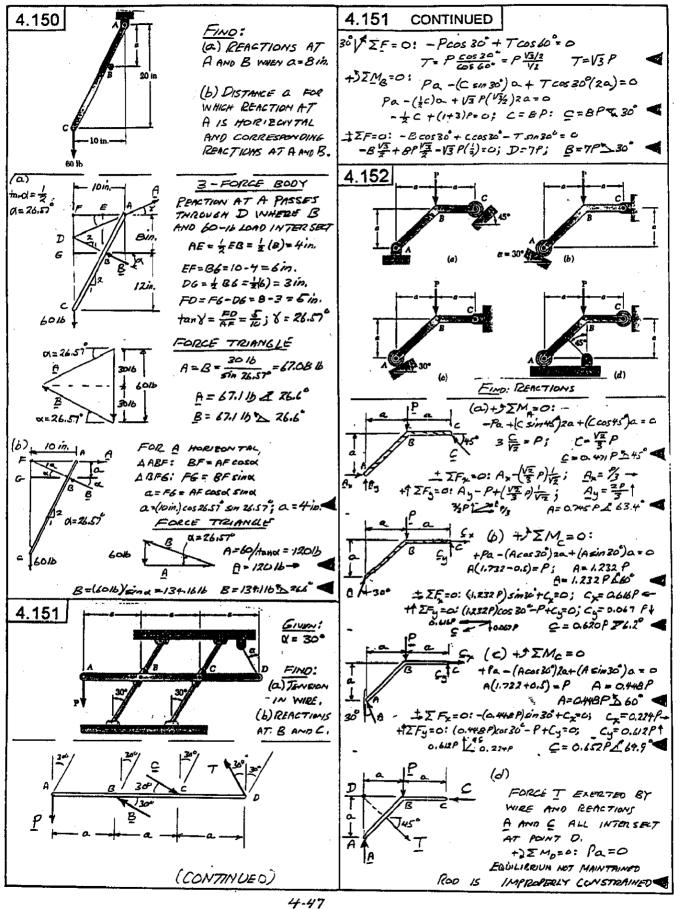


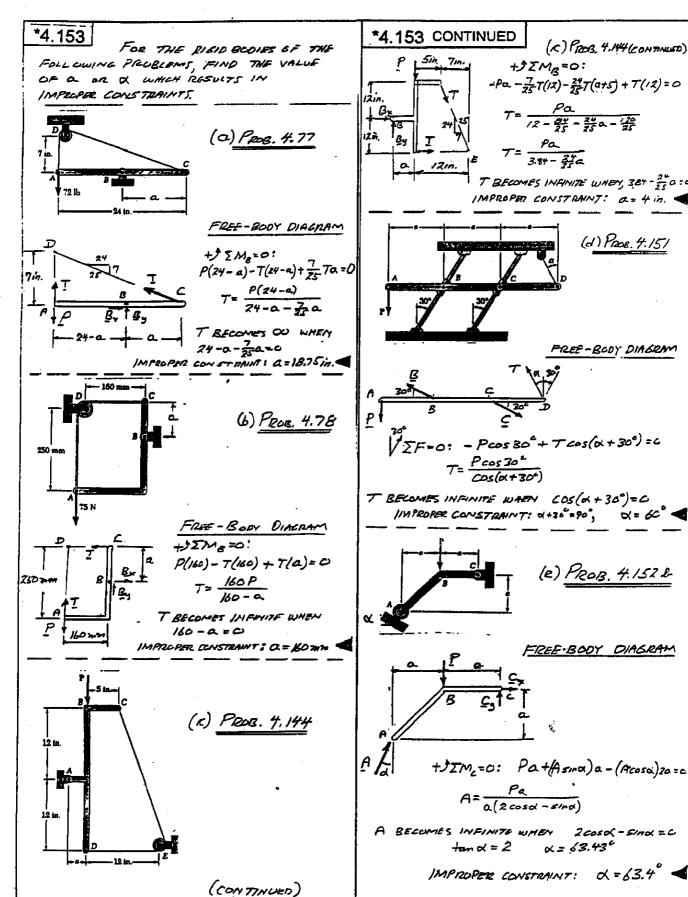
FIND: (a) TENSION IN

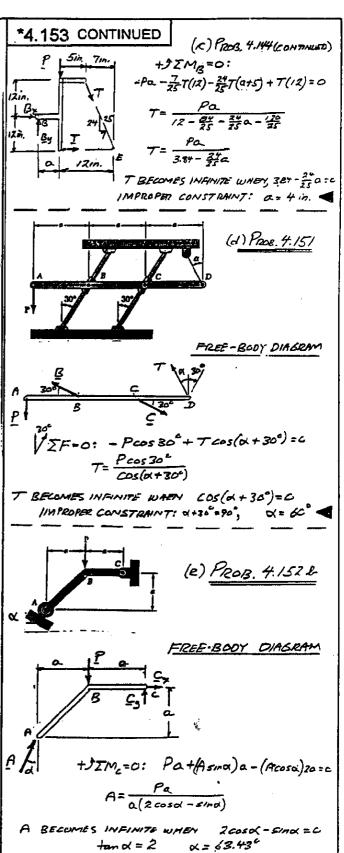
EACH LINK.

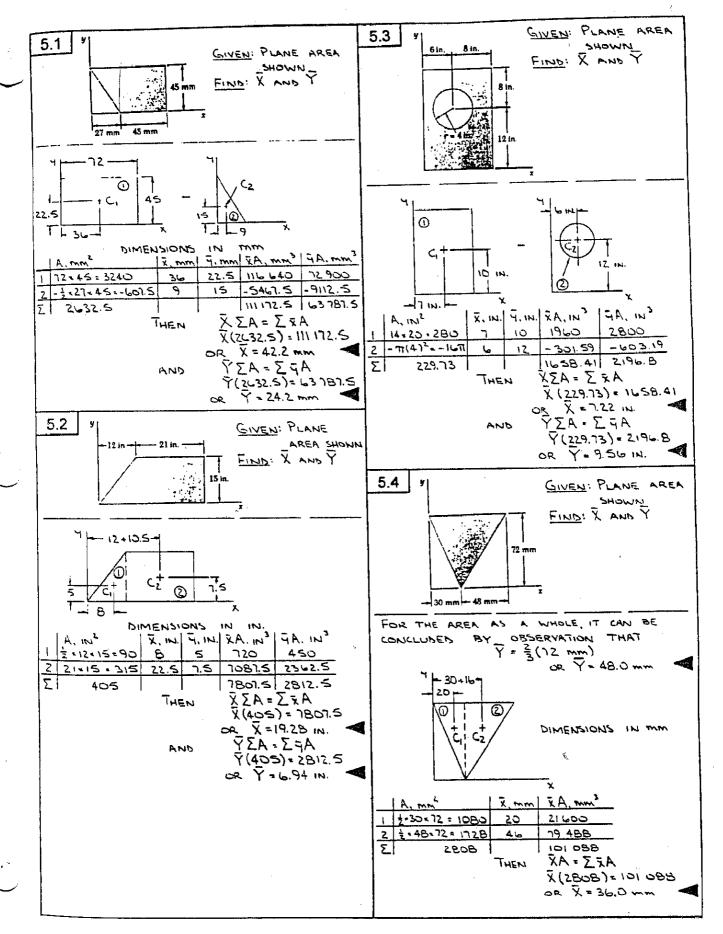
(a) TED=0.954 AN; TE=5.90 AN

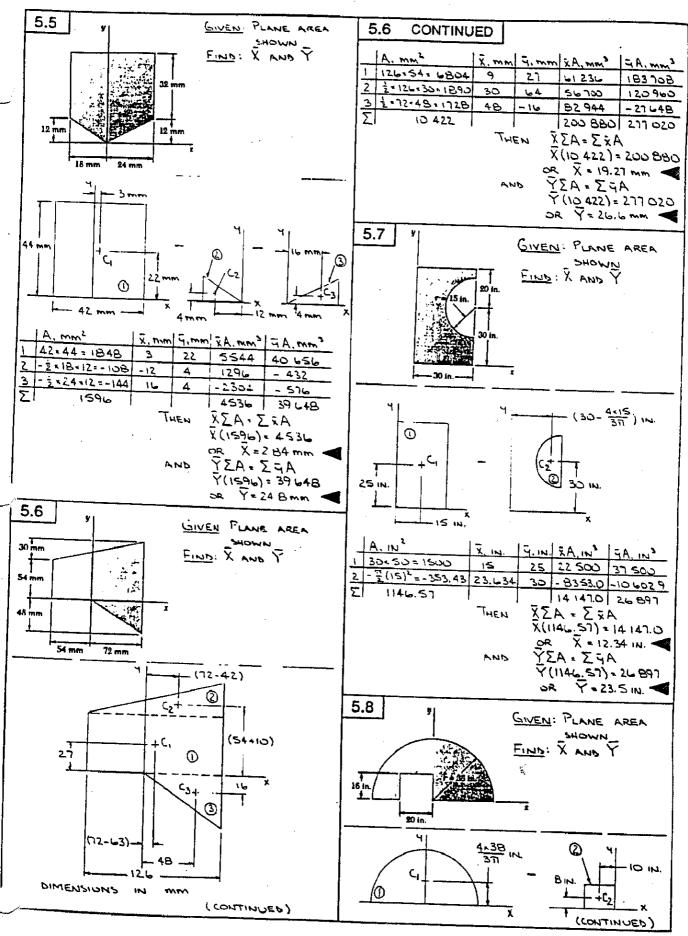
A = (5.77-12N)+(1.443BM) j-(0.833BN) &

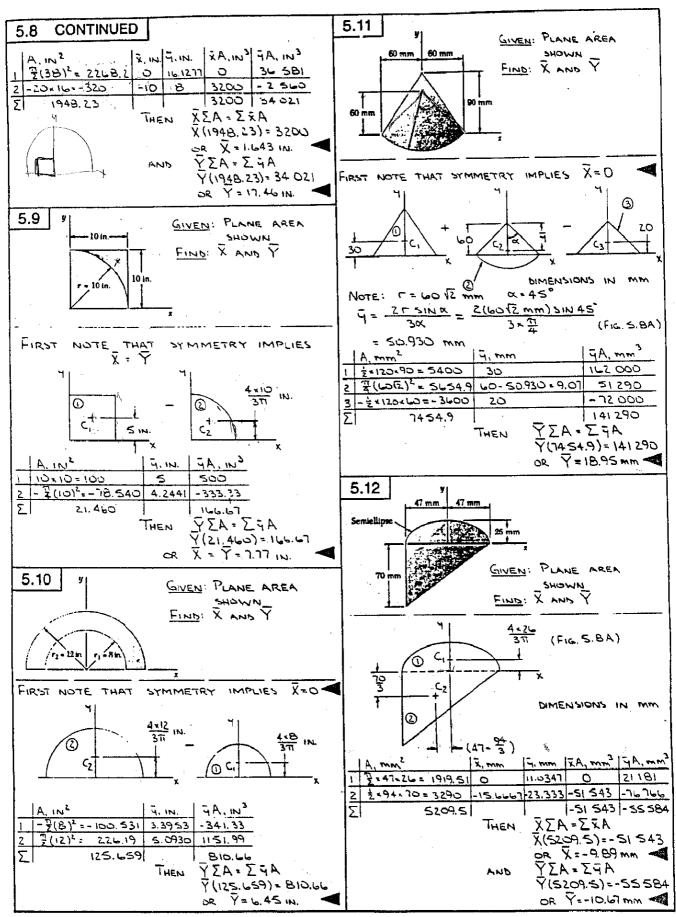






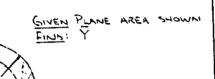




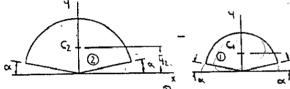


5.16 CONTINUED A. mm² X, mm X, mm XA, mm^3 YA, mm^3 Y

5.17 and 5.18



5.17



$$Fic = \frac{2}{5}L^{2} \frac{\left(\frac{1}{2} - \alpha\right)}{\left(\frac{1}{2} - \alpha\right)} \qquad A^{2} = \left(\frac{1}{2} - \alpha\right)L_{2}^{2}$$

AND
$$\sum A = (\frac{\pi}{2} - \alpha) r_2^2 - (\frac{\pi}{2} - \alpha) r_1^2$$

= $(\frac{\pi}{2} - \alpha) (r_2^2 - r_1^2)$

Now
$$\frac{1}{\sqrt{\sum A}} = \frac{1}{2} \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} \frac$$

5.18 GIVEN: PLANE AREA SHOWN SHOW: Y APPROACHES Y OF AN ARC OF RABOUS \$(\(\Gamma\) + \(\Gamma\) AS \(\Gamma\) - \(\Gamma\)

Using Fig. 5.8B,
$$\overline{Y}$$
 of an arc of radius $\frac{1}{2}(\Gamma_1 + \Gamma_2)$ is $\frac{1}{2}(\Gamma_1 + \Gamma_2)$ $\frac{\sin(\frac{\pi}{2} - \alpha)}{(\frac{\pi}{2} - \alpha)}$

$$= \frac{1}{2}(\Gamma_1 + \Gamma_2) \frac{\cos \alpha}{(\frac{\pi}{2} - \alpha)} \tag{1}$$
(continuely)

GIVEN: PLANE AREA

5.17 and 5.18 CONTINUED

FROM THE SOLUTION TO PROBLEM 5.17 HAVE
$$\frac{1}{2} = \frac{1}{3} \frac{1}{12^{3} - 11^{3}} = \frac{1}{12^{3} - 11^{3}} \frac{1}$$

LET
$$\Gamma_2 = \Gamma + \Delta$$

 $\Gamma_1 = \Gamma - \Delta$
THEN $\Gamma = \frac{1}{2}(\Gamma_1 + \Gamma_2)$
 $\frac{\Gamma_2^2 - \Gamma_1^2}{\Gamma_2^2 - \Gamma_1^2} = \frac{(\Gamma + \Delta)^2 + (\Gamma + \Delta)(\Gamma - \Delta) + (\Gamma - \Delta)^2}{(\Gamma + \Delta) + (\Gamma - \Delta)}$
 $= \frac{3\Gamma^2 + \Delta^2}{2\Gamma}$

IN THE LIMIT AS
$$\Gamma_1 - \Gamma_2$$
, $\Delta \rightarrow 0$. THEN
$$\frac{\Gamma_2^3 - \Gamma_1^3}{\Gamma_2^2 - \Gamma_1^2} = \frac{3}{2}\Gamma$$

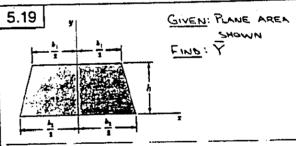
$$= \frac{3}{2} \times \frac{1}{2} (\Gamma_1 + \Gamma_2)$$

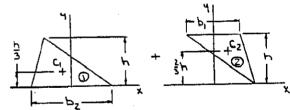
$$= \frac{7}{2} \times \frac{7}{2} \binom{r_1 + r_2}{r_2} \frac{205 \, R}{2 - K}$$

$$= \frac{3}{3} \times \frac{3}{4} \binom{r_1 + r_2}{r_2} \frac{205 \, R}{2 - K}$$

$$= \frac{7}{2} \times \frac{1}{2} \binom{r_1 + r_2}{r_2} \frac{205 \, R}{2 - K}$$

WHICH AGREES WITH EW. (1).



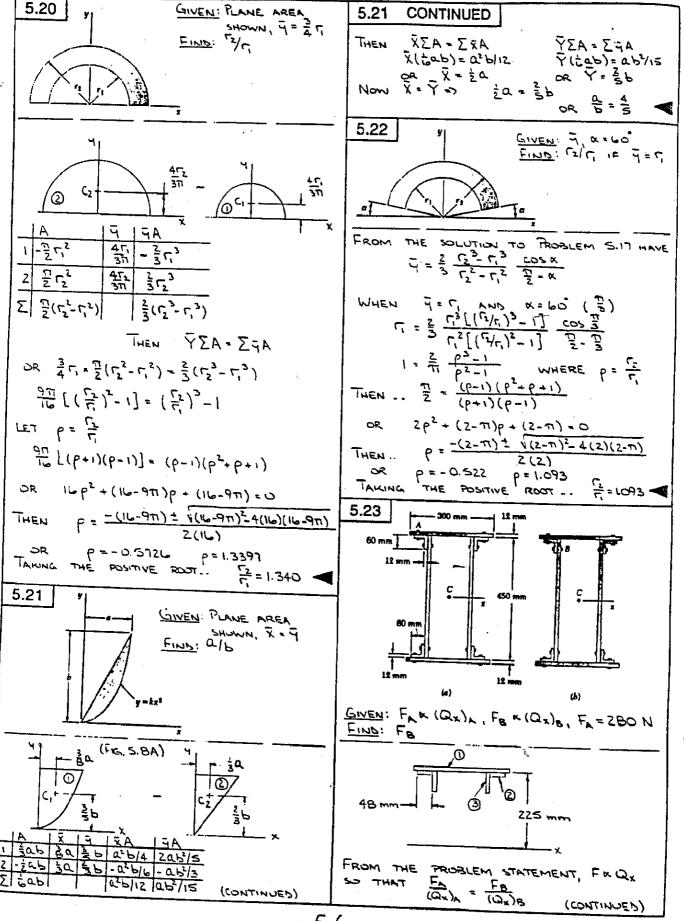


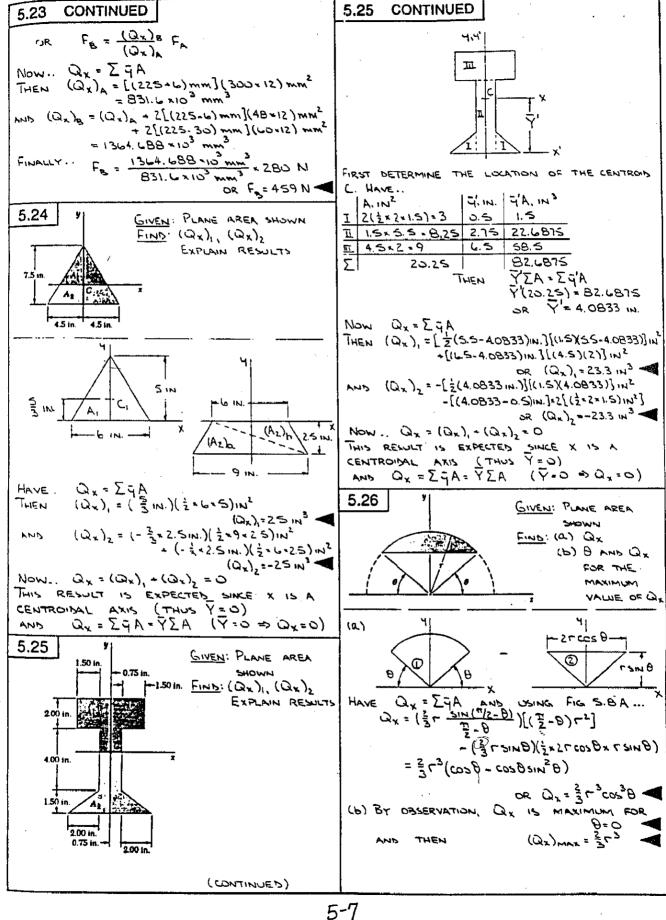
	A	4		
١	₹ bah	34	to baha	
	かり	75	子アング	
Σ	5(p1+p5)p		1 (2b1+b2)h	١.

THEN
$$\overline{Y} \sum A = \sum \overline{c_1} A$$

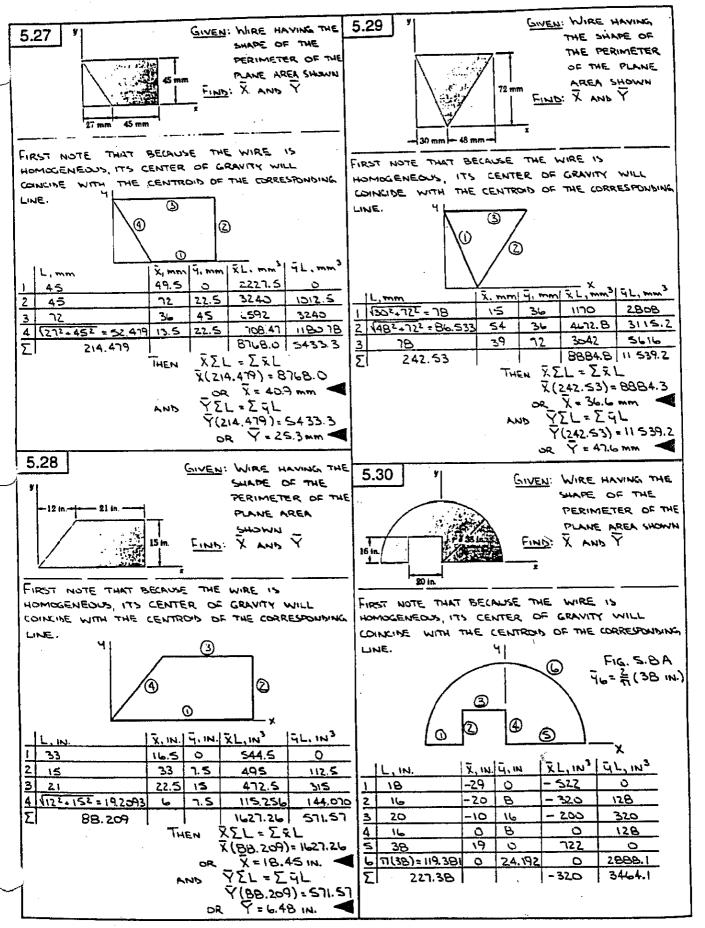
 $\overline{Y} \left[\frac{1}{2} (b_1 + b_2) h \right] = \frac{1}{6} (2b_1 + b_2) h^2$
OR $\overline{Y} = \frac{2b_1 + b_2}{b_1 + b_2} \frac{h}{3}$

60 mm



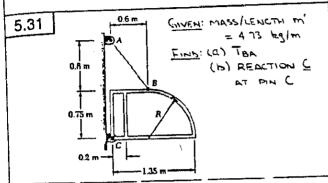


X=18.45 IN. 75L = 5 21

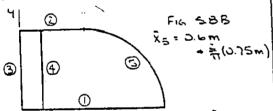


5.30 CONTINUED

THEN $\vec{X} \Sigma L = \Sigma \hat{x} L$ $\vec{X}(227.38) = -320$ $CR \quad \vec{X} = -1.407 \text{ in.}$ $\vec{Y} \Sigma L = \Sigma \vec{y} L$ $\vec{Y}(227.38) = 3464.1$ $CR \quad \vec{Y} = 15.23 \text{ in.}$



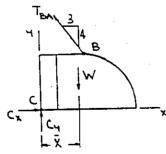
FIRST NOTE THAT BECAME THE FRAME IS
FABRICATED FROM UNIFORM BAR STAK, ITS
CENTER OF CRAVITY WILL COINCIDE WITH THE
CENTROID OF THE CORRESPONDING LINE.



	1	- 1	~L.m3
	L.m	x' w	
ī	1.35	3.675	U.911 25
Z	طاري	D. 3	0 1B
3	J.75	٥	<u> </u>
4	v.15	0.2	0.15
5	3 (3.75) = 1.17B10	1.07746	1,26334
7	4 1-28 10		2 5106

THEN XZL = ZiL X (4.628 10) = 2 5106 OR X = 0 542 47 m

THE EREE-BODY DIAGRAM OF THE FRAME IS



WHERE W = (m' \(\subseteq \subseteq \) = 4.73 \(\subseteq \subseteq \) m = 4.628 10 m = 9.81 \(\subseteq \subseteq \) = 214.75 N

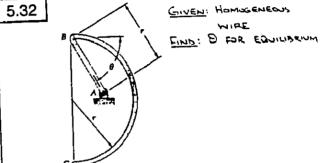
EQUILIBRIUM THEN REQUIRES -. (CONTINUES)

5.31 CONTINUED

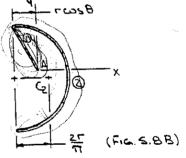
(a) EMc=0: (1.55m)(3TBA) -(0.54247m)(214.75N)=0 OR TBA=125.264N OR TBA=125.3N

(b) $\Sigma F_{x} = 0$: $(v - \frac{3}{5}(125.264 N) = 0)$ or $C_{x} = 75.158 N - \frac{4}{5}(125.264 N) - (214.75 N) = 0$ $\Sigma F_{y} = 0$: $C_{y} + \frac{4}{5}(125.264 N) - (214.75 N) = 0$ $\overline{C}_{y} = 114.539 N$ $\overline{C}_{z} = 137.0 N \Delta 567$

THEN .. = 137.0 N \$ 56.1

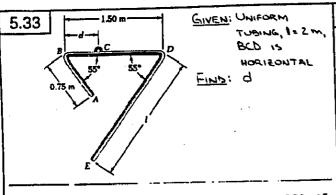


FIRST NOTE THAT FOR EQULIBRIUM, THE CENTER OF GRANTY OF THE WIRE MUST LIE ON A HERTICAL LINE THROUGH A. FURTHER, BECAUSE THE WIRE IS HOMOGENEOUS, ITS CENTER OF GRANTY WILL CONCIDE WITH THE CENTRON OF THE CORRESPONDING LINE. THUS,

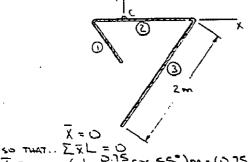


OR 8 = 56.7°

SO THAT $\Sigma \overline{L} = 0$ THEN .. $(-\frac{1}{2}r\cos\theta)(r) + (\frac{2\pi}{\pi} - r\cos\theta)(\pi r) = 0$ OR $\cos\theta = \frac{4}{1 + 2\pi}$ = 0.54921



FIRST NOTE THAT FOR EQUILIBRIUM, THE CENTER OF GRAVITY OF THE COMPONENT MUST LIE ON A VERTICAL LINE THROUGH C. FURTHER BECAUSE THE TUBUS IS UNIFORM, THE CENTER OF GRAVITY OF THE COMPONENT WILL CONCIDE WITH THE CENTRAL OF THE CORRESPONDING UNE. THUS,



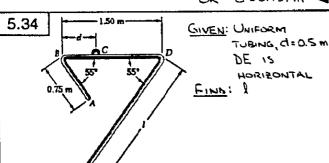
THEN - - (d-0,75 cos 55") m = (0.75 m)

+ (075-d)m=(1.5m)

+ [(1.5-d)m-(2+2m+cos55)]x(2m)

UR (0.75+1.5+2)d = [= (0.75) - 2] cos 55 + (0.75)(1.5) + 3

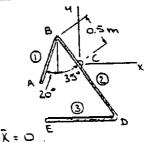
OR d=0.739 m



FIRST NOTE THAT FOR EQUILIBRIUM, THE CENTER OF CRAVITY OF THE COMPONENT MUST LIE ON A VERTICAL LINE THROUGH C. FURTHER, BECAUSE THE TUBING IS UNIFORM, THE CENTER OF GRAVITY OF THE COMPONENT WILL COINCIDE WITH THE CENTROID OF THE CURRESPONDING LINE. THUS.

(CONTINUED)





SO THAT [X X L = 0]

OR - (2 SIN 20 - 0.5 SIN 35) m. (0.75 m) + (0.25 m = 514 35°) = (1.5 m) + (1.0 < 514 35° - 12) m = (1 m) = 0

- 0.096193 + (51035- 12)1 = 0 (XL)DE (XL) + (XL)BO

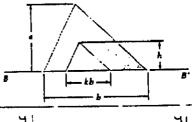
THIS ECULATION IMPLIES THAT THE CENTER OF GRAVITY OF DE MUST BE TO THE RIGHT OF C

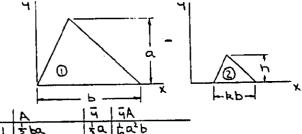
12-1147151+ 0.1923B6 = 0 D = 1.14715 + V(-1.14715)2-4(0.192386)

1=0.204 m AND 1=0.943 m SIN 35° - 10 FOR BOTH VALUES SO BOTH VALUES ARE ACCEPTABLE

5.35 and 5.36

GIVEN: PLANE AREA NWOHE





1 200 3h-686h 2 - F(KP)H 1 (a2-kh2)

THEN YZA-ZAA Y[= (a-kh)] = = (a2-kh2) or $\overline{Y} = \frac{\Omega^2 - kh^2}{3(\alpha - kh)}$

AND $\frac{d\overline{Y}}{dh} = \frac{1}{3} \frac{-2kh(a-kh)-(a^2-kh^2)(-k)}{(a-kh)^2} = 0$

(b) k = 0.80

2h(a-kh)-a2+kh2=0 FIND: h SO THAT Y IS MAXIMUM

(a) k = 0.10

(CONTINUED)

5-10

5.35

1.CTE وعنده (4.)

(0)

<u>5.36</u>

745

E 44

5.3

5.35 and 5.36 CONTINUED

SIMPLIFYING EQ (2) YIELDS - the 2 2 ah + a2 = 0

THEN h = = = 1(-2a)2-4(k)(a2)

= = [1 + (1-R)

NOTE THAT ONLY THE NEGATIVE ROOT IS ACCEPTABLE SINCE TYOU. THEN.

h: 0.10 [1- 11-0.10]

or h=0.513a ◀

(b) k = 0.80

h= 080 [1- VI-080]

DR H= D. 691a

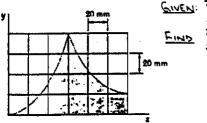
5.36 Show: Y=3h FOR THE VALUE OF h WHICH MAXIMIZES Y

REARRANGING EQ. (2) (WHICH DEFINES THE VALUE OF h WHICH MAXIMIZES Y) YIELDS $a^2 - kh^2 = 2h(a-kh)$

THEN SUBSTITUTING INTO EQ. (1) (WHICH DEFINES Y)... $\overline{Y} = \frac{1}{3(\alpha - Rh)} \cdot 2h(\alpha - Rh)$

OR 7 + 3 h

5.37 and 5.38



GIVEN: PLANE AREA

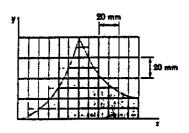
SHOWN

FIND X (5.37) AND

Y (5.38) USING

MEANS

THE AREA IS FIRST DIVISED INTO TWELVE VERTICAL STRIPS, EACH 10 MM WINE, AND THEN THE AREA :AND THE LOCATION OF THE CENTROD ARE APPROXIMATED FOR EACH STRIP. A 10 : 10 - MM GRID IS USED TO FACILITATE APPROXIMATING THE VALUES.



(CONTINUED)

5.37 and 5.38 CONTINUED

57812	A, mm2	Z.mm	4, mm	EA.mm3	44, mm3
1	15	7	\	105	15
2	45	2	3	1040	195
3	150	2.4	٦	3900	1050
4	250	34	14	3000	3500
_ 	400	47	21	18 800	6400
	450	รา	33	37 050	21 450
<u>ك</u> ٢	100	L3	36	44 100	25 200
8	520	74	רצ	38 480	14 040
3	393	83	18	32 370	7020
7	295	94	15	27 730	4425
	240	104	12	24960	c885
12	210	113		23730	5310
Σ	3885	1,1,1	1	261 265	90485

5.37 HAVE .. XXA = ZXA X(3885) = 261 265

OR X-67.2mm

5.38 HAVE . YEA = EAA Y(3885) = 90485 OR Y = 23.3 mm ■

5.39

Silven: Plane Area

Shown,

\$\hat{x} = \hat{So}/106

Find: \$\hat{x} \quad \text{sing}

Approximate

Mean's Based

On Retargles

bcc'b'

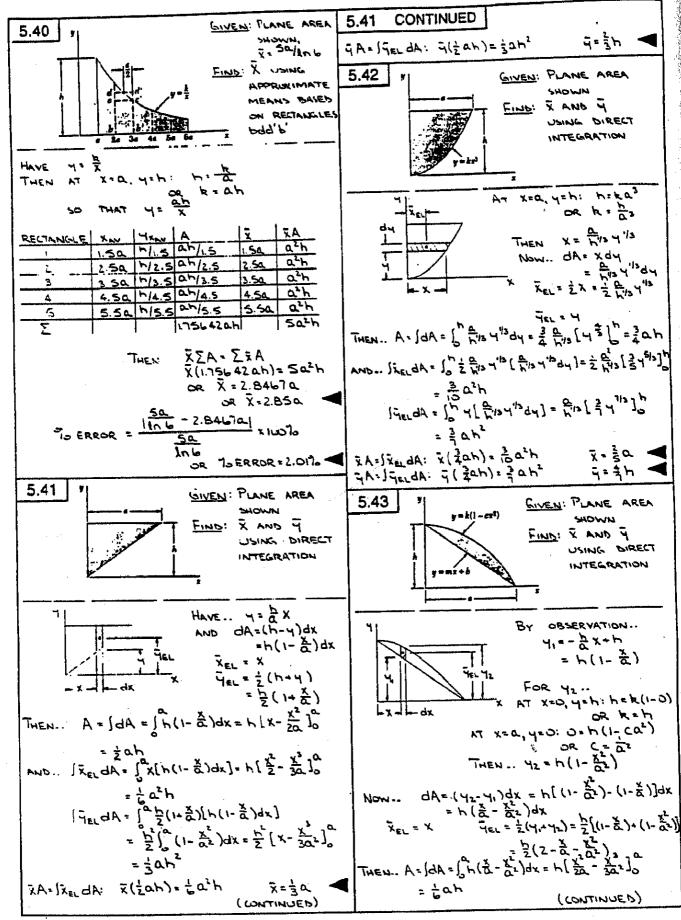
HAVE $Y = \frac{R}{X}$ THEN AT X=Q, Y=h: h=Q SO THAT Y=X

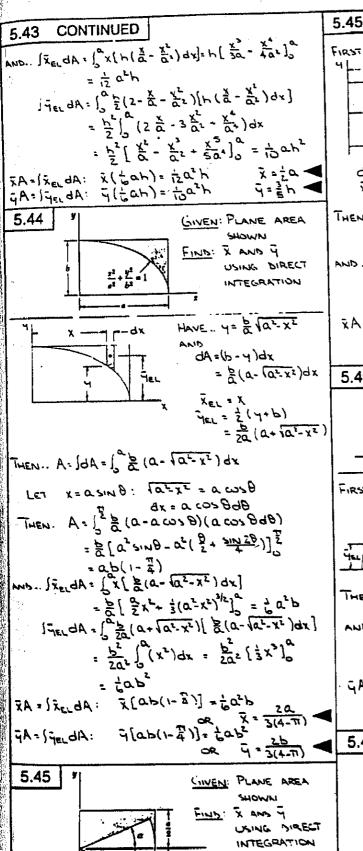
RECTANGLE	1 XX	الادا	IA	<u> </u>	хA
1	2α	n/2	an/2	1.50	0.7502h
7	30	7/3	ah/3	2.50	0.833a2h
3	40.	h/4	0.7/4	3,50	0.875a2h
4	50	nis	ah/s	4.50	3.9a2h_
	La	n/6	anle	5.5Q	0.917a2h
<u> </u>	<u> </u>		1.45ah		4.275 a2h

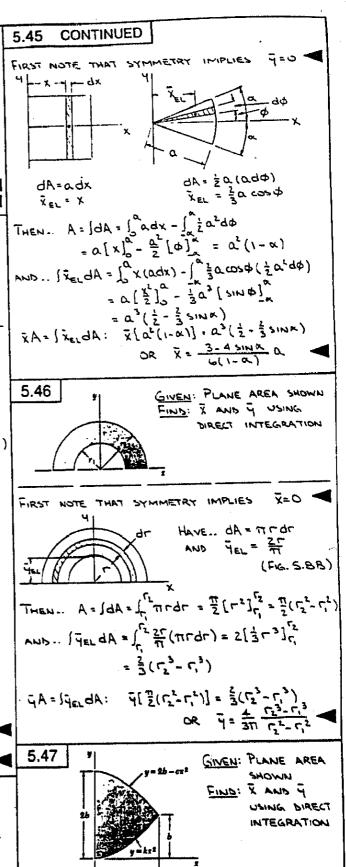
THEN XEA = ERA X(1.45ah) = 4.275a2h CR X = 2.94B3 a CR X = 2.95 a ◀

TO ERROR = \[\frac{150}{100} - 2.94830 \] = 1007.

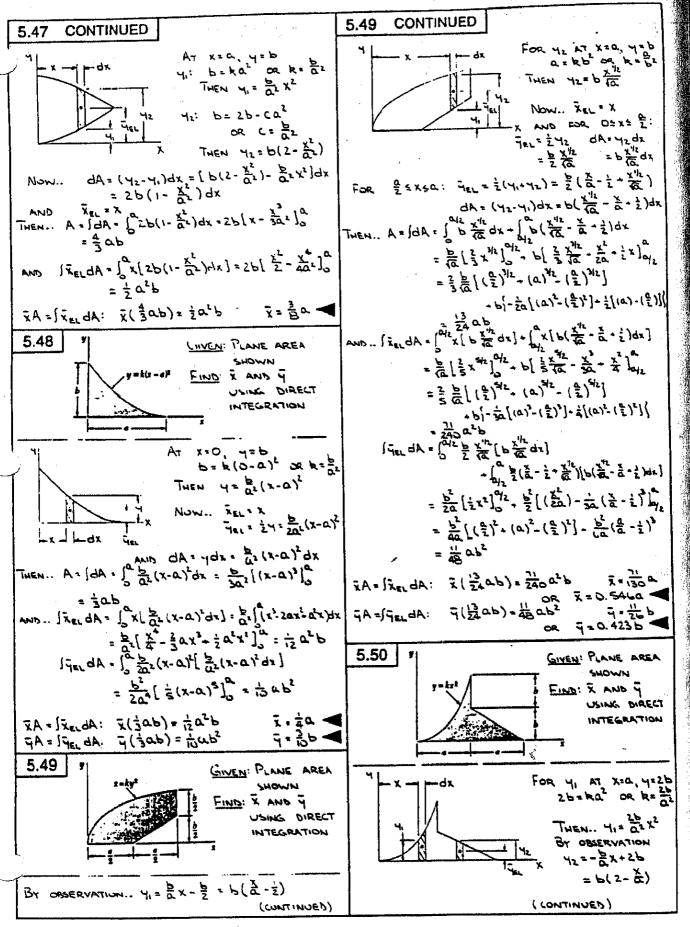
OR % ERROR = 5.65%

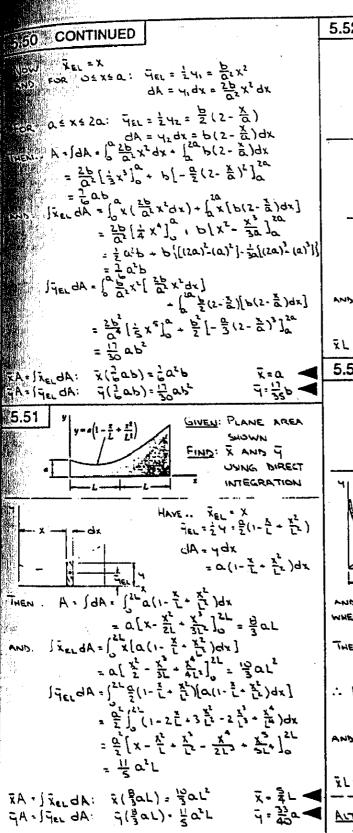


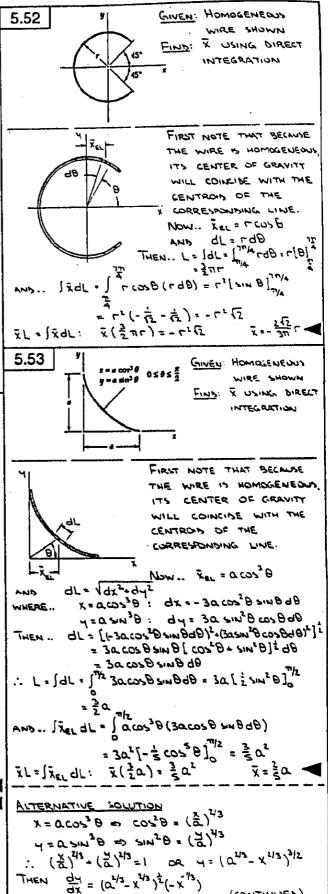




(CONTINUED)

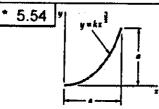




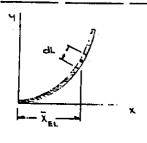


5.53 CONTINUED

Now. $\bar{x}_{E_L} = x$ AND $dL = \sqrt{1 + \left(\frac{d+1}{dx}\right)^2} dx = \left(1 + \left[\left(\alpha^{45} - x^{45}\right)^{16} \left(-x^{45}\right)^3\right]^{16} dx$ THEN.. L = $\int dL = \int_{0}^{\infty} \frac{\chi''_{3}}{\chi''_{3}} dx = \alpha'^{1_{3}} \left(\frac{3}{2}\chi^{2_{1_{3}}}\right)_{0}^{\alpha} = \frac{3}{2}\alpha$ AND .. | Xer dr = | x (x1/2 dx) = 2/3 (3x5/3) = 302 xL = | x = dL x (\frac{3}{2}a) = \frac{3}{5}a^2 \qquad \frac{7}{8}a \frac{2}{5}a \qquad



GIVEN: HOMOGENEOUS WIRE SHOWN FIND: X USING DIRECT INTEGRATION



FIRST NOTE THAT BECAUSE THE WIRE IS HOMOGENEOUS IT'S CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROIS OF THE CORRESPONDING LINE.

HAVE AT X=Q, Y=Q Q=kQ312 OR k= THEN Y= TA X312 AND & = 3 = x 12

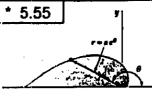
Now.. dL= (1+(3) dx = [1+(3 x12)2]12 dx AND .

= 20 140+9x dx THEN.. L= |dL= | 20 140+9x dx $= \frac{1}{2\sqrt{\alpha}} \left[\frac{1}{3} \times \frac{1}{9} (4\alpha + 9x)^{3/2} \right]_{0}^{\alpha} = \frac{\alpha}{27} \left[(13)^{3/2} - B \right]$

= 1.43971Q AND. JREL dL = Jax[216 (40.49x dx]

Use integration by PART'S WITH U=X du = \$4449xdx 5 = 3 (40+9x)312 du .dx THEN .. | XEL dL = 210 | [x - 27 (40+9x)3/2] $= \frac{\int_{0.27}^{0.27} (4\alpha+9x)^{3/2} dx}{27} \alpha^{2} - \frac{1}{2760} \left[\frac{2}{45} (4\alpha+9x)^{3/2} \right]_{0.27}^{0.27}$ $= \frac{\Omega^2}{27} \left\{ (13)^{3/2} - \frac{2}{45} \left[(13)^{3/2} - 32 \right] \right\}$

* 0.785 46 a2 XL= | XEL dL: X (1.439 71 a) = 0.785 66 a2 or x • 0.546a ◀



GIVEN: PLANE AREA ZHOWN, FIND: X AND Y USING PIRECT

INTEGRATION

HAVE .. \$ = \$ T COS B TEL = \$ 7 510 B AND dh = 2 . T . T dB

THEN .. A = | dA = | 2 02 20 dB . 20 [2 02] $= \pm \alpha^{2} (\alpha^{2n} - 1) = 133.423 \alpha^{2}$

AND | \$\hat{x}_{EL} dA = \int \frac{1}{2} a e cos \theta (\frac{1}{2} a e d\theta) = 303 1 e 30 cos 8 d8

u=e³e^{3θ}dθ du=cosθdθ du=³e^{3θ}dθ u= sinθ Then... ∫e^{3θ}cosθdβ= e^{3θ}sinθ-∫sinθ(3e^{3θ}dθ) Now LET u=e³e du=sinθdθ

- ا(-ص*ه ۱۹۷۵*عد)

SO THAT $10^{30} \cos \theta d\theta = \frac{29}{10} (\sin \theta + 3\cos \theta)$

.. | TrendA = 3 a3 [20 (SNU 8 + 30058] $=\frac{\alpha^3}{30}\left(-3e^{3\pi}-3\right)=-1239.26\alpha^3$

ALSO. I fee dh = 5 3 200 SINB (202028 d8) = 1 03 (" c 30 smB d0

USE INTEGRATION BY PARTS WITH 97 = 1 21M B 98

Then. $\int e^{3\theta} \sin \theta d\theta = e^{3\theta} \cos \theta - \int (-\cos \theta)(3e^{3\theta} d\theta)$ Now LET $u = e^{3\theta} \cos \theta - \int (-\cos \theta)(3e^{3\theta} d\theta)$

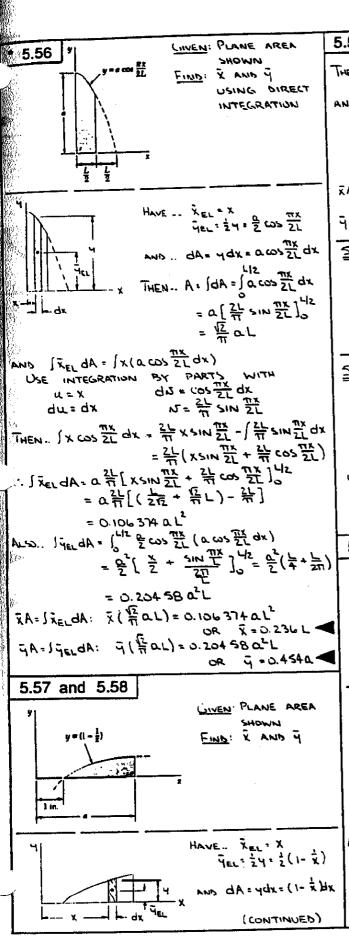
THEN .. 1 & 30 SIN 0 40 8 - 6 30 COS 0 + 3[230 SIN 0 - (Sub) 38 (80) -

(8 mis 6 + 8 cos -) = 868 mis 85

 $\therefore \left| \tilde{\gamma}_{EL} dA = \frac{1}{3} Q^3 \left[\frac{\partial^3 Q}{\partial Q} (-\omega \partial + 3 \sin \theta) \right]_0^{\pi} \right|$ $=\frac{\alpha^3}{30}(e^{30}+1)=413.09e^3$

XA = | XELdA: X(133.623 a2) = - 1239.26 a3 OR X =- 9.27 a

4 + 1 9 eL dA: 4 (133.623 a2) = 413.09 a3 or 4=309a =



CONTINUED 5.57 and 5.58 THEN. A= IdA = \(\big|^{\alpha}(1-\forall)\dx = \big[x-1\timex], = (a - lna - 1) 1N2 = [x - x]a = (= 0 + 2) 1113 I GEL dA = 1 = 1 = = 1 (1 - 1/2)[(1 - 1/2)dx] = 1/2 (1 - 1/2 + 1/2)dx = $\frac{1}{2} \left[x - 2 \ln x - \frac{1}{x} \right]_{1}^{\alpha} = \frac{1}{2} (\alpha - 2 \ln \alpha - \frac{1}{\alpha}) \ln^{3}$ XA = | XELdA : X = 2 - a+2 7 1 - 17 = dA: 9 = \frac{a-2lna-\documenta}{2(a-lna-1)} 5.37 FIND: X AND Y WHEN Q. 2 IN. HAVE.. $\bar{X} = \frac{\dot{z}(2)^2 - 2 \cdot \dot{z}}{2 - \ln 2 - 1}$ OR X=1.629 IN $rac{1}{9} = rac{2-2(n2-\frac{1}{2})}{2(2-3n2-1)}$ OR 4 = 0.1853 m 5.58 FIND: a so THAT \$ = 9 THEN .. \(\frac{1}{2}\alpha^2 - a + \frac{1}{2}\) = 9 OR a3 - 11a2 + a + 18a (na + 9 = 0 USING TRIAL AND ERROR OR NUMERICAL METHORS AND IGNORING THE TRIVIAL SOLUTION Q= I IN., FIND .. Q = 1,901 IN. AND Q = 3.74 IN. 5.59 GIVEN: PLANE AREA SHUWN FIND: VOLUME AND SURFACE AREA OF SOUR OBTAINED BY ROTATING THE AREA ABOUT (a) THE X AXIS (b) THE LINE X:72mm FROM THE SOLUTION TO PROBLEM SI HAVE ZXA : 111 172.5 mm A = 2632.5 mm2 ΣqA * 63 787.5 mm3 APPLYING THE THEOREMS OF PAPPUS-GULBINUS HAVE. (A) ROTATION ABOUT THE X AXIS: VOLUME = 271 Y A = 271 (∑ 7 A) = 271 (63 787.5 mm)

OR VOLUME = 401=10 mm AREA : 271 YUNE L = 271 [(June) L

5.59 CONTINUED

AREA = 217 (4262+ 4363+ 4664) = 271 [(22.5)(45) + (45)(72)+(22.5)((272+452)) OR AREA = 34.1 10 mm2 4

(b) ROTATION ABOUT THE LINE X:12 MM: VOLUME = 271(72- XAREA)A = 271(72A- ERA) = 277 (C72 mm X2632.5 mm2) - (111 172.5 mm3))

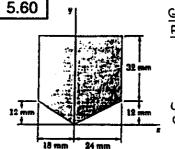
OR VOLUME = 492 1103 mm3

AREA = 271 X LINE L = 271 E(X LINE) L

 $= 2\pi \left(\tilde{X}_1 L_1 + \tilde{X}_2 L_2 + \tilde{X}_4 L_4 \right)$ WHERE $\tilde{X}_1, \tilde{X}_2, \text{ AND } \tilde{X}_4$ ARE MEASURES WITH RESPECT TO THE LINE X: 72 MM. THEN AREA = 27 [(22.5)(45)+(36)(72)

+ (42+15) (515+425)]

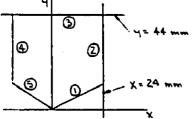
OR AREA = 41.9 = 10 mm2 .



GIVEN: PLME AREA SHOWN FIND: VOLUME AND WREALE AREA OF SOLID OBTAINED BY ROTATING THE AREA rear

(a) THE LINE 42 ++ ++ (b) THE LINE X=24 mm

FROM THE SOLUTION TO PRUBLEM S.S HAVE A = 1536 mm2 Σ x A : 4536 mm E4A = 39 64B mm3



Applying the theorems of Pappus Gulbinus have (a) ROTATION ABOUT THE LINE 4: 44 mm ! VOLUME = 2TI (44- YAREA) A = 2TI (44A - IJA) = 2TI (44 mm) (1596 mm²) - (39 64B mm²)

OR VOLUME = 192.1 × 10 MM

AREA = 2TTY LINE L = 2TT (TILLE) L = 211 (4, 6, 4 7262 + 4464 + 4566)

WHERE $\vec{q}_1,...,\vec{q}_5$ ARE MEASURES WITH RESPECT

TO THE LINE Y = 44 mm. THEN ... AREA = 27 [(38) (242+122)+(16)(32)+(16)(32)

+ (38)((182+122)]

OR AREA = 18.01410 mm

(b) ROTATION ABOUT THE LINE X=24 mm: VOLUME = 271(24 · X)A = 271 (24A · ZXA)

= 277 [(24 mm)(1596 mm²) - (4536 mm³)] OR VOLUME = 212x103 mm3

AREA = 2TI X LINE L = 2TI E (\$ LINE) L

= 271 (x, L, - x 3 L 3 + x 4 L 4 + x 5 L 5)

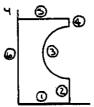
WHERE $\bar{x}_1, \dots, \bar{x}_S$ ARE MEASURES WITH RESPECT (CONITINUED)

5.60 CONTINUED

TO THE LINE X=24 mm. THEN .. AREA = 27 (12) (242-122) + (21)(42) + (42)(52) + (>3)((182+121)) OR AREA = 20.5 4103 mm2

5.61 GIVEN: PLANE AREA MUMM FIND: VOLUME AND SURFACE AREA OF SOUD OBTAINED BY ROTATING THE AREA **NECOST** LAY THE X AWS (b) THE Y AXIS

FROM THE SOLUTION TO PROBLEM 5.7 HAVE A=1146.57 IN2 EXA = 14 147.0 in EqA + 26 897 143



APPLYING THE THEOREMS OF PAPPUS- GULDINUS HAVE ..

(a) ROTATION ABOUT THE X AXIS: $V_{\text{NORTH}} = V_{\text{NORTH}} = V_{$ OR VOLUME = ICA O KID IN

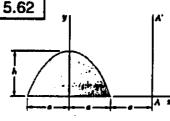
AREA = 277 Y LINE A = 271 E (GUNE)A = 271 (72 Lz + 73 Lz + 94 L4 + 96 L6 + 96 L6) = 271[(7.5)(15)+(30)(71=15)+(47.5)(5)

+ (50)(30)+(25)(50)] OR AREA - 28.4 MID. IN

(b) RUTATION ABOUT THE Y AXIS: VOLUME = 271 XAREA A = 271 EXA = 271 (14 147.0 IN3) OR VOLUME = BB.9 = 10 11 -

AREA = 271 XLINE L = 271 [KLINE)L = 27 (X, L, + X2 L2 + X2 L3 + X4 L4 + X & L5) = 27 [(15)(30)+(30)(15)+(30-2015)(11-15) +(30)(5)+(15)(30)]

OR AREA = 154BAID IN2 4



A. GIVEN: PLANE PARABOLIC AREA SHOWN FIND: YOWME OF SOLID OBTAINED BY ROTATING THE AREA ABOUT (a) THE X AXIS (b) THE LINE AA'

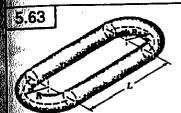
FIRST, FROM FIG. S. BA HAVE .. A= 3ah 4 = { h APPLYING THE SECOND THEOREM OF PAPPUS-GULDINUS HAVE .. (a) ROTATION ABOUT THE X AXIS: (CONTINUED)

5-18

5.62 CONTINUED

VOLUME : 277 A = 27 (= h) (= ah)

(6) ROTATION ABOUT THE LINE AA':
VOLUME - 2TI(ZQ)A = ZTI(ZQ)(3ah)
OR VOLUME = 14TIQZh



AREA

(<u>siven</u>: d=6 mm, R=10 mm, L=30 mm Find: Volume V and Surface area As Of the link

DASERVING THAT THE SEMICIRCULAR ENDS OF THE LINK CAN BE OBTAINED BY ROTATING THE CROSS SECTION THROUGH A HORIZONTAL SEMICIRCULAR ARC OF RADIUS R. THEN, APPLYING THE THEOREMS OF PAPPUS GULDINUS LIAVE

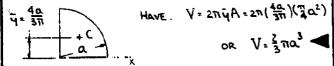
VOLUME: V = 2(VSIDE) + 2(VEND) = 2(AL) + 2(TRA) = 2(L+TR)A = 2[(30 mm)+T(10 mm)][7(6 mm)] OR V=3470 mm

> As = 2(AsibE) + 2(Asub) = 2(CL) + 2(TRC) = 2(L+TR)C = 2[(30 mm)+n(10mm)]T(6 mm)] OR A= 2320 mm²

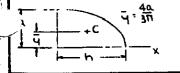
5.64 GIVEN: FIRST FOUR SHAPES OF FIG. 5.21
FIND: VOLUME OF EACH SHAPE

FOLLOWING THE SECOND THEOREM OF PAPPUS. GULDINUS, IN EACH CASE A SPECIFIC GENERATING AREA A WILL BE ROTATED ABOUT THE X AXIS TO PRODUCE THE GIVEN SHAPE. VALUES OF YORKE FROM Fig. 5.8 A.

(1) HEMISPHERE: THE GENERATING AREA IS A GUARTER CIRCLE



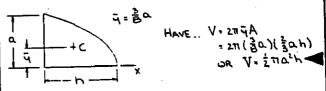
(2) SEMIFILIPSOID OF REVOLUTION: THE CENERATING AREA IS A QUARTER ELLIPSE



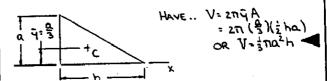
HAVE.. V= 2719A = 271(\frac{40}{371})(\frac{7}{2} ha) OR V=\frac{7}{37102}h

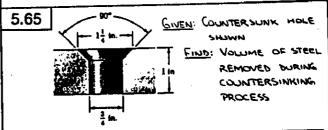
5.64 CONTINUED

(3) PARABOLOID OF REVOLUTION: THE GENERATING AREA IS A GUARTER PARABOLA

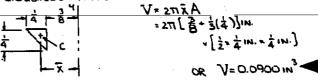


(4) CONE : THE GENERATING AREA IS A TRIANGLE

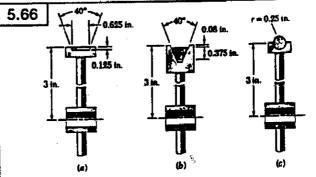




THE REDURED VOLUME CAN BE GENERATED BY ROTATING THE AREA SHOWN ABOUT THE Y AXIS. APPLYING THE SECOND THEOREM OF PAPPUS-GULDINUS HAVE...



ALL DIMENSIONS ARE IN INCHES



GIVEN: THREE DRIVE BELT PROFILES, EACH BELT CONTACTS ONE-HALF OF THE CIRCUMFERANCE OF ITS PULLEY FIND: CONTACT AREA BETWEEN EACH BELT AND ITS PULLEY

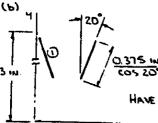
APPLYING THE FIRST THEOREM OF PAPPUS-GULDINUS, THE CONTACT AREA AC OF A BELT (CONTINUED)

5.66 CONTINUED IS GIVEN BY_ Ac= TYL + TEAL (Q)

WHERE THE INSINIONAL LENGTHS ARE THE LENGTHS OF THE BELT CROSS SECTION WHICH ARE IN CONTACT WITH THE PULLEY.

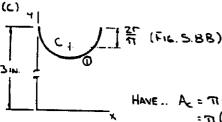
> HAVE .. Ac = TI [2 (], L,) +] 2 L2] = 7 [2(3- 2125)(2125) +(3-0.125)(0.625)]

A = 8.10 102



HAVE .. A = TI[2(4, L,)] $= 5U(3-0.08-\frac{2}{0.312})$ (cos 20.)

Ac= 6.85 IN2



HAVE .. A = T (J, L,) = T (3 - 2x0.25) * (71 - 0.25)

CR A = 7.01 IN2 €





GIVEN: BOWL SHOWN, K = 250 mm FIND: VOLUME V IN LITERS

THE VOLUME CAN BE GENERATED BY ROTATING THE TRIANGLE AND CIRCULAR SECTOR SHOWN ABOUT THE 9 AKIST APPLYING THE LECONS - THEOREM OF PARTYS-GULDINUS AND USING 3 FIG. 5.BA, HAVE.. 0 (CONTINUES)

5.67 CONTINUED

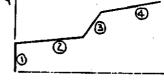
 $V = 2\pi \overline{\lambda} A = 2\pi \Sigma \overline{\lambda} A = 2\pi (\overline{\lambda}_1 A_1 + \overline{\lambda}_2 A_2)$ $= 2\pi \left[\left(\frac{1}{3} * \frac{1}{2} R \right) \left(\frac{1}{2} * \frac{1}{2} R * \frac{13}{2} R \right) + \left(\frac{2R \times 100 \, \frac{30}{20}}{3} \cos_3 30^{\circ} \right) \left(\frac{\pi}{10} R^2 \right) \right]$ $= 2\pi \left(\frac{R^3}{10 \cdot 10} + \frac{R^3}{2 \cdot 10} \right) = \frac{3\sqrt{3}}{8} \pi R^3$ = $\frac{36}{8}\pi (0.25 \text{ m})^3 = 0.031883 \text{ m}^3 \cdot \frac{10^3}{1 \text{ m}}$ OR V=3198 4

5.68

GIVEN: LAMP SHADE SHOWN, DENSITY P . 2800 2 . THICKNESS & = 1 mm

FIND MASS M

THE MASS OF THE SHADE IS GIVEN BY m=pV-pAt WHERE A IS THE SURFACE AREA OF THE SHADE. THIS AREA CAN BE GENERATED BY ROTATING THE LINE SHOWN ABOUT THE X AXIS. APPLYING THE FIRST THEOREM OF



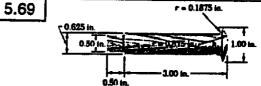
PAPPUS-GULBING

 $A = 2\pi \sqrt{\frac{2}{L}} + 2\pi \sqrt{\frac{2}{3}L} + 2\pi (\sqrt{\frac{2}{3}L_1 + \sqrt{2}L_2 + \sqrt{2}L_3 + \sqrt{2}L_4})$ $= 2\pi \left[(\frac{2}{12})(13) + (\frac{2}{12} + \frac{2}{12})(\sqrt{\frac{2}{3}L_2 + \frac{2}{3}L_3}) \right]$ $+(\frac{16+28}{2})(\frac{8^{2}+12^{2}}{2})+(\frac{28+53}{2})(\frac{28^{2}+5^{2}}{2})$

= 271 (1735.33 mm2)

THEN .. M = 2800 2 "[27 (1735.33mm2)] = 1 mm = 100

OR m = 0.0305 Eg €

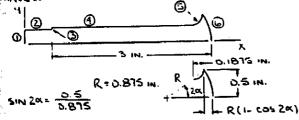


GIVEN: 20,000 PEGS HAVING SHAPE SHOWN, 2 COATS OF PAINT, I GALLON PAINT / 100 HZ FIND: NUMBER OF GALLONS NEEDED

THE NUMBER OF GALLONS OF PAINT NEEDED IS GIVEN BY NUMBER OF GALLOUS " (NUMBER OF PEGS) (SURFACE AREA OF 1 PEG/ 100 (E) (2 CONTS)

5.69 CONTINUED

OR NUMBER OF GALLONS + 400 As (As - \$t^2)
WHERE As IS THE SURFACE AREA OF ONE PEC.
As CAN BE GENERATED BY ROTATING THE LINE
SHOWN ABOUT THE X AXIS. USING THE EIRST
THEOREM OF PAPPUS - GULDINU'S AND FIG. 5.88,
NAVE --

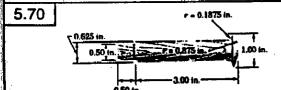


9	As = 27 YL = 27 Eq	L	
4	L, IN	9. IN.	4L, 12
<u>.</u>	0.25	0.125	0.03125
,	0.5	0.25	0.125
 .	J.0625	521820 = 038152	0.01757B1
14	3-0.875(1-cos34.850) -0.1875 = 2.656	0.3125	o. 829 88
\ n \.	12 - 0.1875 - 2.294 52	3.5 - <u>2~0.1815</u> - 0.380 63	CO1 511.0
ی	Za(0.875)	0.875 3IN 17.425	3.137314
	<u> </u>		

ZqL=1.25312 m² THEN.. As = 271 (1.25312 IN²)= 144 IN2 = 0.054678 ft²

FINALLY. NUMBER OF GALLONS 4000 0.054678 = 21.87 GALLONS

ORDER 22 GALLONS



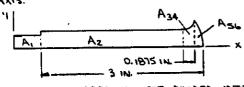
GIVEN: PEG HAVING THE SHAPE SHOWN, INITIAL

SIZE OF DOWEL .. I IN. DIA. * 4 IN. LONG

FIND: PERCENT (VOLUME) OF DOWEL THAT

BECOMES WASTE

TO CIBTAIN THE SOLUTION IT IS FIRST NECESSARY TO DETERMINE THE VOLUME OF THE PEG. THAT VOLUME CAN BE GENERATED BY ROTATING THE AREA SHOWN ABOUT THE X AXIS.



THE GENERATING AREA IS NEXT DIVIDED INTO SIX

5.70 CONTINUED

OR $2N=34.850^{\circ}$ $N=17.425^{\circ}$ | PPLYING THE SECOND THEOREM OF PAPPUS-GULDINUS AND THEN USING FIG. 5.8A, HAVE... $V_{--}=2\pi\ YA=2\pi\Sigma \Delta$

9, IN.	44.123
0.125	0.05 <u>-25</u>
0.15625	0.09667
0.25	0.013438
-0.42042	-0.011 - 03
2 = 0.875 3HN 17.425	o.04005
3 (0.5)	-0.029920
	0.125 0.15625 0.25 0.5- 4 = 0.1815 = 0.42042 2 = 0.875 3 m 17.425 3 (0.5)

EqL = 0.167 252 in 3
THEN .. VACC = 271 (0.167252 in 3) = 1.05088 in 3

Now .. VDOWEL = \$\frac{7}{4} (BIAMETER)^2 (LENGTH) = \$\frac{7}{4}(1 in.)^2 (4 in.)\$

THEN .. YO WASTE = VMASTE x 100%

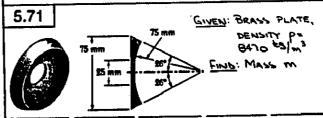
= VMASTE = VMASTE x 100%

- VMASTE = VMASTE x 100%

VMASTE x 100%

- (1- 1.05088) x 100%

OR TO WASTE . LL. 5%



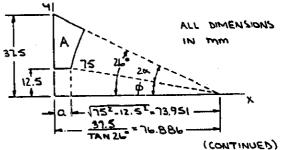
THE MASS OF THE ESCUTCHEON IS GIVEN BY

M = PV

WHERE V IS THE VOLUME OF THE PLATE. V CAN

BE GENERATED BY ROTATING THE AREA A

ABOUT THE X AXIS.

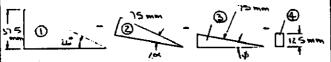


5.71 CONTINUED

HAVE.. $\alpha = 76.886 - 73.951 = 2.935 \text{ mm}$ AND.. $\sin \phi = \frac{12.5}{2.5} \implies \phi = 9.5941$

THEN 2x = 26 - 9.5941 = 16.4059

THE AREA A CAN BE OSTAINED BY COMBINED THE FOLLOWING FOUR AREAS AS INDICATED.



Applying the second theorem of Papeus-Guldinus and then using Fig. 5.8A, have .. $V : 2\pi \ YA : 2\pi \ \Sigma \ A$

	A. mm2	14 = 211 24 M 4, mm	9A, mm3
-	₹×76.886×37.5 = 1441.61	±(37,5) + 12.5	E1.050 BI
2	-x(75)2	2(75) SIN B. 203, SIN (B. 203.4954)	-12 245.30
3	- 2 · 13.951 · 12.5 .	3(12.5) +4.1667	- 1925.81
٩	- 2.935 • 12 5 = - 36.688	हु(12.5) = ७.25	- 229.30

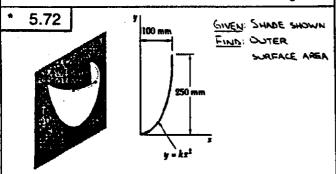
Σ η Α = 3599.72 mm³

THEN , V = 27 (3599.72 mm³) = 22 617.7 mm³

SO THAT M = 8470 m³

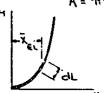
22 17.17 m = 0.1910 m³

OR m= 191.69 4



FIRST NOTE THAT THE REQUIRES SURFACE AREA A CAN BE GENERATED BY ROTATING THE PARABOLK CROSS SECTION THROUGH TI RADIANS ABOUT THE Y AXIS APPLYING THE FIRST THEOREM OF PAPPUS GULDINUS HAVE

A = TIXL



Now. AT x = 100 mm, y = 250 mm
250 = k(100)2

CR k = 0.025 mm

WHERE $\frac{dy}{dt} = 2kx$

THEN . $dL = \sqrt{1+4k^2x^2} dx$ HAVE.. $\bar{x}L = \sqrt{x_{EL}} dL = \sqrt{x_{EL}} \sqrt{(1+4k^2x^2)} dx$

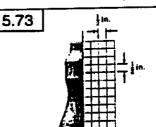
5.72 CONTINUED

 $\overline{\chi} = \left[\frac{1}{3} \frac{1}{4 \pi^2} \left(1 + 4 \pi^2 \chi^2 \right)^{3/2} \right]_0^{100}$ $= \frac{1}{12} \frac{1}{(0.025)^2} \left\{ \left(1 + 4(0.025)^2 (100)^2 \right)^{3/2} - (1)^{9/2} \right\}$

= 17 543.3 mm²

FINALLY ... A = TY (17 543.3 mm2)

OR A = 55.1x10 mm



 G_{IVEN} : BOTTLE OF CROSS SECTION SHOWN, W= 0.131 1b, SPECIFIC WEIGHT Y=59.0 1b/ ξ_L^3

FIND: AVERAGE WALL

THE WEIGHT OF THE BOTTLE IS GIVEN BY

W = 8 V = 8 Ast.

WHERE As IS THE SURFACE AREA OF THE
BOTTLE As CAN BE GENERATED BY ROTATING

THE CURVE BOWNING THE CROSS SECTION ABOUT

THE VERTICAL AXIS OF SYMMETRY.

APPROXIMATING THE PORTION OF THIS CURVE

TO THE RIGHT OF THE VERTICAL AXIS WITH A

SERIES OF SHORT, STRAIGHT LINE SEGMENTS

AND THEN APPROXIMATING THE LENGTH AND

THE VALUE OF X FOR EACH SEGMENT

USING THE GIVEN GRID, AS IS THEN

DETERMINED USING THE FIRST THEOREM OF

PAPPUS - GULDINUS.

As = 27 XL = 27 ExL

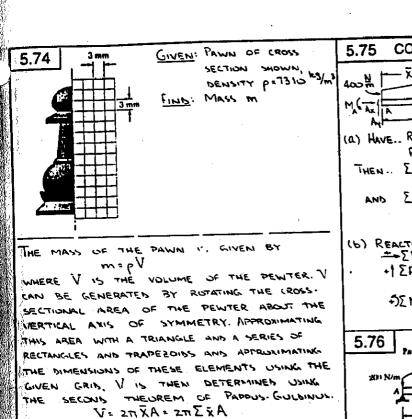
WITH THE ELEVEN SEGMENTS NUMBERED STARTING AT THE TOP, HAVE ..

| L, IN. X, IN. XL, IN. 1 0.76 0.38 0.2888

1		L, IN.	X, 1N.	KL, IN'
ì	$\overline{\Delta}$	0.76	D.18	0.28BB
ار	2	o.48	م ر	0.3448
	3	ა.98	3.98	J. 8624
1	4	į	1.20	1.272
7	5	ა.36	1.08	<u>6</u> 888.c
	L	1.12	99.0	1.0976
	٦	I.7B	1.32	2.3496
+	В	2.50	بر د د	4.15
7	9	1.12	1.74	1.9488_
×	10	S.48	1.48	0.8064
	П	1.56	อเาย	1.2168
	5			14.7440

THEN .. As = 2TI (14.7460 IN2) = 92.652 IN2

FINALLY.. 0.131 16 = 59.0 H3 = 92.652 IN2 (12 in) t OR t=0.0414 IN.



WITH THE AREAS TAKEN STARTING AT THE

A, mm2

1 3 -3 -1.5 -2 25 1-52(3+39)=105

4 3 6-1 2 : 4 32

7 5 25 4 1.2 4 3

9 315 - 0.9 - 2.84

12 2.25 . 2.85 . 6.41

15 125 (3+1.95): 3.34

435.1.20 = 5.22

THEN .. V = 27 (453.12 mm2) = 2847 = mm2

14 3 . 1.5 . 4.5

(b) REACTIONS AT A

3 1-8 (3.9+3.6)=675

ح ا انتي⁵ (ع ب - ۲.25) و ط 23

8 990 (1.35.2.56)= 19.31

2-25(2.25+515)18 44

10 315 (315+585): 14.18 3 B

275 (165-2.15)1 1 46

1.05 (5 1501 105) 1 2 0 5

2 (1.95 + 435): 5.51 7 35

104.33

K.mm KA.mm3

175

3.5

3 1

₩.つ

<u>ر با</u>

7 7

695

(CONTINUED)

2 25

6, 34

2295

14 26

14 49

<u> د د د د</u>

25.83

48.28

P 89

23 88

978

45 59

13.74 32 40

-321

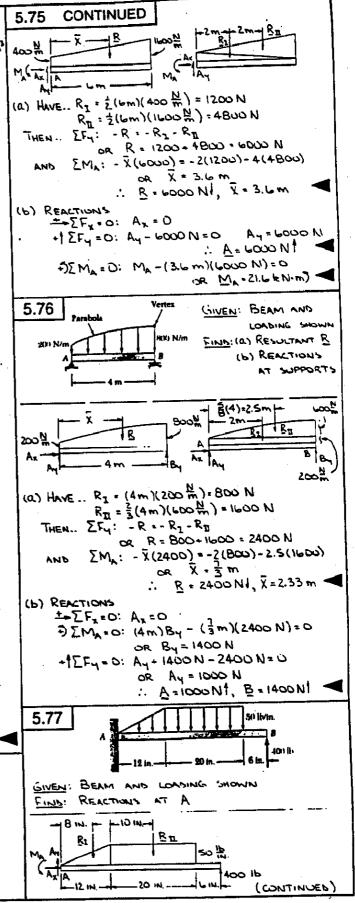
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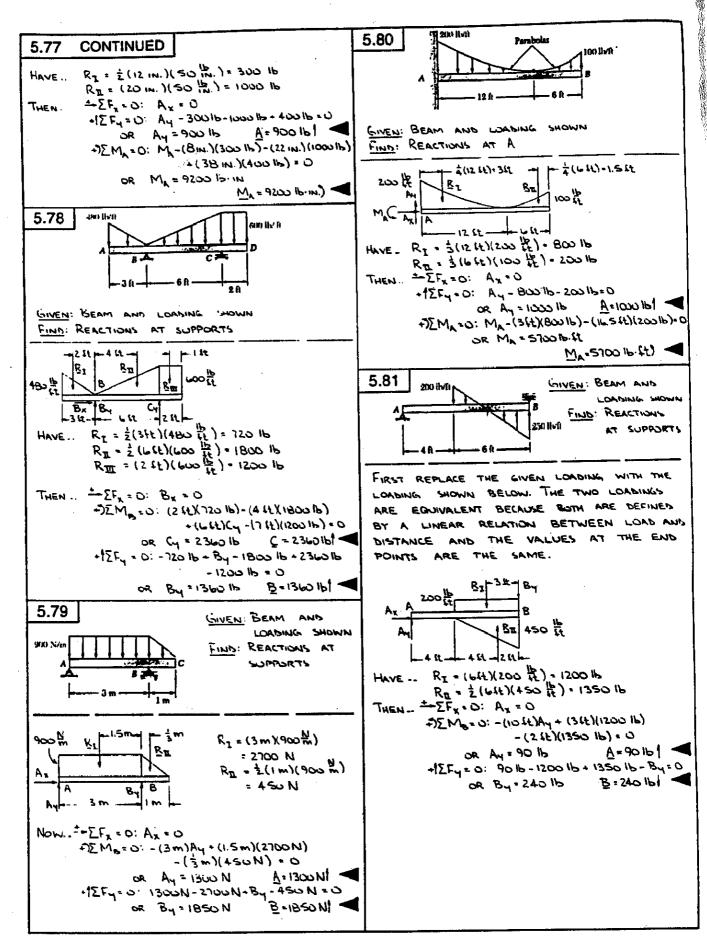
ALZA

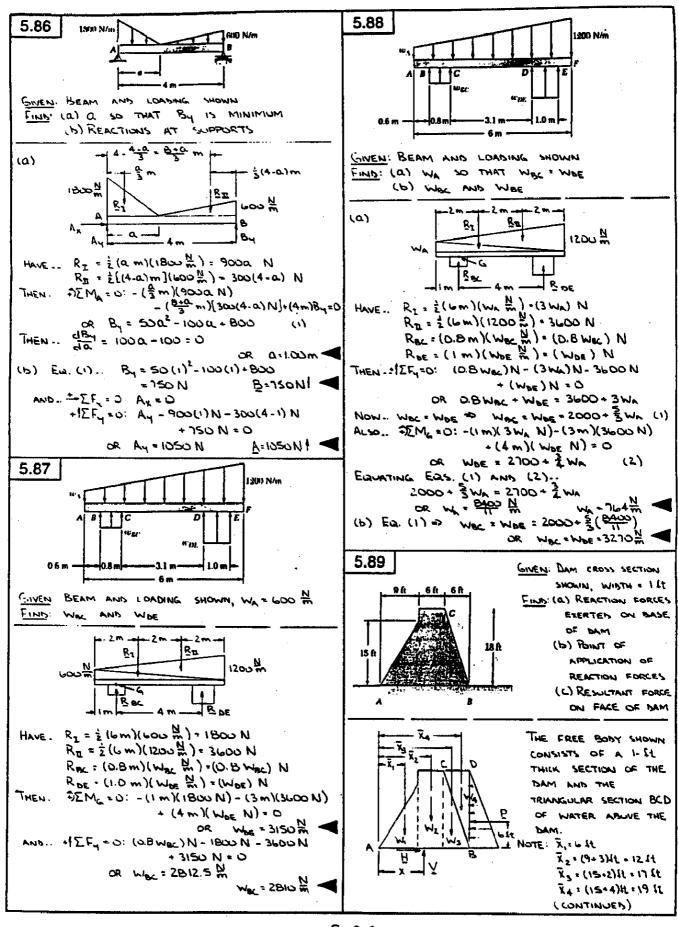
453.12

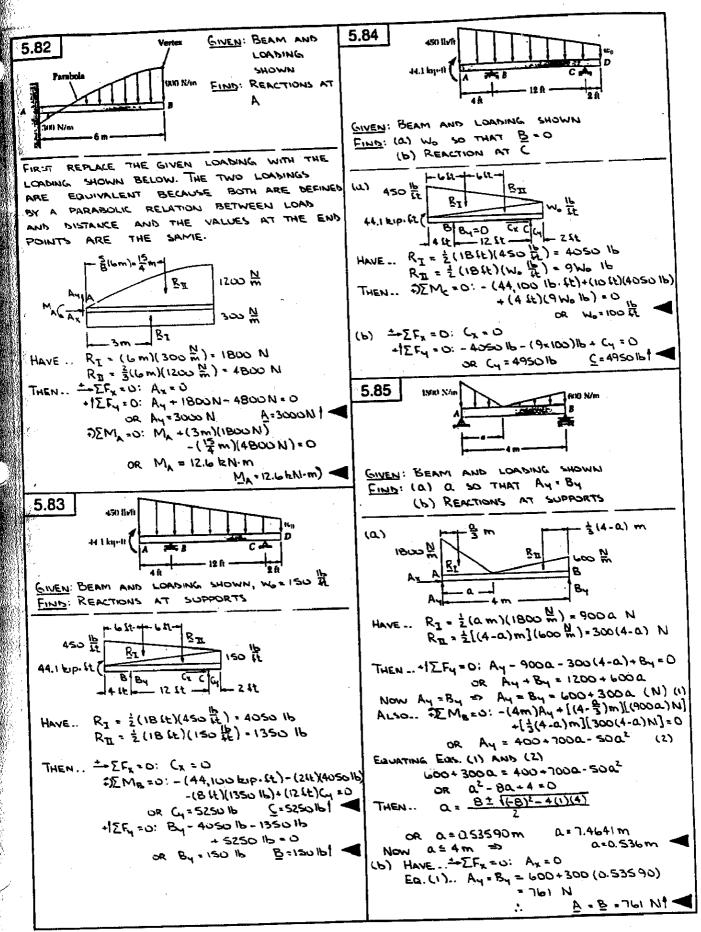
TOP HAVE --

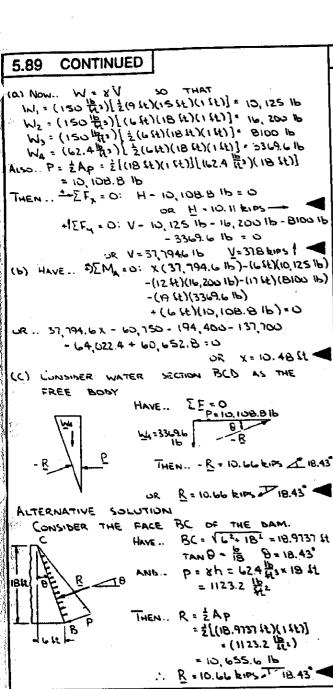
5.75

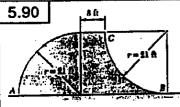












GIVEN: DAM CROSS
SECTION SHOWN,
WINTH = 1 St
FIND: (Q) REACTION
FORCES EXERTED
ON BASE OF
DAM

(b) POINT OF APPLICATION
OF REACTION FORCES
(C) RESULTANT FORCE ON

FACE OF DAM

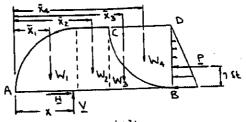
THE FREE BONY SHOWN (TOP OF NEXT COLUMN)

CONSISTS OF A 1- LY THICK SECTION OF THE

DAM AND THE GUARTER CIRCULAR SECTION OF WATER

ABOVE THE DAM. (CONTINUED)

5.90 CONTINUED



NOTE: $\bar{X}_1 = (21 - \frac{4 + 21}{377}) \text{ ft} + 12.0873 \text{ ft}$ $\bar{X}_2 = (21 + 4) \text{ ft} + 25 \text{ ft}$ $\bar{X}_4 = (50 - \frac{4 + 21}{377}) \text{ ft} + 41.087 \text{ ft}$

FOR AREA 3 FIRST NOTE ..

THEN .. $\bar{\lambda}_{3} = 29 LL + \left[\frac{\frac{1}{2}(21)(21)^{2} + (21 - \frac{4 \times 21}{377})(-\frac{7}{4} + 21^{2})}{(21)^{2} - \frac{7}{4}(21)^{2}} \right] H$

= (29 + 4.6907) \$2 . 33.691 \$2

(a) Now.. W = 8V 30 THAT $W_1 = (150 \frac{1}{12}) \left[\frac{2}{4} (2116)^2 (161) - 51,954 \text{ lb} \right]$ $W_2 = (150 \frac{1}{12}) \left[(866)(2166)(166) - 25,200 \text{ lb} \right]$ $W_3 = (150 \frac{1}{12}) \left[(21^2 - \frac{1}{4} \cdot 21^2) 66^2 \cdot (166) - 14,196 \text{ lb} \right]$ $W_4 = (62.4 \frac{1}{12}) \left[\frac{1}{4} (2166)^2 (166) - 21,613 \text{ lb} \right]$ ALSO $P = \frac{1}{2}AP = \frac{1}{2} \left[(2166)(166) - (166) - 21,613 \text{ lb} \right]$ = (13.759 lb)

THEN .. \$= \$\sum_{x=0}^{\infty} H = 13,759 | \begin{align*}
OR \(\text{H} = 13.76 \) \(\text{kips} -- \)

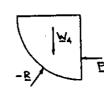
4\(\text{EF}_{y} = 0: \(V = 51,954 \) \(\text{b} - 25,200 \) \(\text{b} - 14,196 \) \(\text{b} \)

- 21,613 16 = 0 OR V=112,96316 Y=113.0 E/B = (6) HAVE .. TEM, = 0: X (112,963 16) - (12.087342)(51,954 16)

- (25 ft)(25,200 lb) - (33.691 ft)(14,196 lb) - (41.087 ft)(21,613 lb) - (7 ft)(13,759 lb) • 0

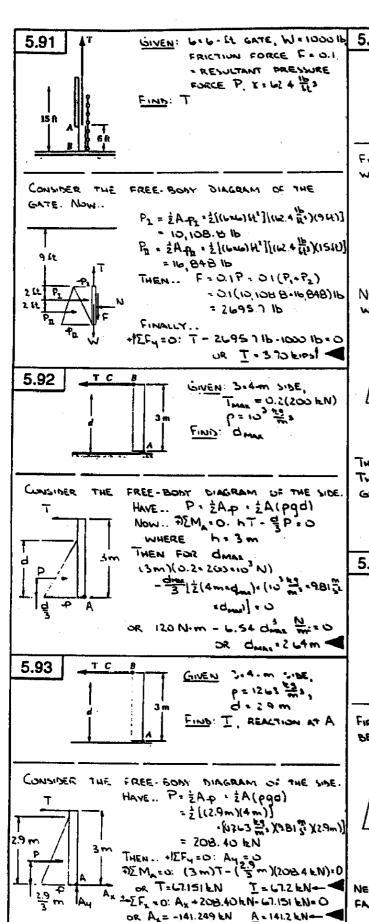
OR 112,963 X - 627,980 - 630,000 - 478,280 - 888,010 + 96,313 = 0 OR X = 22.4 ft €

(C) CONSIDER WATER SECTION BCD AS THE FREE BODY



HAVE .. \(\sum_{\begin{subarray}{c} \begin{subarray}{c} \begin{su

THEN .. + R = 25.6 EIPS 157.5°

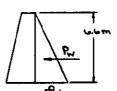




GIVEN: Po = 1.76x10 123 WIDTH'- Im. d= 2 m FIND: PERCENTAGE

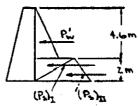
INCREASE OF FORCE ON DAM FACE BECAUSE OF SILT

FIRST DETERMINE THE FORCE ON THE DAM FACE WITHOUT THE SILT. HAVE ..



Pw = 2A-pw = 2A(pgh) = = 2[(6.6 m)(1 m)] ·[(10 3 pm)(9.81 22))(mm m)] = 213. LL KN

NEXT DETERMINE THE FORCE ON THE DAM FACE WITH THE SILT. HAVE ..

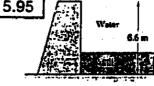


Pn = 2[(4.6m)(1m)] ·[(10) 19 19.81 (4.6m)] = 103.79 EN (B) = 2[(2m)(1m)][(1760) 2] *(3.B1 2)(4.6 m))

= 79.42 KN (b) = = = [(5m)(1m)][(1. Jen 2) = 2 mg · (9.81 th)(6.6m)] =113.95 KN

THEN. P'= P" + (Ps), + (Ps), = 297.16 kN THE PERCENTAGE INCREASE TO INC. IS THEN GIVEN BY .. P'-PW = 100% = (297.16-213.66) = 1000

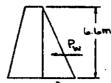
OR % INC. = 39.170



GIVEN: (FBASE) MAX = 1.2% FORCE OF WATER, Parlinerio kgs, WITH = I M. RATE IS AT WHEN SILT IS DEPOSITED = 12 mm/YEAR

FIND: NUMBER OF YEARS IN UNTIL DAM BECOMES UNYAFE

FIRST DETERMINE THE FORCE ON THE DAM FACE BEFORE MY SILT IS DEPOSITED HAVE ..



Pw = 2A+w = 2A(pgh) = { [(6.6m)(1 m)] [(md.d) (2 18.8) (2 2 (cm))]. = 213.66 kN

THE MAXIMUM ALLOWED FORCE PALLOW ON THE DAM IS THEN .. PALOW = 1.2 PW = 1.2 (213.66 kN) = 256.39 kN NEXT DETERMINE THE FORCE P' ON THE DAM FACE AFTER A DEPTH & OF SILT HAS SETTLED. · (CONTINUES)



Pw. = E[(w.b-d)m. (1m)] ·[(10 m))(9.81 32)(6-d)m] (6.6-d)m = 4,905(6.6-d)2 kN ·[(1.)Pain m) (3.81 2) · (6.6-d)m] $(L^2)^T$ $(L^2)^H$ = 8.6328(6.6d-d2) kN (be) # = \$ { (q) m = (1 m)} = (b.b m)]

= 56.976 d kN THEN P' = PW. + (Ps) I + (Ps) II = (4905(6.6-d)2+ B.6328(6.6d-d2) + 56.976d] KN

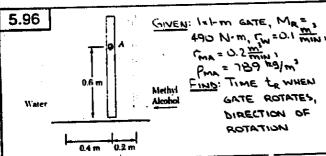
= (213.66 + 49.206d - 3.7278d2) kN

NOW REQUIRE THAT P' PALLOW TO DETERMINE THE MAXIMUM VALUE OF d. : (213.66+49.206d-3.7278de) kN=25639 kN

3.7278 d2 - 49.206d + 42.73 = 0 d = 49.206 = V(-49.206)-4(3.7278)(42.73) HEN .. 2 (3.7278)

d= 0.934 56 m AND d= 12.2652 m 9 = UN Now, deble m AND 0.934 56 m = 12×10 TEAR " N THEN

N = 11.9 YEARS



CONSIDER THE FREE-BODY DIRGRAM OF THE GATE. FIRST NOTE .. V = ABASE d AND Vert dw = 3.1 mm = + (min) THEN (0.4 m)(1 m) = 0.25 t (m)
dm = 0.2 min = t(min) (02m)(1m) = f (w)

Now. P= 2Ap = 2A(pgh) 50 THAT
Pw = 2[(0.25t)m.(1m)][(10) m3 X9.B1 = X0.25t)m] = 306.56 t2 N PML = 2[(+)m= (1m)][(189 m2)(9.81 5)(+)m] = 3870t2 N

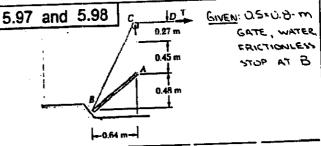
NOW ASSUME THAT THE GATE WILL ROTATE CLUCKWISE AND WHEN CHAS DIG. WHEN (CONTINUED)

CONTINUED 5.96

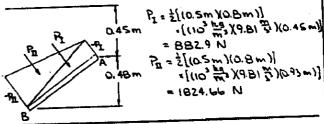
ROTATION OF THE GATE IS IMPENDING, REQUIRE EMA: MR = (0.6m-3dm)PMA-(0.6m-3dw)Pw SUBSTITUTING .. 490 N·m = (0.6-3 t)m = (3870t2) N -(0.6-3-0.25t)m =(306 56t2)N SIMPLIFYING .. 1264.45 t = 2138.1 t2 + 490 = 0 SOLVING (POSITIVE ROOTS ONLY) .. t: 0.594 51 min AND t= 1.524 11 min

NOW CHECK ASSUMPTION USING THE SMALLER ROUT. HAVE ...

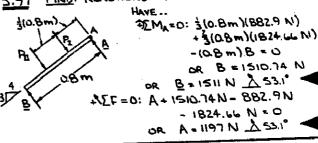
dma =(t)m = 0.59451 m < 0.6 m : t = 0.594 SI min = 35.75 AND THE GATE ROTATES CLICKWISE



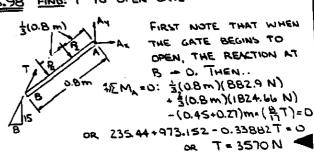
FIRST CONSIDER THE FORCE OF THE WATER ON P= 2Ap = 2A(pgh) so THAT. THE GATE. HAVE



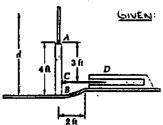
FIND REACTIONS AT A AND B WHEN TO 5.97 \$(0.8m)



5.98 FIND: T TO OPEN GATE

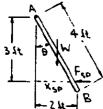






GIVEN: 4 = 2- St GATE, K = BZB TR. SPRING IS UNDEFORMED WHEN GATE IS VERTICAL WATER

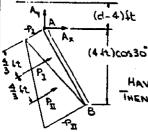
FIRST DETERMINE THE FORCES EXERTES ON THE GATE BY THE SPRING AND THE WATER WHEN B IS AT THE END OF THE CYLINDRICAL PORTION OF THE FLOOR.



SIN 8 = 4 HAVE ... B = 30° X = 13 (t) TAN 30° THEN Fup = Kxyp AND

= BZB 片·341·TAN30 = 1434,14 lb

Assume d= 4 St



HAVE .. P = 2A-P = 2A(Xh)

THEN. Pz = \$ [(4 ft)(2 ft)] ·[(L2.4 造)(d-4)代]

= 249.6(d-4) 1b

Pn = 2[(4 4)(26)] =[(4.4 [2)(d-4+4cos30)]

= 249 6(d-0 53590) 1b

5.99 Fing: d, W=0

Using the above free-body diagrams OF THE GATE, HAVE ..

かEMA = 0: (音化)[249.6(d-4)16]

+(&tt)[249.6(d-0.53590)16]

- (3ft)(1434.14 1b) = 0

OR (332.8 d - 1331.2) + (665.6d - 356.70) - 4302.4 = 0

or d=6.00 st

d ≥ 4 st => ASSUMPTION CORRECT

: 0.6.00 It

5.100 FIND: d. Wallow 16

Using the above free-body biagrams of THE LATE, HAVE... PEMA =0: (316)[249.6 (d-4) 16]

+(= 16)[249.6 (d-0.535 90) 16]

- (3 ft)(1434.14 fb)-(1 ft)(1000 fb) = 0

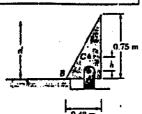
OR (332.8 d-1331.2)+ (665.6d-356.70)-4302.4 - 1000 + 0

OR d = 7.00 ft

d2 4ft & ASSUMPTION CHRECT

:. d=200 lt ◀

5.101 and 5.102



3(0.4 m)

GIVEN: PRISMATICALLY SHAPED GATE.

WATER

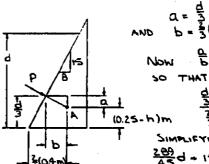
FIRST NOTE THAT WHEN THE GATE IS ABOUT TO OPEN (CLOCHWISE ROTATION IS IMPENDING), By -O AND THE LINE OF ACTION OF THE

RESILTANT P OF THE PRESINCE FORCES PRISES THROUGH THE PIN AT A. IN ABBITION, IF IT

IS ASSUMED THAT 1(0.75m) . J.25m THE GATE IS

HOMOGENEOUS THEN ITS

CENTER OF GRAVITY (COINCIDES WITH THE CENTROID OF THE TRIANGULAR AREA. THEN ...



a = 3 - (0.25-h) AND b= 3(0.4)- 13(3)

Now P = 12

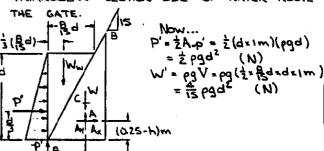
본 - (0.25-ト/)

SIMPLIFYING YIELDS कुर्व + 12 P = 100 P (1)

ALTERNATIVE SOLUTION

--- 3(0.4 m)

COUSIDER A FREE BODY CONSISTING OF A I-M THICK SECTION OF THE GATE AND THE TRIANGULAR SECTION BDE OF WATER ABOVE



THEN WITH By = 0 (AS EXPLAINED ABOVE) HAVE.. DEM = 0: (3(0.4)-3(2d)(3 pgd2)

-[3-(0.25-h)](2 pgd1) =0

SIMPLIFYING YIELDS .. 289 d+ 15h = 10.6 AS ABOVE.

5.101 and 5.102 CONTINUED

5.101 FIND: d, h= 0.10 m

289 d + 15(0.10) = 30.6

OR d=0.683m

5.102 Find: H. d=0.75 m

Substituting into Eq. (1) -- $\frac{269}{45}$ (0.75) + 15 h = $\frac{70.6}{12}$

OR h=0.0711m 4

5.103

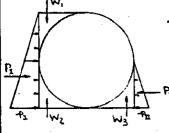
GIVEN: WINTH = 30 IN., WATER

FIND: RESULTANT R OF

PRESSURE FORCES

ACTING ON DRUM

CONSIDER THE ELEMENTS OF WATER SHOWN. THE RESULTANT OF THE WEIGHTS OF WATER ABOVE EACH SECTION OF THE DRUM AND THE RESULTANTS OF THE PRESSURE FORCES ACTING ON THE VERTICAL SURFACES OF THE ELEMENTS IS EQUAL TO THE RESULTANT HYDROSTATIC FORCE



ACTING ON THE DRUM.

THEN.. $P_1 = \frac{1}{2}A_1P_2 = \frac{1}{2}A(xh)$ $= \frac{1}{2}[(\frac{12}{12})H_1(\frac{23}{12})ft]$

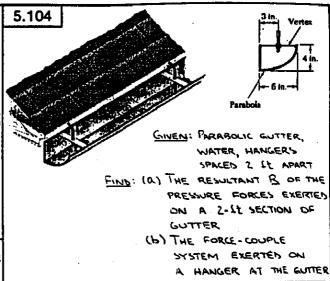
 $W_{1} = 8V_{1} = (L2.4 \frac{16}{12})[(\frac{11.5}{12})^{2}tt^{2} - \frac{7}{4}(\frac{11.5}{12})^{2}tt^{2}](\frac{30}{12}tt)$ = 30.74L Ib $W_{2} = 8V_{2} = (L2.4 \frac{16}{12})[(\frac{11.5}{12})^{2}tt^{2} + \frac{7}{4}(\frac{11.5}{12})^{2}tt^{2}](\frac{30}{12}tt)$ = 255.80 Ib

 $W_3 = 8\sqrt{3} = (-5.4 \frac{16}{12}) \left(\frac{1}{12} \right)^2 H_2 \left(\frac{30}{12} \right)^2$ = 112.525 IP

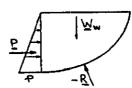
THEN.. \$\frac{1}{2}\sum_{x} : R_{x} = (286.542 - 71.635)16 = 214.91 16
+\$\frac{1}{2}\sum_{y} : R_{y} = (-30.746 + 255.80 + 112.525) 16
= 337.58 16

FINALLY.. R = VRX+RY TAND = RX = 400.18 16 0 = 57.5

.: R = 400 16 157.5° ◀



(a) Consider a 2-12-long parabolic section of water. Then...



P= ½Ap = ½A(8h) = ½[(½4e)(24e](42.4½)(42.4½) = 6.93.33 lb W= 8V =(62.4½)(3(124)(24))

NOW. \(\sum_{e} = 0 : (-\bar{R}) \cdot \bar{P} \cdot \bar{M} \cdot \bar{P} \cdot \bar{M} \cdot \bar{P} \cdot \cdot \bar{P} \cdo

(b) CONSIDER THE FREE-BOSY DIAGRAM OF A

2-11-LONG SECTION OF WATER AND GUTTER.

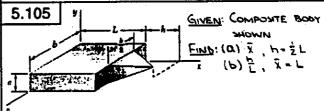
1-3 III - M.

THEN...

 $\frac{+1}{-1}\sum_{k=0}^{+1}F_{k}=0: B_{k}=0$ $+1\sum_{k=0}^{+1}F_{k}=0: B_{k}=13.866716=0$ $CR B_{k}=13.866716$ +13.866716 +13.866716 +13.866716

OR Mo = 8.320 lb·m THE FORCE - COUPLE SYSTEM EXERTED ON THE HANGER IS THEN...

13.87 lb (, 8.32 lb-in.)



	V	x	žVV
RECTANGULAR PRISM	Lab	½ L	± L2ab
PYRAMID	3a(2)h	L+#h	6abh(L+4h)

THEN. $\Sigma V = ab(L+bh)$ $\Sigma \bar{x}V = bab[3L^2 + h(L+bh)]$ (continues)

5.105 CONTINUED

Now. $\bar{X} \sum V \cdot \sum \bar{x} V$ so that $\bar{X} [ab(L+bh)] = bab(3L^2 + bh + bh^2)$ or $\bar{X} [1+bb] = bh (3+b^2 + b^2 + b^2)$ (1)

(a) $\bar{X} = \hat{I}$ WHEN $h = \hat{z}L$ Substituting $\hat{L} = \hat{z}$ into Eq. (1)... $\bar{X}\{1 + \hat{b}(\hat{z})\} = \hat{b}L[3 + (\hat{z}) + \hat{A}(\hat{z})^2]$

OR $\bar{\chi} = \frac{51}{104} L$

X = 0.548 L

(b) \(\hat{b} = \frac{7}{2} \) WHEN \(\hat{X} = \hat{L} \)

SUBSTITUTING INTO EQ. (1)...

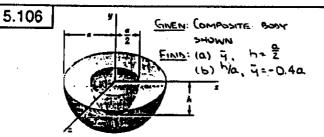
L(1+\(\hat{b} \hat{L} \) = \(\hat{c} \L(3 + \hat{L} + \frac{1}{2} \hat{L} \hat{L} \)

OR... \(1 + \frac{1}{6} \hat{L} = \frac{1}{2} + \frac{1}{6} \hat{L} + \frac{1}{24} \hat{L} \hat{L} \)

OR... \(\hat{L} = 12 \)

∴ \(\hat{L} = 23 \)

\(\tag{L} = 23 \)



	lv	4	4V
HEMISPHERE	± πα ³	- <u>ફ</u> ੋਨ	- A TI &-
SEMIECLIPSOIS	- 37 (\$) L = - 5710 L P	-Bh	+itmazhz

THEN. $\Sigma V = \frac{\pi}{6} \alpha^{2} (4\alpha - h)$ $\Sigma \vec{q} V = -\frac{\pi}{16} \alpha^{2} (4\alpha^{2} - h^{2})$ 5.108 NOW... $\Upsilon \Sigma V = \Sigma \vec{q} V$ So THAT $\Upsilon \left[\frac{\pi}{6} \alpha^{2} (4\alpha - h) \right] = -\frac{\pi}{16} \alpha^{2} (4\alpha^{2} - h^{2})$ OR $\Upsilon \left(4 - \frac{\pi}{6} \right) = -\frac{\pi}{6} \alpha \left[4 - \left(\frac{\pi}{6} \right)^{4} \right]$ (1)

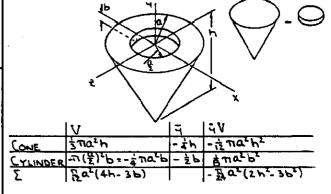
(a) \bar{Y}^{\pm} when $h^{\pm} \bar{z}$ Substituting $\bar{a}^{\pm} \bar{z}$ into Eq. (1). $\bar{Y}(4+\bar{z})^{\pm} = \bar{a}a[4-(\bar{z})^2]$ or $\bar{Y}^{\pm} = \frac{45}{112}a$

UR A S AND A S

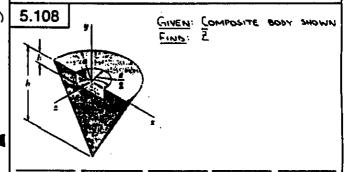
(b) $\frac{\pi^2}{a^2}$ WHEN $\frac{7}{a^2} = 0.4a$ SUBSTITUTING INTO EQ. (1)... (-0.4a)(4- $\frac{\pi}{a}$) = - $\frac{\pi}{a}$ a[4-($\frac{\pi}{a}$)²] OR 3($\frac{\pi}{a}$)² = 3.2($\frac{\pi}{a}$) +0.8 =0 THEN... $\frac{\pi}{a}$ = $\frac{3.2^{\frac{1}{a}}\sqrt{(-3.2)^2-4(3)(0.8)}}{2(3)}$ = $\frac{3.2^{\frac{1}{a}}0.8}{6}$ 5.107

GIVEN: COMPOSITE BODY SHOWN

FIRST NOTE THAT THE VALUES OF Y WILL BE THE SAME FOR THE GIVEN BODY AND THE BODY SHOWN BELOW. THEN..



HAVE .. $\overline{Y} \sum V = \sum \overline{q} V$ THEN .. $\overline{Y} \left[\sum_{12}^{12} \alpha^2 (4h - 3b) \right] = -\sum_{24}^{14} \alpha^2 (2h^2 - 3b^2)$ OR $\overline{Y} = -\frac{2h^2 - 3b^2}{2(4h - 3b)}$



FIRST NOTE THAT THE BODY CAN BE FORMED BY REMOVING A HALF-CYLINGER FROM A HALF-CONE.

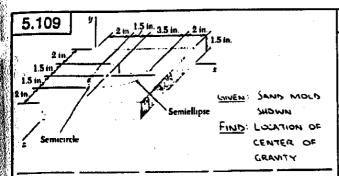


'	IV	1	l s V
HALF - CONE	tπa ² h	- 11 *	- & a3h
HALF- CYLINGER	- 3(E), P = - Ba, P	在一(生)施一	(\$ 02P
Σ	五at(4h-3b)		-1203(2h-b)

FROM SAMPLE PROBLEM 5.13

HAVE . ZZV = ZZV

THEN .. $\hat{z}[\frac{\pi}{24}\alpha^2(4h-3b)]=-\frac{1}{12}\alpha^3(2h-b)$



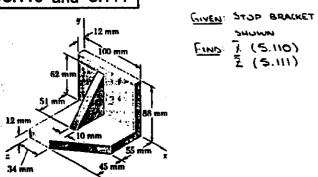
FIRST ASSUME THAT THE MOLD IS HOMOGENEOUS SO THAT ITS CENTER OF GRANTY WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING VOLUME, SYMMETRY THEN IMPLIES \$\bar{Z} \times 35 in.

Now	41		
k:		n	_
		· 🕢 -	<u> </u>
	$\langle \rangle$		
	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	, Σ _Ε +35-	4015 - 2.8634 m. 4035 - 4.9854 m.
		Y#233.	- 777 - 77 - 776 -

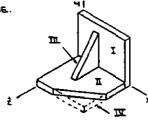
	V. 1N3	X.IN	٦, ₁₈₄	xV.1N4	4 V. IN4
1	(9)(1.5)(1)= 94 5	4.5	ن ۱۹۶	425.25	10.815
	- ?(1.5)(0.75)=-2.6507	2.8434	1.125	-7 5900	- 2.9820
	- g(3.5)(1.5)x0.75) 6.1850				-6.9581
Σ					60.935
	.ue 85V-55V:	. X (RS	,	12 3 A	. B3 M4

OR YEODINA S

5.110 and 5.111



FIRST ASSUME THAT THE BRACKET IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROIS OF THE CORRESPONDING VOLUME.



Xm = 34+2(110) = 39 mm Zm = 12+2(18)=56 mm

XX = 34+3(66)=18 mm 2x = 55+3(45)=85 mm

(CONTINUED)

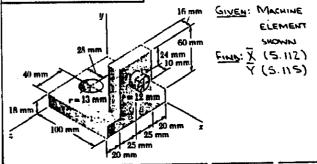
5.110 and 5.111 CONTINUED

	V mm3	X, mm	Ł, mm	XV, mm4	2V, mm4
	(100)(88)(12)=105 600	_	ب	280 000	r33 r00
	(100)(12)(88):105 600	50	56	5 280 000	5913 600
	£(10)(13)(51)+15 810	39	29	616 SAD	458 490
	- ¿(66)12)45) = -17 BZO	าธ	85	- 1 389 960	-1 514 700
Σ	209 190			9 786 630	5490490

5.110 HAVE. $\bar{X} = V = \bar{X} \bar{V}$ $\bar{X} (209 \cdot 190 \cdot mm^3) = 9 \cdot 186 \cdot 630 \cdot mm^2$ or $\bar{X} = 46.8 \cdot mm^2$

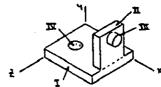
5.111 HAVE.. ₹ [V : ∑ ₹ V ₹ (209 190 mm³) = 5 490 990 mm² OR ₹ = 26.2 mm

5.112 and 5.115



FIRST ASSUME THAT THE MACHINE ELEMENT 15
HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL
CONCIDE WITH THE CENTROID OF THE CORRESPONDING
VOLUME:

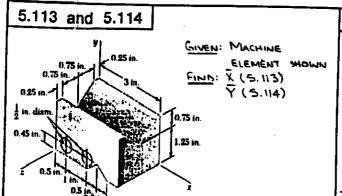
41 #



	V.mm ³	×. mm	4, mm	xV.mm	4V.mm4
Ī	(100)(18)(90)=162 000	50	g	8 100 000	
	(16)(60)(50)= 48000	92	48	4 416 000	2 304 000
\overline{m}	TI(12)2(10) = 45239	105	54	475 010	244 290
V	_7(13)E(1B)=-9556.7	26	9	- 267 590	- 86 010
$\overline{\overline{\Sigma}}$	204 967.2			12 723 420	3 950 580

5.112 HAVE .. \(\bar{X}\bar{V} = \bar{X}\bar{V}\) = 12.723.420 mm
OR \(\bar{X} = \bar{\alpha} \alpha \bar{\alpha} \).

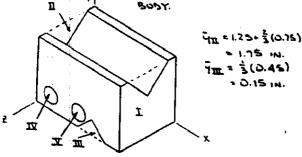
5.115 HAVE .. YEV . EYV Y(204 967,2 mm²) = 3 920280mm² OR Y = 19.13 mm ◀



FIRST ASSUME THAT THE MACHINE ELEMENT IS HOMOGENEOUS SO THAT IT'S CENTER OF GRAVITY WILL COINCINE WITH THE CENTROID OF THE CORRESPONDING VOLUME. ALSO NOTE THAT THE TWO HOLE'S AND THE Y-NOTCH EXTEND THROUGH THE

- 1.75 IN.

2 0.15 IN.

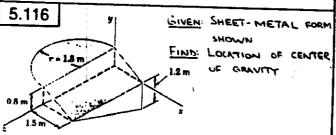


_	V. 12	Ž.IN.	Q.in.	1 x V 1 1 1 4	4V. 104
	(3)(2)(2)=12	1.5	1	18	12
<u>11</u>	- <u>‡(1.5)(3.75)(3) = -1.487</u> 5	1.5	1.75	- 2.53125	- 2.9531
	- 1(1)(0.45)(2)=-0.45	2	0.15	-0.90	-0.0675
72	-11(2)2-0.39270	0.5	0.45	-0.19635	
포	orse.c-=(s)*(\$) n-	1.5	0.45		-0.11612
Σ	וררס.פ		\Box	13.7B34	8.4240

5.113	:	HAVE	_XZV - ZxV
			X(9.0171 INS) = 13.7834 IN
			or X ± 1.518 in. ◀

5.114 HAVE. YZV. ZTV Y (9.0771 IN3)= 8.6260 IN Ÿ =0.950 in. ◀

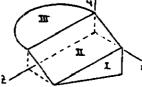
5.115 SEE SOLUTION TO PROBLEM 5.112



FIRST ASSUME THAT THE SHEET METAL IS (CONTINUED)

5.116 CONTINUED

homogeneous so that the center of gravity OF THE FORM WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING AREA.



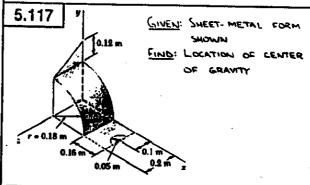
٩==غ(١٠٤) ==0.4 m == = 1(36) = 1.2 m

 $\sqrt{x_{m}} = -\frac{4(1.8)}{371} = -\frac{2.4}{37} m$

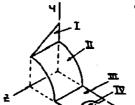
\(\frac{\bar{\pi}_m \bar{\pi}_m \bar{\pi}_m \bar{\pi}_n \mathred{\pi}_n \bar{\pi}_n \bar{\ 2(3.6)(1.2)= 2.16 1,5 -0.4 1.2 3.24 -0.864 2.592 IL (3.6)(1.7) = 6.12 | 0.75 0.4 1.8 4.59 2.448 11.016 III 7 (1.8)2 = 5.0894 - 24 0.8 1.8 - 3.888 4.0715 9.1609 13.3694 3.942 5.6555 22.769

HAVE. XXV - XXV: X(13.3694 m2) = 3.942 m3 OR X = 0.295 m YEV- Eq V: Y (13.3694 m2) + 5.6555 m

OR Y=0.423 m 2 EV= 22V: 2 (13.3694 m2)= 22.769 m3 = 1.703 m OR



FIRST ASSUME THAT THE SHEET METAL IS HOMOGENEOUS SO THAT THE CENTER OF GRAVITY OF THE FORM WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING AREA.



41=0.18+ \$(0.12), 222 m === \$(0.2 m)

Xn - 4n = 210.18 = 0.36 m

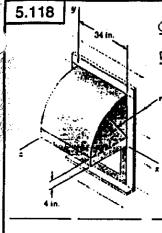
XIX = 0.34 - 4 = 0.05 = 0.31878 m

_	A, m2	X,m	4,11	ž,n	XA.m3	FA. m2	3A m3
	\$(0.2)\0.12)=0.DIZ	0	0.55			0.00264	
1	I (0.18)(0.2)= 0.0181	3.3L	j.	0.1	0.0048	D.00L48	3.005655
皿	(0.10)(0.5)=0.032	0.26	0		0.00832	٥	0.0032
区	-}(0.05) = -0.0012511	0.31818	0	0.1	-0001258	0	-0.000393
٤	0.096622						0.009 5-5
11.	VCV. C-	(r 7)		_			0.00 I CAL

HAVE. X \(\subseteq \times \ti

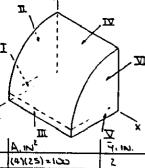
OR X+0.1402m Y ΣV= ΣqV: Y (0.096 ω22 m²) = 0.00912 m3

OR Y=0.0944m 2 ΣV - Σ 2V: 2 (0.096 622 m²) = 0.009 262 m² OR = 0.0959m.



GIVEN: SHEET- METAL AWNING SHOWN FIND: LOCATION OF CENTER OF GRAVITY

FIRST ASSUME THAT THE SHEET METAL IS HUMOLENEOUS SO THAT THE CENTER OF GRAVITY OF THE AWNING WILL COINCIBE WITH THE CENTROIN OF THE CORRESPONDING AREA.



II (4)(34)×136

V (4)(25)=100

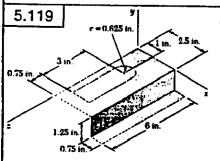
ЧП - ЧШ - 4 + 3П - 14.0103 IN. En - EN - 4-25 100 IN.

 $\frac{q_{1N}}{q_{1N}} = 4 + \frac{2 \times 25}{11} - 19.9155 \text{ in.}$ $\frac{2}{21N} = \frac{2 \times 25}{11} \cdot \frac{50}{11} \text{ in.}$

A = A = = = = (25)=156.257 IN $A_{12} = \frac{1}{2}(25)(34) = 425\pi \text{ in}^2$ $\frac{1}{2}, \text{in} = \frac{1}{4}, \text{in}^3 = \frac{1}{4}, \text{in}^3$ 200 1250 I 156.25 TT 490.87 14.6103 ส.เกเร 5208.3 ZZZ 3400 425TT = 1335.1B 199155 26,591 21,250 VI 154.25 TI : 493.87 14.4103 פורור. 5200.3

2652.9 41,606.6 37,566.6 NOW .. SYMMETRY IMPLIES $\bar{\chi}$ =17.00 IN. NO YEA = EqA: Y(26529 IN²) = 41,606.6 IN³ OR Y = 15.68 IN.

- Z Σ Α + Σ Ξ Α: - Z (2652.9 m²) = 37,566.6 m² 2 = 14.16 IN. OR.



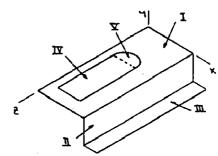
GIVEN: SHEET- METAL BRACKET SHOWN FIND: LOCATION OF CENTER OF GRAVITY

FIRST ASSUME THAT THE SHEET METAL IS HUMDGENEUGS SO THAT THE CENTER OF GRAVITY OF THE BRACKET WILL COINCIDE WITH THE CENTRO'S OF THE CORRESPONDING AREA. THEN (SEE DIAGRAM AT THE TOP OF NEXT COLUMN)

 $\frac{2}{2N} = 2.25 - \frac{4 \times 0.625}{3\Pi}$ = 1.984 74 m.

Au = - 2 (0.425)2

5.119 CONTINUED



	A. INZ	Ž.W.	٦, _{۱N} ,	2,14.	KA, IN 3	EM, AP	2A. IN3
			0	3	18.15	0	45
Ī	(1.25)(4)+7,5	2.5	-ಎ.ಆಽ	3	18.75	-4,6875	22.5
	(0.75)(6):45		-1.25	3	12,9375	-5.425	13.5
īV	(\$)(5)-375	١	0	3.75	-3.75	<i>ن</i> د	-14.0625
I	-0.613 59	1	0	1.984.14	-0.6359	0	- 1.21782
Σ	22,6364				44.073	-12.3125	65.7197

HAVE.. ĪZA=ĪĀA:

X(22.6364 IN2)= 46.0739 IN3

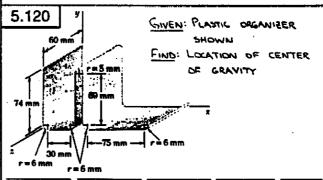
:AFZ = A3Ÿ

00 X = 2.04 IN. Y(22,6364 M1)=-10.3125 M3 OR Y =- 0.456 IN.

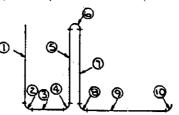
Ξ2A = ΣΞA:

Z(22,6364 W2)=65,7197 IN3

OR 2 = 2.90 IN.



FIRST ASSUME THAT THE PLASTIC IS HOMOGENEOUS SO THAT THE CENTER OF GRAVITY OF THE CRGANIZER WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING AREA. NOW NOTE THAT SYMMETRY IMPLES



x2 = 6- TT = 2.1803 mm = 36 + 77 + 39.820 mm To: 58 - 276 . 54.180 mm

X10 = 133+ 216 = 136.820 mm

42 = 44 = 48 = 410 = 6 - 216 = 2.1803 mm 4 = 75+ 275 + 78.183 mm

(CONTINUED)

= 30 mm

5.120 CONTINUED

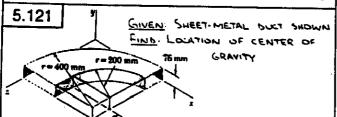
 $A_2 = A_4 = A_6 = A_{10} = \frac{\pi}{2} *6 * 60 * 565,49 mm^2$ $A_6 = \pi *5 * 60 * 942.48 mm^2$

Ì	A. mm2	X,mm	9.mm	XA, mm3	4A, mm3
1	(74)(4): 4440	0	43	D,	190 920
<u> 2</u>	565.49	2.1803	2.1803	1233	1 2 33
3	(30)(60): 1800	21	0	37 800	0
4	545.49	39.820	2 1803	22518	1233
_	(69)(65)+4140	42	40.5	173 880	167670
느	942.48	47	78.183	44 297	73686
	(L9X60): 4140	52	40.5	215280	167670
-		54.180	2.1603	30 638	1233
	(75)(60) - 4500	95.5	0	429750	0
10	Su5.49	136.820	2 1803	כרג רר	1233
Σ	22 224.44			1 032 746	604 FJB

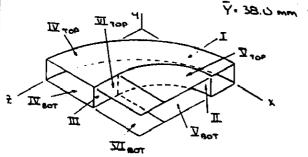
HAVE .. XΣA = Σ x A: X(22 224.44 mm²) = 1 032 766 mm²

YΣA - Σ q A: Y(22 224.44 mm²) = 604 B18 mm²

OR Y = 27.2 mm



FIRST ASSUME THAT THE SHEET METAL IS
HOMOGENEOUS SO THAT THE CENTER OF CRAVITY
OF THE DUCT WILL COINCIDE WITH THE CENTROIS
OF THE CORRESPONDING AREA. NOW NOTE THAT
SYMMETRY IMPLIES



 $\bar{X}_{I} = \bar{\hat{z}}_{I} = 400 - \frac{2 \times 400}{71} = 145.352 \text{ mm}$

XII = 400 - 2220 = 212.68 mm EI = 300 - 77 = 172.676 mm

XX = 2X = 400 - 4x400 = 230.23 mm

 $\bar{X}_{\overline{L}} = 4\omega - \frac{4\pi 200}{3\pi} = 315.12 \text{ mm}$ $\bar{\xi}_{\overline{L}} = 300 - \frac{4\pi 2\omega}{3\pi} = 215.12 \text{ mm}$

Also note that the curresponding top and Bottom areas will contribute equally when determining \bar{X} and \bar{Z} . Thus..

(CONTINUES)

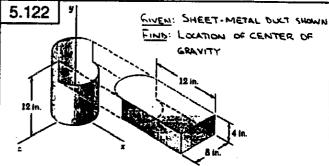
5.121 CONTINUED

	A. mm2	X. mm	Z.mm	XA. mm3	3A, mm3
	12 (400)(76)=47 752	145 352	145.352	6 940 850	6 940 850
Ī	12 (200)(7c)=23 B7c	272.68	172.676	6510 510	4 122 810
	(100)(76)+7600	200	350	1 520 000	2 440 000
V	2= \$ (400) = 251 327	230.23		51843020	
ĮΨ		315.12		- 19 799 620	
	-2(100+200)+-40 000			-12 000 000	
Σ	227 723			41 034 760	

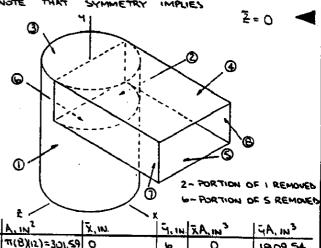
HAVE.. XEA: ExA: X(227 723 mm²): 41 034 760 mm OR X=180.2 mm ◀

Ē ΣA = ΣĒA: Ē(227 723 mm²) = 44 070 260 mm²

DR Ē = 193.5mm ◀



FIRST ASSUME THAT THE SHEET METAL IS
HOMOGENEOUS SO THAT THE CENTER OF GRAVITY
OF THE DUCT ASSEMBLY WILL COINCIDE WITH THE
CENTROIS OF THE CURRESPONDING AREA. NOW
NOTE THAT SYMMETRY IMPLIES

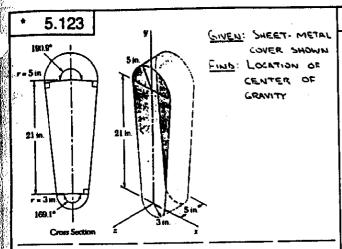


	£ /				
_	A. IN2	X, INL	4,14	ZA.IN3	Eu , Ap
	7(8)(12)=301.59		9	0	1809.54
۷.	-7(8)(4)=-50.27	= 2.5ALS	10	-128	-502.7
3_	5(4)2 = 52.13	-477 1.19765	12	- 42.667	301.56
	(15)(8).96	b	12	576	1152
<u> </u>	(12)(B)=96	و	Ø	576	148
	-2(4)2-25.13	20103.1: 118	8	- 42.667	- 201.04
1	(12)(4)-48	i.	10	288	480
	(12)(4).48	6	10	288	480
Σ	539.32			1514 1-14	429231

HAVE .. XEA - ETA: X (539.32 IN2) - 1514.666 IN2

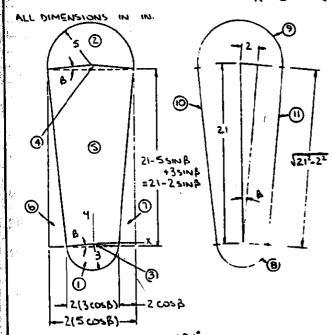
ΥΣΑ • Σ ¬ A : Υ(539.32 IN2) • 4287.32 IN2

OR Y .7.95 IN.



FIRST ASSUME THAT THE SHEET METAL IS
HUMOGENEOUS SO THAT THE CENTER OF GRAVITY
OF THE COVER WILL COINCIDE WITH THE
CENTROIS OF THE CORRESPONDING AREA. NOW
NOTE THAT SYMMETRY IMPLIES

X = 0



FIRST NOTE.. $\beta = \frac{90^{\circ} - \frac{169.1^{\circ}}{2} \cdot 5.45^{\circ}}{2} \cdot 5.45^{\circ}$ $\frac{7}{4!} = -\frac{2(3) \sin(\frac{169.1^{\circ}}{2})}{3(\frac{169.1^{\circ}}{2}, \frac{\pi}{180^{\circ}})} = A_{1} = (\frac{169.1^{\circ}}{2}, \frac{\pi}{180^{\circ}})(3)^{2}$ $= 13.281 \text{ in}^{2}$

 $\begin{aligned} &= -1.3492 \text{ in.} \\ &= -2.1 + \frac{2(5.51N(\frac{190.9^{\circ}}{2})}{3(\frac{190.9^{\circ}}{2}, \frac{11}{180^{\circ}})} & A_2 = (\frac{190.9^{\circ}}{2}, \frac{11}{180^{\circ}})(5)^2 \\ &= 22.99 \text{ in.} \\ &= -\frac{2}{3}(351N5.45^{\circ}) & A_3 = -\frac{1}{2}[2(3\cos 5.45^{\circ})] \end{aligned}$

 $\begin{array}{ll} & (3 \sin 5.45^{\circ}) \\ = -0.18995 \text{ in} & = -0.8509 \text{ in}^2 \\ & = 21 - \frac{3}{3}(5 \sin 5.45^{\circ}) & A_4 = \frac{1}{2}[2(5 \cos 5.45^{\circ})] \\ = 20.68 \text{ in}. & (5 \sin 5.45^{\circ}) \\ & A_4 = 2.364 \text{ in}^2 & (Continues) \end{array}$

5.123 CONTINUED

$\ddot{q}_3 = \frac{1}{2}(21 - 25 \text{ in 5.45}^\circ)$ $= 35 \text{ in 5.45}^\circ$	A== (21-251N5.45°) +2(5c055.45°)
M OS1.61 €	= 207.2 IN2
تار = تام = غ(2١-25١٨ 5.45°)	A Ay = - 2 (2 cos 545)
-3 SIN 5.45	4 (21-25IN 545°)
= 6.652 IN.	= - 20.72 IN2
48.= - 3 sin (1691)	$A_{\Theta} = [(169.1^{\circ} \times \frac{41}{180})(3)](5)$ = 44.27 in2
$= -2.024 \text{ in.} \frac{1909^{\circ}}{29} = 214 \frac{5000}{(1909^{\circ} + 1900)}$ $= 23.99 \text{ in.}$	Ag = [(1909= 180)(5)](5) = 83.30 IN2
= 23.99 IN. 710 = 711 = 75 = 10.120 IN.	A10 = A11 = (\(\overline{\zeta_1^2 - \zeta^2}\)(5) = 104.52 IN2

					1 3
1	A.IN	4.10	Ž. 1N.	3A.143	₹A, 1N3
1	13.281	- 1. 3492	-5	-17.919	4۱ . الما ما
2	41.65	22.99	- 5	951.5	- 2043.3
3	- 0.8509	-0.18995	-5	3.1662	4.255_
4	2.364	25.6B	-5	48.89	-11.850
5	207.2	10.120	- 5	2597	-1036.0
وا	- 20.72	∑دگها رما	- 5	-137.83	103.60
٦	- 20.72	6.62	- 5	-137.B3	103.60
8	44.27	-2.024	-2.5	- 89.60	-110.6B
9	83.30	23.99	-2.5	1998.4	-208.3
10	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	10.120	-2.5	1057.7	- 261.3
11	104.52	10,120	-2.5	1057.7	- 241.3
Σ	558.8			6834	-1952.7

HAVE .. Y [A = []A: Y (55B.B m²) = 6834 m²

OR Y = 12.23 m.

Z[A = []A: Z(55B.B m²) = -1952.7 m²

OR Z = -3.49 m.

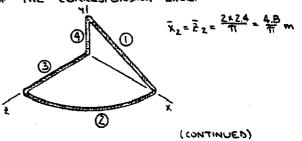
GIVEN: UNIFORM WIRE
BENT INTO THE
SHAPE SHOWN
FIND: LOCATION OF
CENTER OF
GRAVITY

FIRST ASSUME THAT THE WIRE IS

HOMOGENEOUS SO THAT ITS CENTER OF

GRAVITY WILL COINCIDE WITH THE CENTROIS

OF THE CORRESPONDING LINE.



5.124 CONTINUED

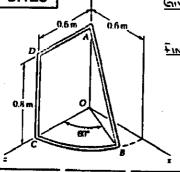
_	L.m	x,m	4,10	3.1	XL, M2	4L.m2	2 L, m2
$\underline{\square}$	2.5	1.2	05	0	3.12	1.3	0
2	₹ 24 - 1211	4.8	0	4.15	5.76	0	5.76
3	24	0	0	1.2	٥	0	2.88
4	1.0	0	٥.5	0	<u>0</u>	۵.5	ی
Σ	97699				8.88	1.8	8.44

X EL= ExL: X (9.7699 m)= 8.88 m2 OR X=0.909 m

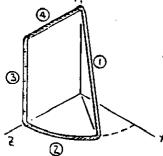
72L-29L: 7(97699m)=1.8 m2

OR Y = 0.1842m 2EL = EZL: 2 (9.7699 m) = B.64 m2 OR 2=0.884m

5.125 GIVEN: UNIFORM WIRE BENT INTO THE SHAPE SHOWN FIND: LOCATION OF LENTER DF GRAVITY



ASSUME THAT THE WIRE IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING LINE.



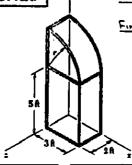
x,=0.3 SIN 60 = 0.1513 m 2. = 0.3 cos 60° = 0.15 m X2 = (\frac{0.6 \sin 30}{\pi | 6}) \sin 30 $\frac{\overline{\epsilon}_{z}}{\overline{\epsilon}} = \left(\frac{0.6 \times 10^{\circ}}{10^{\circ}}\right) \cos 30^{\circ}$ $= \frac{0.9 \times 10^{\circ}}{10^{\circ}} \cos 30^{\circ}$

L2 = (=)(0.6)=0.271 m

_	L,m				XL.m2	4L.m2	EL, m2		
7	1.0	0.1513	0.4	0.15	D.259B1	0.4	0.15		
2	0.27	2.4	o	55/2	0.18	0	3.31177		
3	0.8	0	0.4	0,6	0	0.32	0.48		
4	ا ما .د	0	9.0	0.3	0	0.48	0.18		
Σ	3.0283				0.43981	1.20	1.12177		
Н	HAVE. XEL = EXL: X(3.0283m) = 0.43981m2								

OR X=0.1452m YΣL= ΣqL: Y(3.0283m)=1.20 m2

OR Y=2396m 2ΣL=Σ=L: 2(3.0283m)=1.1217 m²
on 2=0.370 m² 5.126



GIVEN: PORTION OF GREENHOUSE FRAME WOWN

FIND: LOCATION OF CENTER OF GRANTY

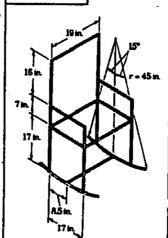
> FIRST ASSUME THAT THE CHANNELS ARE HOMOGENEOUS SO THAT THE CENTER OF GRAVITY OF THE FRAME WILL COINCIDE WITH THE CENTROD OF THE CORRESPONDING LINE.

 $\bar{X}_{B} = \bar{X}_{9} = \frac{2x^{3}}{\pi i} = \frac{5\pi}{\pi}$ it $\bar{X}_{B} = \bar{Y}_{9} = \frac{5\pi}{\pi}$ it $\bar{Y}_{B} = 0.99$ it

		- ω					
	L. \$2	×, 42		3,14	ãL, 422	4L, 422	EL. 622
<u></u>	2	3	٥	١	و	Ö	2
2	3	15	٥	2	4.5	0	L
3	5	3	2.5	0	15	12.5	0
<u>4</u> 5	5	3	2.5	2	15	12.5	10_
5	В	0	4	2	٥	32	16
<u>ط</u>	2	3	5	1	و	10	2_
1	3	1.5	5	2	4.5	15	<u> </u>
8	\$-3=47154	発	6.9099	0	g	32.562	U
9	₹•3•4.7124	¥	6.909	2	σ	32,562	9.4148
10	_2_	0	B	. 1	O	16	Z
Σ	39.4248				S	163,124	53.424B

HAVE .. XEL - ETL: X (39.4748 ft) - L9 ft2 OR X=1.750 St YEL = ΣqL: Y(39.4248 H). 163.124 62 Y = 4.14 lt OR. ₹\$L = \$\bar{2}\$L: \$\bar{2}\$(39.4248 ft) = \$3.4248 ft Ž=1.355 ¥t •

5.127

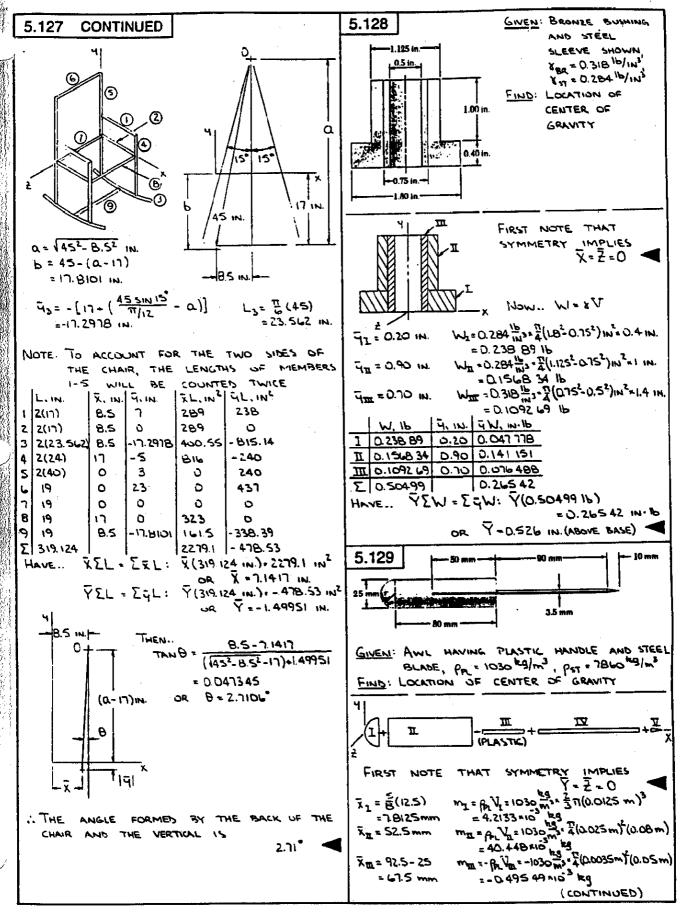


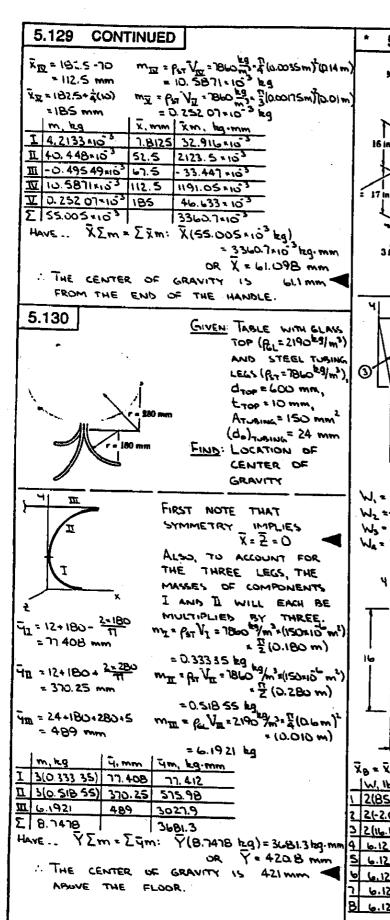
GIVEN: ROCKING CHAIR FRAME MOWN

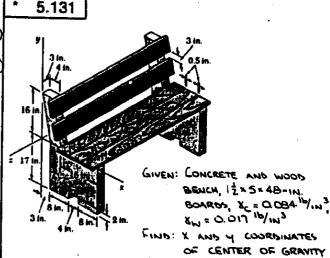
FIND: ANGLE BETWEEN CHAIR BACK AND VERTICAL

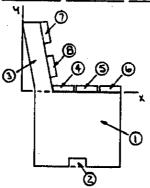
FIRST ASSUME THAT THE erognazomoh ei zuieut SO THAT THE CENTER OF GRAVITY OF THE FRAME WILL COINCIDE WITH THE CENTROID DE THE CORRESPONDING LINE ALXO, NOTE THAT THE CENTER OF GRAVITY MUST LIE ON A VERTICAL LINE THAT PASSES THROUGH THE POINT OF CONTINCT OF A

ROCKER AND THE GROWNS.

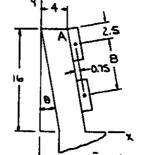








FIRST NOTE TO ACCOUNT FOR THE TWO CONCRETE ENDS, THE WEIGHTS OF COMPONENTS 1-3 WILL BE COUNTED TWICE.



ALL DIMENSIONS IN IN.

A TAN B = 16
B = 10. Lig LL

X7=4+2.5 SIND+075 COSD =5.1979 IN. 47=16-2.5 cos 0+0.75 sin 0=13.6810 in. x8 = x7+85108=6.6722 in. 78=71-8 cos8=5.8180 in W, Ib *W, m.16 7W, m.16 X, IN. 9, IN. 2(BSLB) 13 -8.5 - 1456. Slo 2227.7 2(-2.016) 13 -1b - 52.4K 44.512 3 2 (16.128) 8 112.896 258.05 25 0.15 58.14 4.59

5 6.12 ۱5 <u>0.75</u> 91.8 4.59 20.5 6.12 0.75 125.46 4.59 5.197 13.6BID 6.12 <u> 31.811</u> 83.72B 6.12 4.4722 S.BIBO 40.834 35.406

5.131 CONTINUED

THEN.. EW-230.1816

EXW = 2636.2 IN.16 41.11 PB.0001- = Wil X(230.18 1b)=2636.2 IN-16

OR X=11.45 IN.

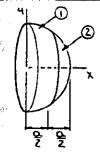
ΤΣΝ•ΣټΝ: Y(230.18 16)=-1000.89 will

OR Y=-4.35 IN.

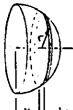
5.132

GIVEN: A HEMISHERE WHICH IS CUT OWT OTH COMPONENTS OF EDUAL INIGH AS SHOWN

FIND: X OF EACH COMPONENT



CHOOSE AS THE ELEMENT OF VOLUME A DISK OF RADIUS T AND THEKNESS dx. THEN di. Tr dx, XEL = X THE EQUATION OF THE GENERATING CURVE 15 X2+42 Q2 SO THAT C2 Q2-X2 AND THEN $dV = \pi (\alpha_z - x_z) dx$



 $\int_{0}^{\infty} \frac{1}{|x|^{2}} \int_{0}^{\infty} \frac{1}{|x|^{2}} \left(\alpha_{s}^{2} - x_{s} \right) dx = \mathcal{U} \left[\alpha_{s}^{2} x - \frac{2}{x_{s}} \right]_{0}^{\infty} dx$ $\frac{1}{2} = \frac{11}{24} \pi \alpha^3$ AND. $\sqrt{x_{EL}} = \sqrt{x_{EL}} \left(\pi (\alpha^2 + x^2) dx \right)$

 $=\pi[a^{2}\frac{x^{2}}{2}-\frac{x^{4}}{4}]^{\alpha/2}$

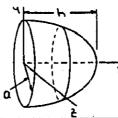
Now.. $\bar{X}_1 \bar{V}_1 = [\bar{X}_{EL} d\bar{V}: \bar{X}_1 (\frac{ii}{24} \pi \alpha^2) - \frac{1}{C_4} \pi \alpha^4]$ Now.. $\bar{X}_1 \bar{V}_1 = [\bar{X}_{EL} d\bar{V}: \bar{X}_1 (\frac{ii}{24} \pi \alpha^2) - \frac{1}{C_4} \pi \alpha^4]$

 $= \mu \left[\left[\sigma_z(\sigma) - \frac{2}{\sigma^2} \right] - \left[\sigma_z(\frac{z}{\sigma}) - \frac{2}{\left(\frac{z}{\sigma}\right)^2} \right] \right]$ $= \mu \left[\left[\sigma_z(\sigma) - \frac{2}{\sigma^2} \right] - \left[\sigma_z(\frac{z}{\sigma}) - \frac{2}{\left(\frac{z}{\sigma}\right)^2} \right] \right]$

AND $\int_{2}^{1} \bar{X}_{EL} dV = \int_{0}^{\infty} X \left\{ \pi(\Omega^{2} - X^{2}) dx \right\} = \pi \left[\Omega^{2} \frac{X^{2}}{2} - \frac{X^{4}}{4} \right]_{0}^{\infty}$ $= \pi \left[\left[\Omega^{2} \frac{(\Omega^{2} - (\Omega^{3}))}{4} \right] - \left[\Omega^{2} \frac{(\Omega^{2} - (\Omega^{3}))}{2} - \frac{(\Omega^{3} - (\Omega^{3}))}{4} \right] \right]$ $= \frac{2}{6} \pi \pi \Omega^{4}$ No.

Now.. $\bar{x}_{2}\bar{v}_{2} = \int_{\bar{x}} \bar{x}_{EL} d\bar{v}$: $\bar{x}_{2} \left(\frac{5}{24}\pi\alpha^{5}\right) = \frac{9}{64}\pi\alpha^{4}$ or $\bar{x}_{2} = \frac{21}{40}\alpha$

5.133

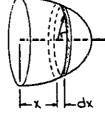


GIVEN: A SEMIELLIPSOID OF REVOLUTION WHICH IS OWT OTAL TWO COMPONENT'S OF EDWAL WINTH AS NWOHE FIND: X OF EACH

COMPONENT

Œ

CHUSE AS THE ELEMENT OF VOLUME A DISK OF RASIUS AND THICKNESS dx. THEN dv: mr2dx, xec=x THE EDUATION OF THE GENERATING CURVE IS 12+ 12 =1 50 THAT TE ME (h= X2) AND THEN dir = 7 (2 (h2-x2) dx



N = The WE (H - x) lax = TT RE [h x - X3] h/2 $= \frac{11}{24} \pi \sigma_s \mu$

 $= \frac{1}{4} \frac{\mu_{s}}{a_{s}} \left[\mu_{s} \frac{S}{x_{s}} - \frac{1}{4} \right]_{MS}^{S}$ $= \frac{1}{4} \frac{\mu_{s}}{a_{s}} \left[\mu_{s} \frac{S}{x_{s}} - \frac{1}{4} \right]_{MS}^{S}$ $= \frac{1}{4} \frac{\mu_{s}}{a_{s}} \left[\mu_{s} \frac{S}{x_{s}} - \frac{1}{4} \right]_{MS}^{S}$ $= \frac{1}{4} \frac{\mu_{s}}{a_{s}} \left[\mu_{s} \frac{S}{x_{s}} - \frac{1}{4} \right]_{MS}^{S}$

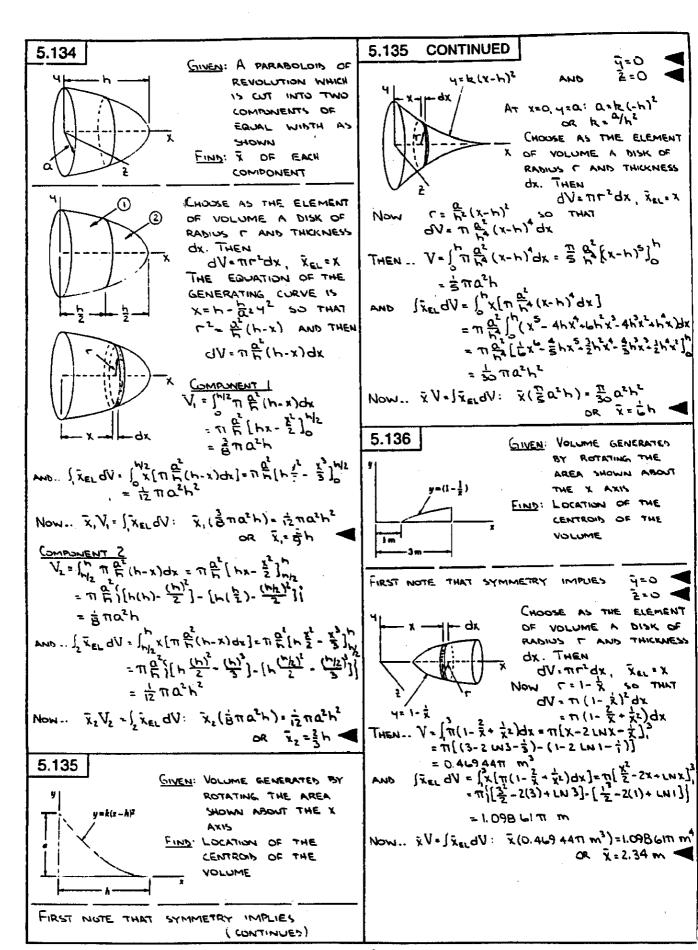
Now.. X, V, = 1, XeLdV: X, (24 πa2h)= 24 πa2h2

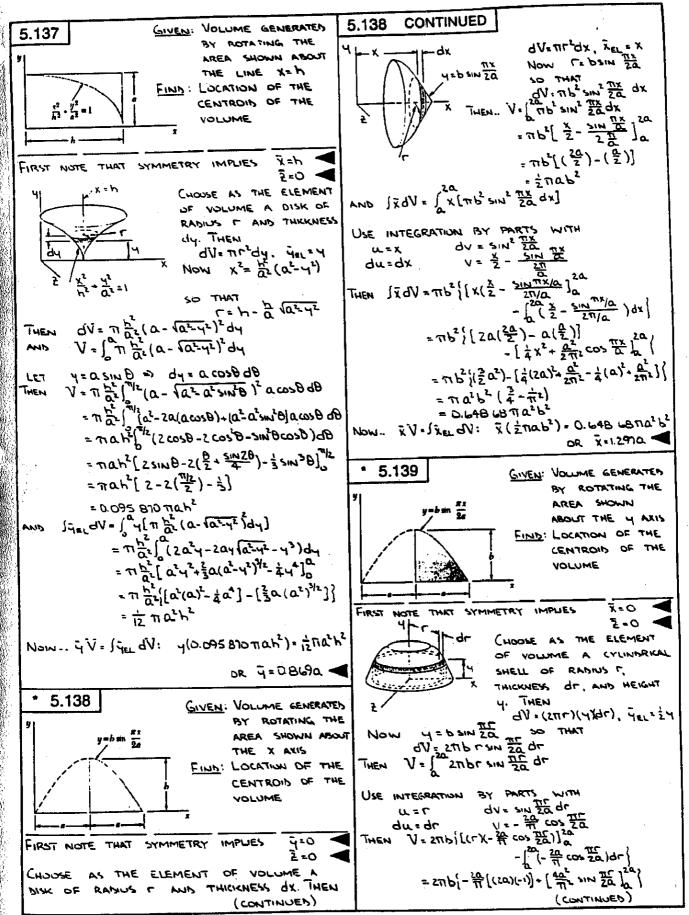
or X, = 24 h

NS = (4 4 5 (45 x5) 9x = 4 45 (45 x - 3) 145 = 4 \frac{\mu_{\sigma_{\end{subset}}}{\sigma_{\chincm\deta}}}}}\limbs_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\chincm\deta}}}}}\limbs_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\chincm\deta_{\sigma_{\sigma_{\sigma_{\sigma_{\sigma_{\chincm\deta_{\sigma_{\sigma_{\chincm\deta_{\sigma_{\sigma_{\chincm\deta_{\sigma_{\chincm\deta_{\sigma_{\chincm\deta_{\sigma_{\chincm\deta_{\sigma_{\chincm\deta_{\sigma_{\chincm\deta_{\chincm\deta_{\chincm\deta_{\chincm\deta_{\sigma_{\chincm\deta_{\din\chincm\deta}}}}}}}}}}\endintintintinting}}}}}}}}}}}}}}}}}}}}} = \$ nath

AND \[\bar{x} \in \text{V} = \int \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell} \bar{\mathbell}{\mathbell}{\mathbell}{\mathbell}{\mathbell}{\mathbell}{\ $= \frac{\mu^{2}}{\sigma_{r}} \left\{ \left[\mu_{r}, \frac{5}{(\nu)_{r}} - \frac{4}{(\nu)_{r}} \right] - \left[\mu_{r}, \frac{5}{(\nu)^{2}} - \frac{4}{(\nu)^{2}} \right] \right\}$ $= \frac{\mu}{\nu^{2}} \left[\mu_{r}, \frac{5}{x_{r}} - \frac{4}{x_{r}} \right]^{\nu/3}$ $= \frac{\mu}{\nu^{1/3}} \frac{\nu}{\sigma_{r}} \left[\mu_{r}, \frac{5}{x_{r}} - \frac{4}{x_{r}} \right]^{\nu/3}$ = 3 m a2 h2

Now .. \$\bar{x}_2 \bar{V}_2 = \int_1 \bar{x}_{eL} dV : \bar{X}_2 (\frac{5}{24} \pi a^2 h) = \frac{9}{64} \pi a^2 h^2 OR X2 = 40 h ◀





5.139 CONTINUED

V= 2776 (402 - 402) = B a z b (1 - #)

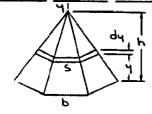
= 5.4535 a2b 17 EL dV . 120 (1 b sin 20) (27 br sin 20 dr) = The Land The dr

BY PARTS WITH dv = SIN 2 20 dr USE INTEGRATION BY PARTS ゲート V= = - SIN TIF/A du : dr

THEN .. I YEL div = 1762 \ [(17)(2 - \frac{510 m/a}{27/a})]a - 10 (2 - 510 0) 9-) $-\left[\frac{2\alpha}{4} + \frac{\alpha}{2n}\cos\frac{\pi}{2}\right]^{2\alpha}$ = 716 2 20 - [(20) + 20 - (0) + 20] = 7 0 6 (3 - 4 = 2.0379 a262

Now .. y V = Sqee dV: y (5.4535 a2b) = 2.0379 a2b2 OR 4=0.3746

5.140 GIVEN: A REGULAR PYRAMIS OF HEIGHT H AND N SIDES PHOM: d = \$ ABOVE THE BASE



CHOOSE AS THE ELEMENT OF VOLUME A HORIZONTAL SLICE OF THICKNESS dy. FOR ANY NUMBER N OF SINES, THE AREA OF THE BASE UE THE

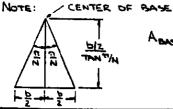
PYRAMIS IS GIVEN BY Amuse = kb2 WHERE It = k(N); SEE NUTE BELOW. USING SIMILAR TRIANGLES HAVE

OR 5= = (h-4) THEN .. di = Asike dy = ks dy = k h (h-y) dy

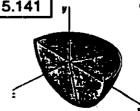
AND V = | k h (h-y) dy = k h [-3(h-y)] h = 3 k b h

Acos. Ter = 4 (= 200 THEN 12 (1) 4-5445043) da = he be (= houz = 3 hous = 4 up) = 12 k be he

Now. 4 /= /4EL dV: 4 (3 & b2 h) = 12 12 12 12 h 4= \$h Q.E.D.



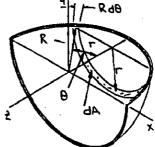
ABASE = N (12 b + D/2 TANTIN) = K(N) PE



GIVEN: ONE. HALF OF A THIN, UNIFORM HEMISPHERICAL SHELL

FIND: LOCATION OF CENTROIS USING DIRECT INTEGRATION

FIRST NOTE THAT SYMMETRY IMPLIES



THE ELEMENT OF AREA da of the shell SHOWN IS OBTAINED BY CUTTING THE SHELL WITH TWO PLANES PARALLEL TO THE XY PLANE. NOW dh=(77)(RdD).

WHERE TERSIND

dA = TIR SINDOD, TEL = TI SIND TAHT OZ A = July TR SINDOD = TR2 [- coop] WIZ THEN

MD ITELDA = Jak (- The sind) (TR2 sind dB) = - 2R3 [B - SIN 2B] TIL

q (mR2) = - = R3 Now. JA = JGELDA: SYMMETRY IMPLIES 2=9 : 2 =- 2R

5.142





GIVEN: PUNCH BOWL OF UNIFORM WALL THICKNESS t, R = 250 mm, teck

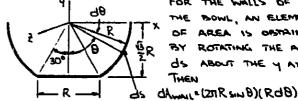
FIND: LOCATION OF THE CENTER OF GRAVITY OF (A) THE BOWL

(b) THE PUNCH

(a) Bowl

FIRST NOTE THAT SYMMETRY IMPLIES

FOR THE COORDINATE AKE'S SHOWN BELOW. NOW ASSUME THAT THE BOWL MAY BE TREATED AS A SHELL! THE CENTER UF GRAVITY OF THE BOWL WILL COINCIDE WITH THE CENTROIS OF THE SHELL.



FOR THE WALLS OF THE BOWL AN ELEMENT OF AREA IS OBTAINED BY ROTATING THE ARC ds ABOUT THE Y AXIS THEN

5.142 CONTINUED

THEN $A_{WALL} = R_{COS}\theta$ $A_{WALL} = \int_{A_{WALL}}^{A_{1/2}} 2\pi R^2 \sin\theta d\theta = 2\pi R^2 \left[-\cos\theta\right]_{A_{1/2}}^{A_{1/2}}$ $= \pi \sqrt{3} R^2$

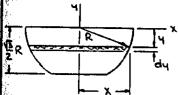
AND TWALL Awall I STELL WALL DA 1 STELL COSE (27) RE SIND de) = TIR (COSE) TO =

BY OBSERVATION. ABASE = TR, JOANE = - 2R
NOW. - JEA = ΣJA
CR. - J(π13R2 - 7R2) = - 3π1R3 - 7R2(- 2R)
OR - J=-0.48763R - R= 250 mm
... - J=-1219 mm

(b) PUNCH

FIRST NOTE THAT SYMMETRY IMPLIES ROOM

AND THAT BECAUSE THE PUNCH IS HOMOGENEOUS IT'S CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING VOLUME



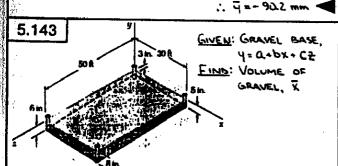
CHOOSE AS THE
ELEMENT OF VOLUME
A DISK OF RABIUS
X AND THICKNESS
dy. THEN
dV=TX2dy, Tel= 4
NOW... X2+42=R2

THEN V = [T(R2-42) dy = T(R4-342) CR - 2R = -T[R2(-2R)-3(-2R)] = 372 CR

MD (JECGL) = [(A)[U(S, A,)94] = U[\$ 8, A, - \$ 4,] & [& 8

=-T[2R2(-ER)2-4(-ER)3]=-157R4
Now 9V=146,UV: 4(376R3)=-157R4

OR 4 = 53 R R= 250 mm



FIRST DETERMINE THE CONSTANTS Q, b, AND C

AT X=0, 2=0: y=-3 in:-12 lt=0 Q=-4 lt

x=30 lt, 2=0: y=-5 in:-12 lt=-4 lt+b(30 lt)

b=-160

X=0, 2=50 lt. y=-6 in:-12 lt=-4 lt+C(50 lt)

(CONTINUED)

5.143 CONTINUED

OR C = - 100 X - 100 2 2 200 2 2 - 4 (1 + 43 X + 502) WHERE ALL DIMENSIONS ARE IN FEET

CHOOSE AS THE

ELEMENT OF VOLUME

A FILAMENT OF BASE

dx -d2 AND HEIGHT

I YI. THEN

dV-141dxd2, Xel = X

THEN $V = \int_{0}^{30} \int_{0}^{30} \frac{1}{4} (1 + \frac{1}{4} \cdot x + \frac{1}{50} \cdot 2) dx dz$ $= \frac{1}{4} \int_{0}^{30} \left[x + \frac{1}{40} x^{2} + \frac{2}{50} x \right]_{0}^{30} dz$ $= \frac{1}{4} \int_{0}^{30} \left[x + \frac{1}{40} x^{2} + \frac{2}{50} x \right]_{0}^{30} dz$ $= \frac{1}{4} \int_{0}^{30} \left[30 + \frac{(30)^{2}}{40} + \frac{2}{50} (30) \right] dz$

 $=\frac{1}{4}\left[402+\frac{3}{10}2^{2}\right]_{0}^{20}=\frac{1}{4}\left[40(50)+\frac{3}{10}(50)^{2}\right]$

AND $|\vec{x}_{2L}dV|^{2} = (87.5)^{2} \cdot (\frac{1}{4}(1+\frac{1}{4})x + \frac{1}{4})^{2} \cdot (30)^{2} \cdot (30)^{2}$ $= \frac{1}{4} \int_{0}^{80} \left[\frac{2}{X^{2}} + \frac{1}{125}x^{3} + \frac{2}{100}x^{2} \right]_{0}^{20} dz$ $= \frac{1}{4} \left[(450 + 200)z + \frac{9}{2}z^{2} \right]_{0}^{80}$ $= \frac{1}{4} \left[(450 + 200)z + \frac{9}{2}(50)^{2} \right]$ $= 10.937.5 \text{ M}^{4}$

5.144 GIVEN: VOLUME PLANE YE TO STANE STAN

GIVEN: VOLUME BETWEEN THE XZ

FLANE AND THE SURFACE

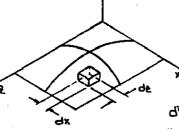
Y = \frac{0.24}{0.24} \left(0.00 \text{V}^2\right)(b.2 - 2^2\right)

FIND: LOCATION OF THE

CENTRON USING

BIRECT INTEGRATION

FIRST NUTE THAT SYMMETRY IMPLIES X = 2



CHOSE AS THE

ELEMENT OF

VOLUME A

X FILAMENT OF BASE

dx d and

HEIGHT Y. THEN

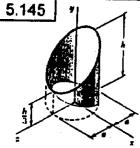
dV= y dxd2, Tel= 2y

THEN $V_*\int_0^b \int_0^a \frac{|bh}{Q^2b^2} (\alpha x - x^2)(bz - z^2) dxdz$ (con7inue5)

5.144 CONTINUED

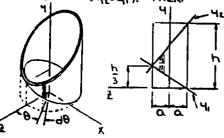
 $V_{2} \frac{1}{16} \frac{1}$

Now.. 可V= 「qec clV: 可(青abh)= 225 abh2 OR 可=是h



CIVEN: THE PORTION OF A CIRCULAR PIPE SHOWN FIND: LOCATION OF THE CENTROIS

FIRST NOTE THAT SYMMETRY IMPLIES X:0 ASSUME THAT THE PIPE MAS A UNIFORM WALL THICKNESS & AND CHOOSE AS THE ELEMENT OF UDLUME A VERTICAL STRIP OF WINTH Qdb AND HEIGHT (42-41). THEN



 $dV = (y_2 - y_1)t a d\theta, \quad \forall e_1 = \frac{1}{2}(y_1 + \vec{y}_2) \quad \vec{\epsilon}_{e_1} = 2$ $Nbw ... \quad y_1 = \frac{h/2}{2a} + \frac{h}{a} \qquad \qquad y_2 = \frac{2h/2}{2a} + \frac{2}{3}h$ $= \frac{h}{ba}(2+a) \qquad \qquad = \frac{h}{3a}(-2+2a)$

AND $2 = \Omega \cos \theta$ THEN $(4^r - 4^l) = \frac{10}{10} (-\Omega \cos \theta + 2\Omega) - \frac{10}{10} (\Omega \cos \theta + \Omega)$ $= \frac{10}{10} (1 - \cos \theta)$

MD $(y_1+y_2) = \frac{h}{h}(a\cos\theta + a) + \frac{h}{h}(-a\cos\theta + 2a)$ $= \frac{h}{h}(5-\cos\theta)$ (continues) 5.145 CONTINUED

: $dV = \frac{aht}{2}(1-cos\theta)d\theta$, $\forall e_L = \frac{h}{12}(5-cos\theta)$, $\hat{\epsilon}_{e_L} = a cos\theta$ Then $V = 2\int_0^{\pi} \frac{aht}{2}(1-cos\theta)d\theta = aht[\theta - sin\theta]_0^{\pi}$ $= \pi aht$ And $\int \vec{\gamma}_{E_L} dV = 2\int_0^{\pi} \frac{h}{12}(5-cos\theta)[\frac{aht}{2}(1-cos\theta)d\theta]$ $= \frac{ah^2t}{12}\int_0^{\pi} (5-cos\theta + cos^2\theta)d\theta$ $= \frac{ah^2t}{12}[5\theta - cos\theta + \frac{aht}{2} + \frac{sin^2\theta}{4}]_0^{\pi}$ $= \frac{ah^2t}{12}[5\theta - cos\theta + \frac{aht}{2} + \frac{sin^2\theta}{4}]_0^{\pi}$ $= \frac{ah^2t}{12}[5\theta - cos\theta + \frac{aht}{2} + \frac{sin^2\theta}{4}]_0^{\pi}$

 $= \frac{11}{24} \pi \alpha h^2 t$ $\left\{ \tilde{z}_{el} dV \cdot z \right\} \alpha \cos \theta \left\{ \frac{\alpha h t}{2} (1 - \cos \theta) d\theta \right\}$ $= \alpha^2 h t \left\{ \sin \theta - \frac{\beta}{2} - \frac{\sin 2\theta}{4} \right\}_0^{\pi}$ $= -\frac{1}{2} \pi \alpha^2 h t$

Now. $\vec{q} \vec{V} = \vec{q}_{el} \vec{d} \vec{V}$: $\vec{q} (\pi a h t) = \frac{1}{24} \pi a h^2 t$ or $\vec{q} = \frac{1}{24} h$ AND $\vec{e} \vec{V} = \vec{e}_{el} \vec{d} \vec{V}$: $\vec{e} (\pi a h t) = -\frac{1}{2} \pi a^2 h t$ or $\vec{e} = -\frac{1}{2} a$

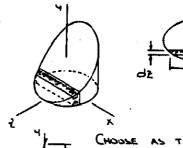
5.146

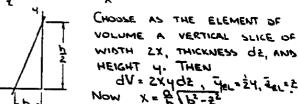
CIVEN: THE PORTION OF AN ELLIPTICAL CYLINDER SHOWN

FIND: LOCATION OF THE CENTROIS

FIRST NOTE THAT SYMMETRY IMPLIES

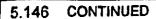






THEN $V = \int_{P} (2\frac{P}{P} \frac{(P_1 - 5_2)}{(P_2 - 5_2)} \left(\frac{P}{P} (P - 5_2) \right) d5$

THEN $V = \frac{\partial h}{\partial t} \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} (b \cos \theta) [b(i-sin\theta)] b \cos \theta d\theta$ $= \alpha b h \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} (\cos^2 \theta - \sin \theta \cos^2 \theta) d\theta$ $= \alpha b h [\frac{2}{4} + \frac{\sin 2\theta}{4} + \frac{1}{3} \cos^3 \theta]_{-\frac{\pi}{4}}^{\frac{\pi}{4}}$



V= 270pp = [{ = 50 (p- =) { (2 = 6-20) 20 (p- e) de} = # 8pg [(P-5), (P-5, 4p-5, 95 THEN $\int_{A}^{A} \frac{1}{4} \frac{1}{$

= \$\frac{1}{4} app_5 \int \((co2_5\theta - 5 > 10\theta co2_5\theta) d\theta \\ \frac{1}{4} \(\alpha - \frac{1}{2} \theta \) \\ \text{18} \\ \tex

Mow sin 2 B = 2 (1- cos 20) cos 2 B = 2 (1+ cos 20) + \$\frac{1}{4}\text{0} - \$\frac{1}{4}(\frac{5}{5} + \frac{1}{2\int 40})\frac{1}{2}\frac{

Using single cost θ = $\Delta b^2 h \int_{-\pi/2}^{\pi/2} (\sin\theta \cos^2\theta - \sin\theta \cos^2\theta) d\theta$ $= \Delta b^2 h \int_{-\pi/2}^{\pi/2} (\sin\theta \cos^2\theta - \sin\theta \cos^2\theta) d\theta$ $\int_{-2\pi/2}^{2\pi/2} dV = \Delta b^2 h \int_{-\pi/2}^{\pi/2} [\sin\theta \cos^2\theta - \frac{1}{4}(1-\cos^2\theta)] d\theta$

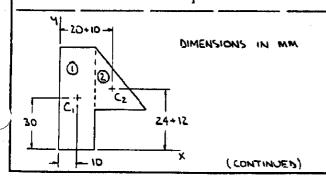
= ab2 + [- = cos2 - 40+4(= + SIN4B)] NS

=- # 48PsH

NON .. 9 V = SqEL dV: q (ETABH) = 32 Tabh व्य प्राहित

2 - SEL dV: 2 (2 TRABH) = - B TI A B'H 5 - 4 P

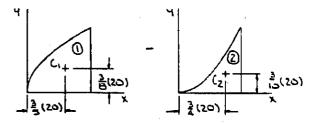
5.147 GIVEN: PLANE AREA 20 mm, 30 mm FIND: X AND Y



CONTINUED 5.147

	A, mm2	x,mm	4.mm	KM, MM3	9A. mm3	
\exists	20160:1200	9	30	12 000	36 ooo	
2	2+30+36+540	30	ى ش	16 200	19 440	
Σ	1740			28200	55440	
		THEN		ž3 = A3		
			፟፟፝ኢ	(1740)=	78 mo	
			_		X=16.21 mm	4
		AND		ΣA - Σ;		
ŀ			Y	(1740) .	55440	
				DR '	Y = 31.9 mm	-

5.148 GIVEN: PLANE AREA SHOWN FIND: X AND Y 20 in



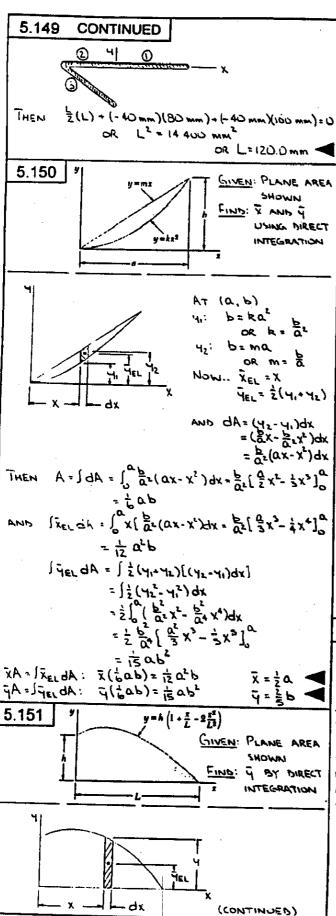
	DIMENSIO				_
A.10	1 ₅	X.1N.	์ จุงพ.	24.1N3	7A. 123
	2)(20)= 800/3	12	7.5	3200	2000
2 -3(2	0)(20)= .400)z	15	صا	-2000	- <i>90</i> 0
Σ	400/3			1200	1200
		THE		ΣA - Σ:	
			Ϋ́	(400/3) =	1200
				OR	Z = 9.00

(400/3) = 1200 DR Ÿ=9.00 IN. ◀

NOTE: SYMMETRY IMPLIES X = Y. WHICH IS CONFIRMED THE ABOVE SOLUTION. BY

5.149 GIVEN: HOMOGENEOUS WIRE BCD IS HORIZONTAL FIND: L

FIRST NOTE THAT FOR EQUILIBRIUM, THE CENTER OF GRAVITY OF THE WIRE MUST LIE ON A VERTICAL LINE THROUGH C. FURTHER, BECAUSE THE WIRE IS HOMOGENEOUS, THE CENTER OF GRAVITY OF THE WIRE WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING LINE. THUS V = 0 (SEE SKETCH ON THE NEXT SO THAT EXL = O PAGE) (CONTINUED)

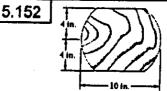


5.151 CONTINUED

HAVE dA = 4dx = h(1+ = - 2 12)dx

THEN A: $\int_{0}^{L} h(1+\frac{x}{L}-2\frac{x^{2}}{L^{2}})dx$ = $h[x+\frac{1}{2L}x^{2}-\frac{2}{3L^{2}}x^{3}]_{0}^{L} = \frac{2}{5}hL$ AND $\int_{0}^{L} dA = \int_{0}^{L} \frac{1}{2}h(1+\frac{x}{L}-2\frac{x^{2}}{L^{2}})f_{h}(1+\frac{x}{L}-2\frac{x^{2}}{L^{2}})dx]$ = $\frac{1}{2}h^{2}[x+\frac{1}{L}x^{2}-\frac{1}{L^{2}}x^{3}-\frac{1}{L^{3}}x^{4}+\frac{x^{4}}{5L^{4}}x^{5}]_{0}^{L}$ = $\frac{1}{5}Lh^{2}$

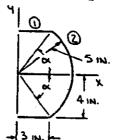
 \ddot{q} A=| \ddot{q} _{EL}dA: \ddot{q} (\ddot{g} hL)= \ddot{g} Lh² \ddot{q} = \ddot{u} 2sh \ddot{q} 0ρ \ddot{q} =048h \ddot{q}



GIVEN: WOODEN SPHERS
WITH TWO EDUCAT
CAPS REMOVED

FIND: SURFACE AREA UK

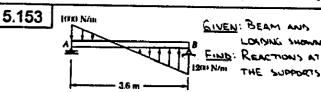
THE SURFACE AREA CAN BE GENERATED BY ROTATING THE LINE SHOWN ABOUT THE Y AXIS APPLYING THE FIRST THEOREM OF PAPAUS. GULDINUS HAVE



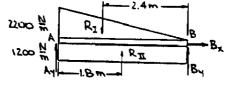
A = $2\pi \bar{X}L = 2\pi \bar{\Sigma}L$ = $2\pi (2\bar{x}, L_b + \bar{x}_2 L_2)$ NOW TANK = $\frac{3}{3}$ OR $x = 53.130^{\circ}$ THEN $\bar{X}_2 = \frac{5iN \cdot 5iN \cdot 53.130^{\circ}}{53.130^{\circ} \cdot \frac{7}{180^{\circ}}}$ = 4.313L in. AND $L_2 = 2(53.130^{\circ} \cdot \frac{7}{180^{\circ}})(5 \text{ in})$

= 9.2729 IN.

 $\therefore A = 2\pi \left\{ 2\left(\frac{3}{2} \text{ in.}\right)(3 \text{ in.}) + (4.3136 \text{ in.})(9.2729 \text{ in.}) \right\}$ or $A = 308 \text{ in}^2$

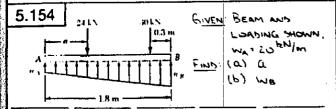


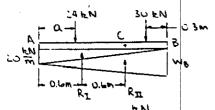
FIRST REPLACE THE GIVEN LOADING WITH THE LOADING SHOWN BELOW. THE TWO LOADINGS ARE EQUIVALENT BECAUSE BOTH ARE DEFINED BY A LINEAR RELATION BETWEEN LOAD AND DISTANCE AND THE VALUES AT THE END POINTS ARE THE SAME.



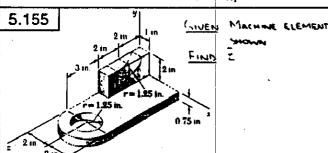


HAVE.. $R_1 = \frac{1}{2}(3.6m)(2200 \frac{N}{m}) = 3960 N$ $R_1 = (3.6m)(1200 \frac{N}{m}) = 4320 N$ THEN.. $\frac{1}{2} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{j=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{j=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{i=1}^{4} \sum_{j=1}^{4} \sum_{j=$

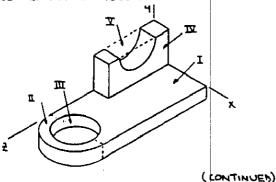




HAVE. R_1 = \(\frac{1}{2}\left(1.8 m)\left(20 \frac{k_N}{m}\right) = 18 k_N \\
R_1 = \(\frac{1}{2}\left(1.8 m)\left(\omega_0 \frac{k_N}{m}\right) \cdot 0.9 \omega_0 \frac{k_N}{m} \\
(\Omega) \quad \text{TS} M_c = \Omega \text{C} \left(1.2 - \Omega) m \cdot 24 k_N - \Omega \omega_0 \text{kN} \cdot 0 \\
- \Omega 3 m \cdot \delta \cdot \omega \text{kN} \cdot \Omega \\
- \Omega 3 m \cdot \delta \cdot \omega \text{kN} \cdot \Omega \\
- \Omega 3 m \cdot \delta \cdot \omega \omega \omega \omega \omega \omega \cdot \omega \omega



FIRST ASSUME THAT THE MACHINE ELEMENT IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROIS OF THE CORRESPONDING VOLUME.

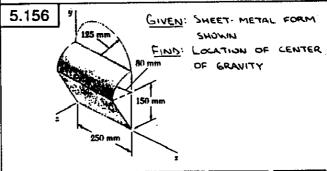


5.155 CONTINUED

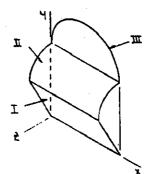
12. in. EV. in.	V. 1113	1
3.5 73.5	I (4)(0.15)(1) = 21	7
7+ 37 - 7.8488 36,987	I 2(2) (0.75) = 4.7124	
	III -77 (1.25) (0.75) = -3.6816	
2 16	立 いパンメイトトラ	立
2 - 4.9088	V - 1 (1.25)2(1) =- 2.4544	$\overline{\mathbf{x}}$
95.807	27.516	Σ
2 -4	\[\frac{1}{2} \left(1.25)^2 (1) = -2.4544 \] \[\frac{1}{2} \left(1.25)^2 \left(1) = -2.4544 \]	고

TLAVE. 25V. [2V: 2(27.57614)= 95.80714

OR 2=3.47114



FIRST ASSUME THAT THE SHEET METAL IS
HOMOGENEOUS SO THAT THE CENTER OF GRAVITY
OF THE FORM WILL COINCINE WITH THE CENTROIS
OF THE CURRESPONDING AREA. NOW NOTE THAT
SYMMETRY IMPLIES



 $\vec{Q}_{II} = 150 + \frac{2480}{17}$ = 200.93 mm $\vec{E}_{II} = \frac{2480}{17}$ = 50.930 mm

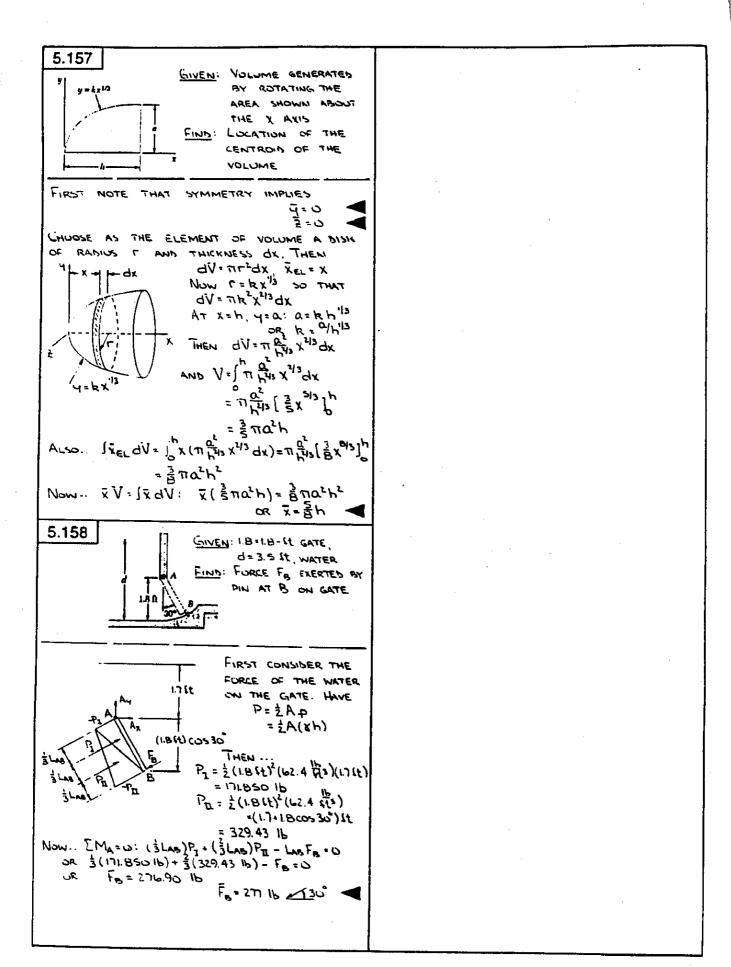
X = 125 mm

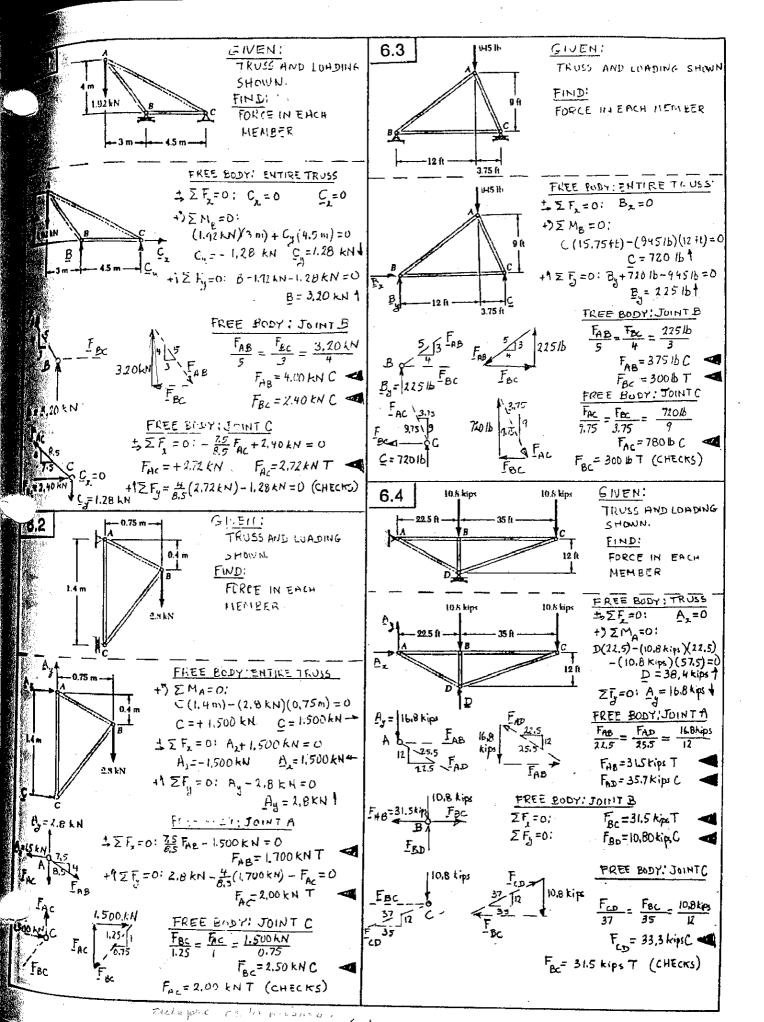
 $\sqrt{37} = 230 + \frac{4 \times 125}{377}$ = 283.05 mm

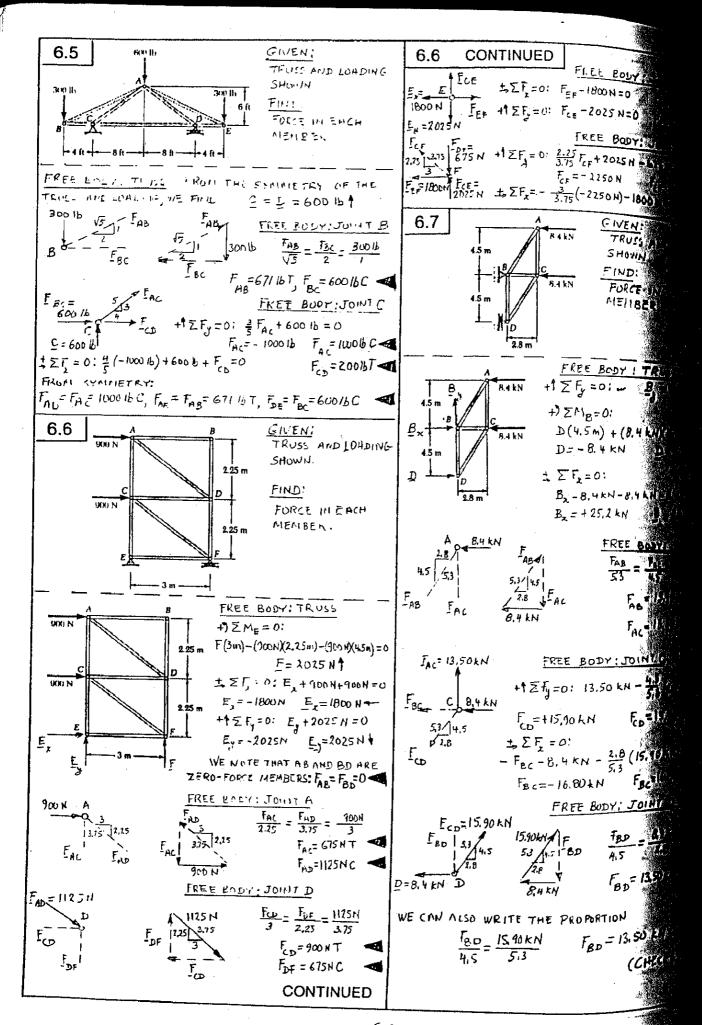
			^		_ 1
	A. mm2	4,000	2, mm	JA,mm3	2A, mm3
I	(250)(170)=42 500	75	40	3 187 500	1700 000
П	7(80)(250)=31416	200.93	50.930	6312400	1 600 000
Ŋ	7 (125)2 24 544	263.05	0	6 947 200	0_
Σ	98 460			16 447 100	3 300 000

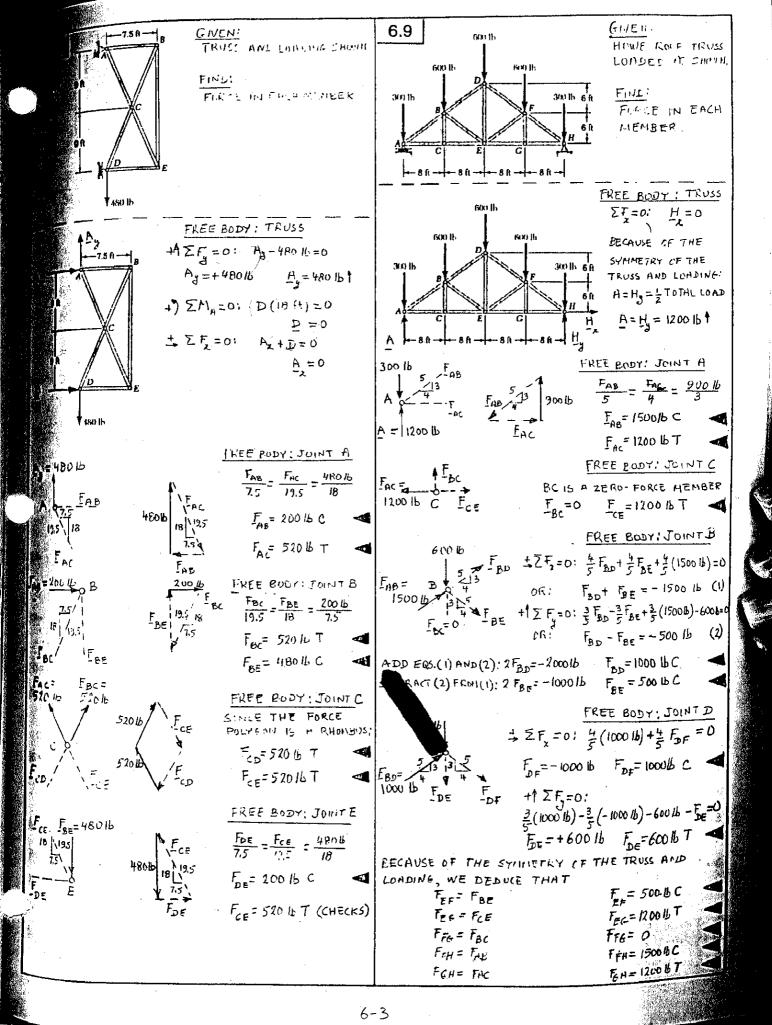
HAVE .. YEA = EGA: Y(98 460 mm²) = 16447 100 mm²
OR Y=1620 mm

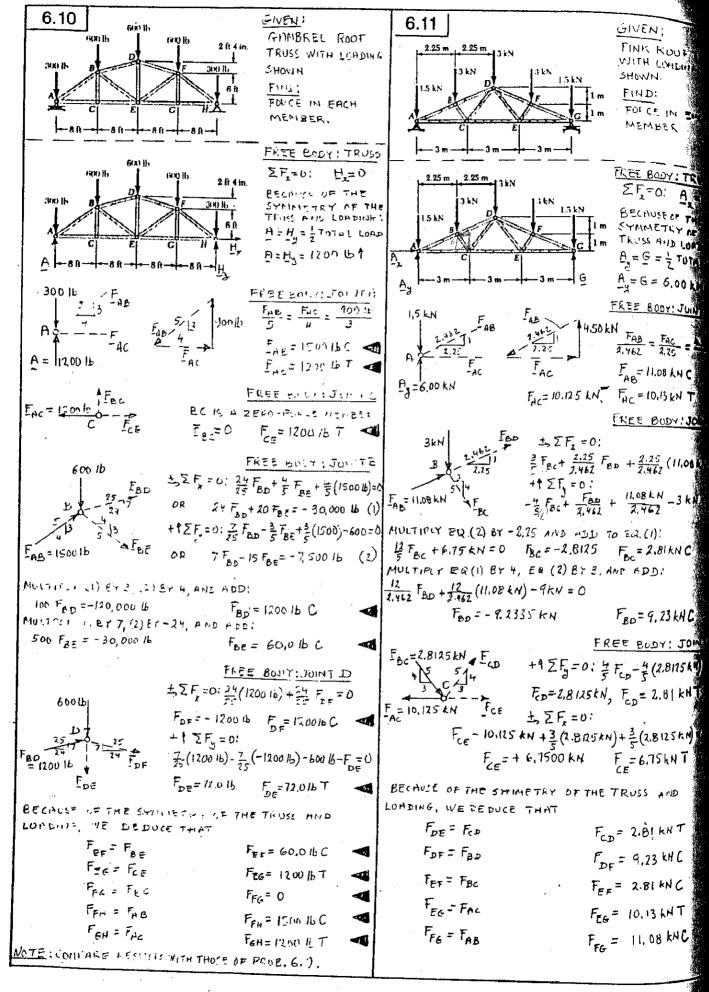
ZΣA = ΣZA: Z(98460 mm²) = 3.300 = 10 mm or Z = 33,5 mm

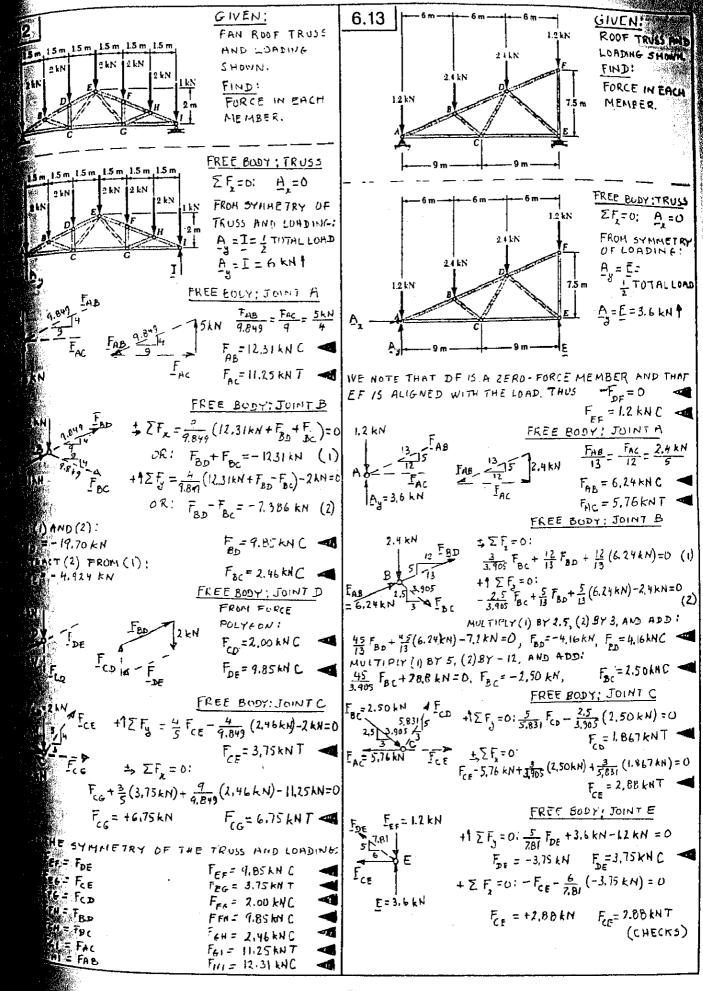


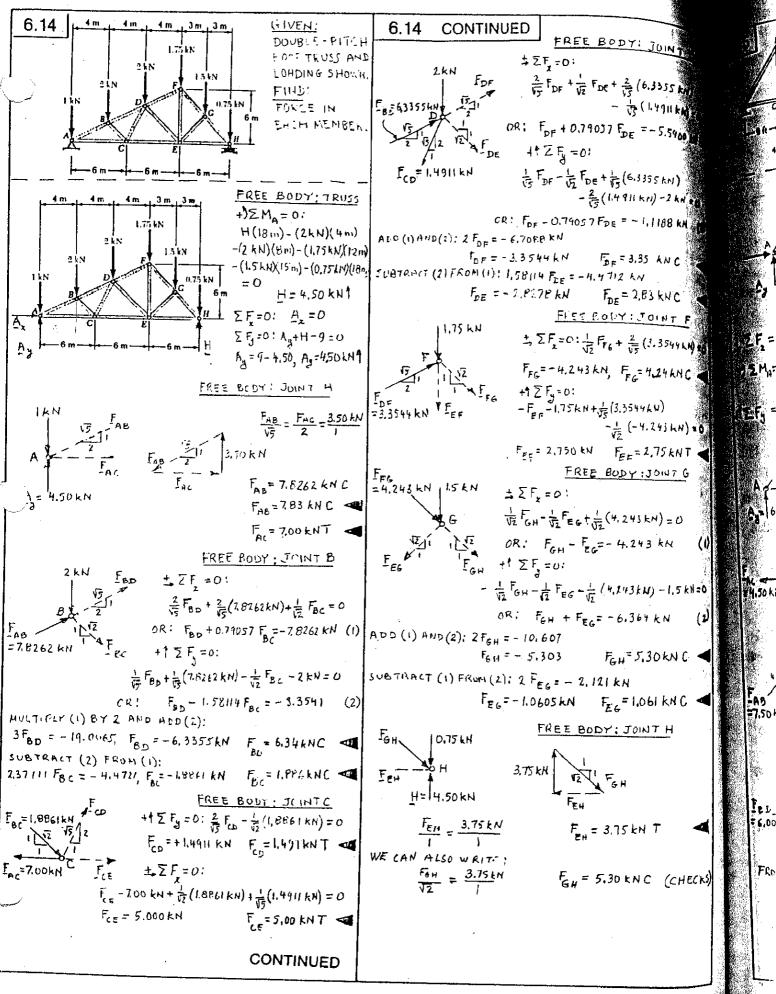


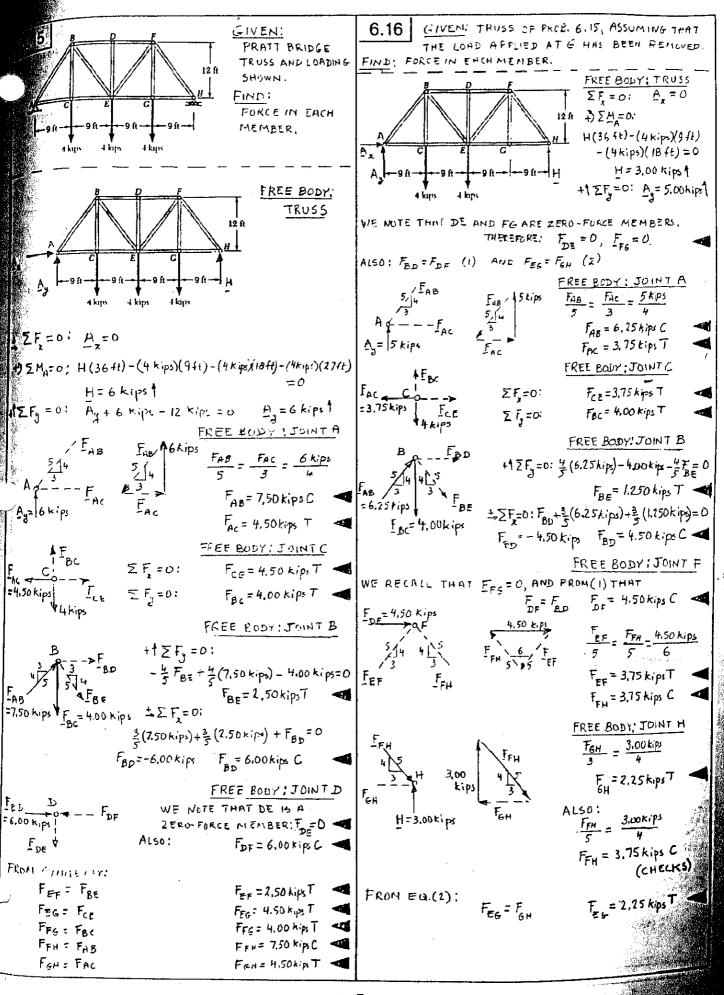


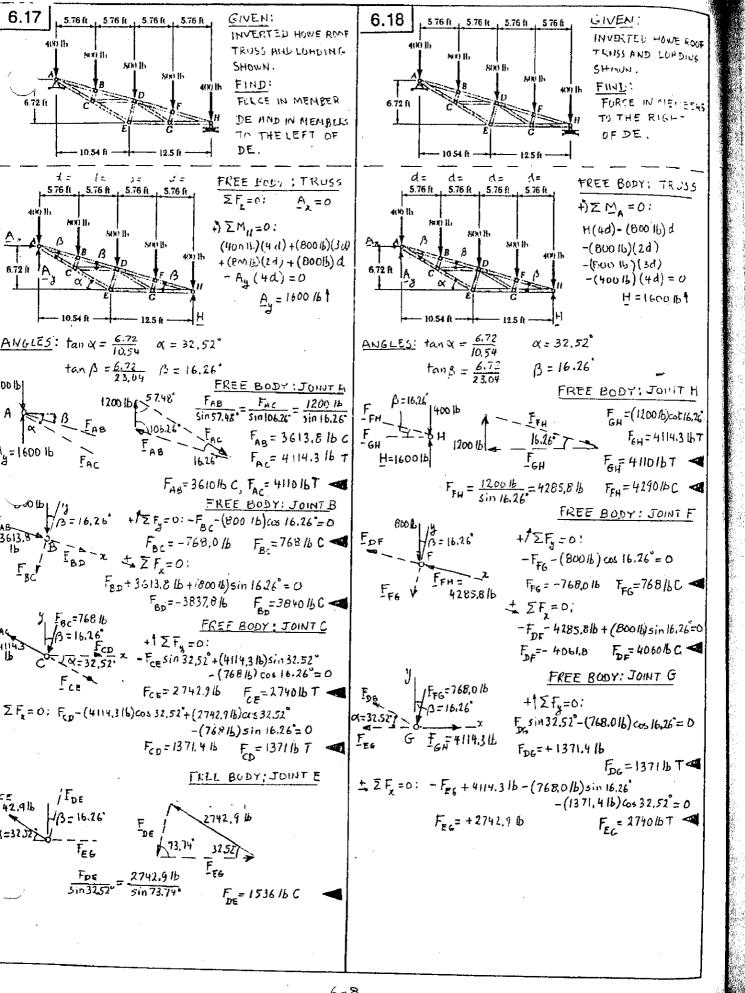












6.1

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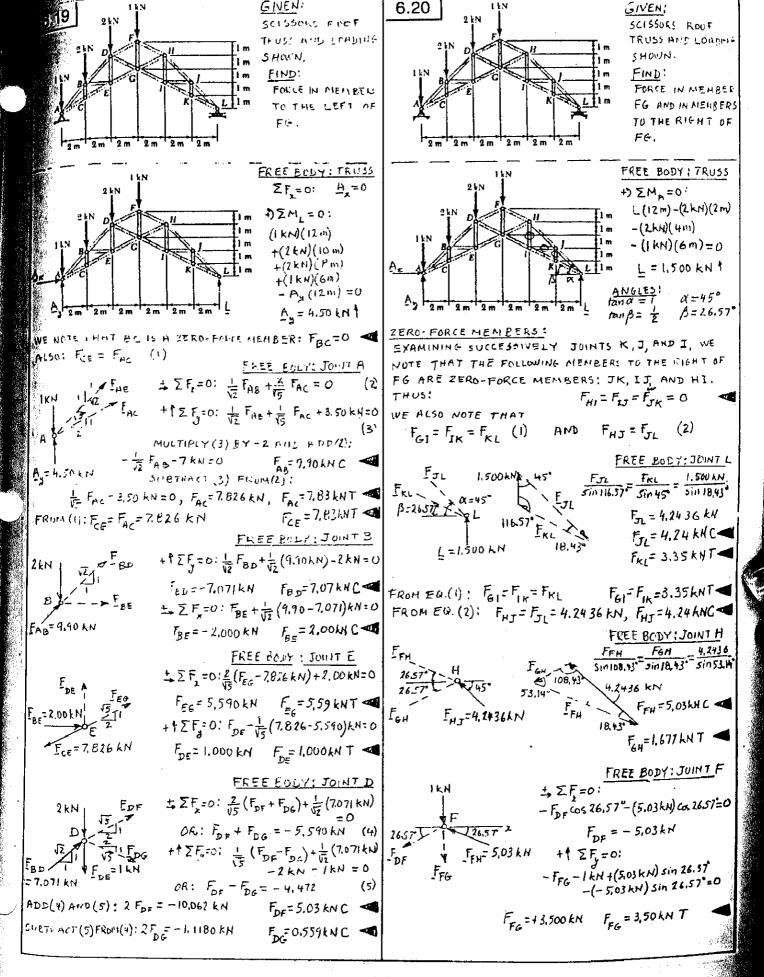
FAR

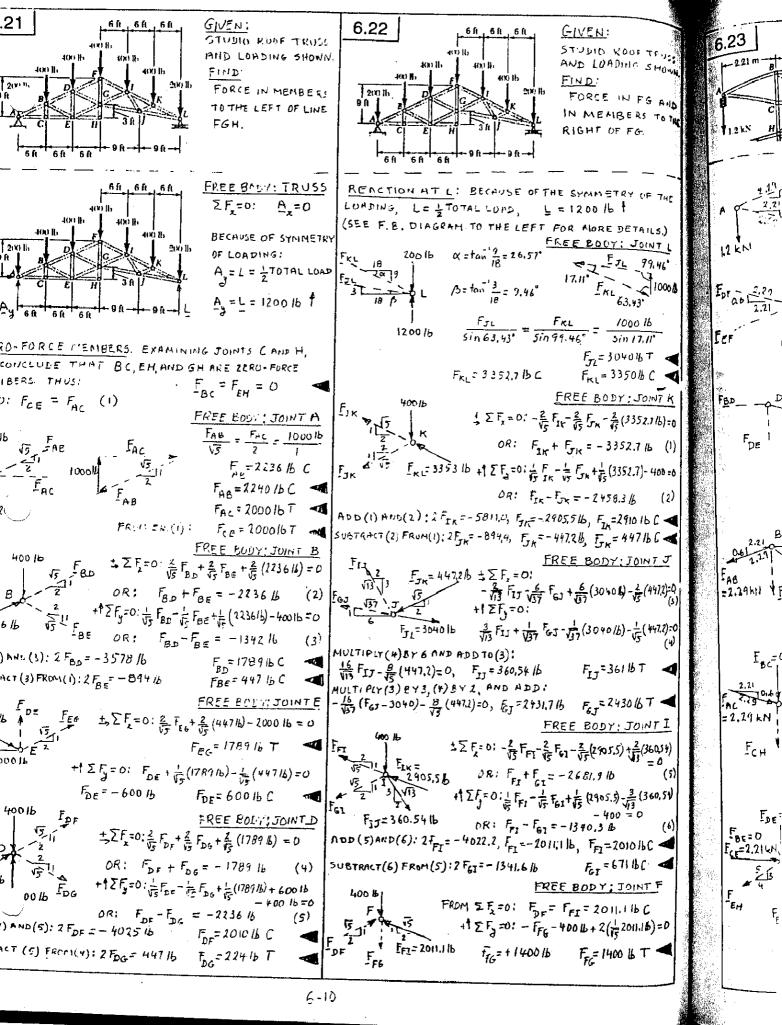
FBE-

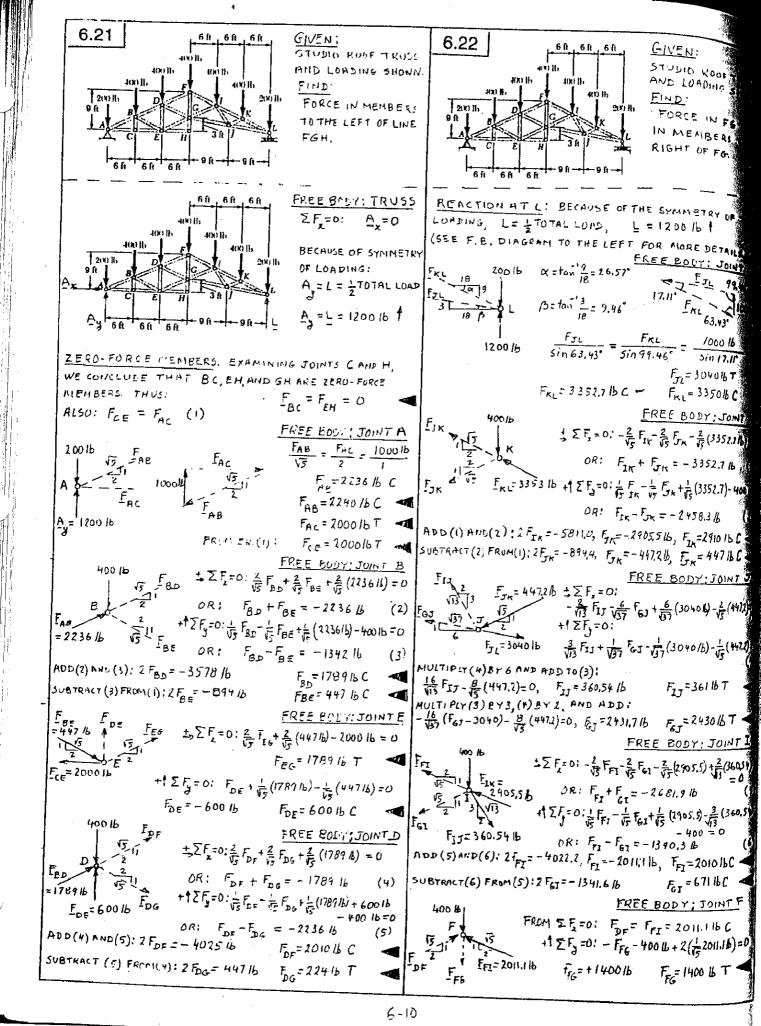
FBE

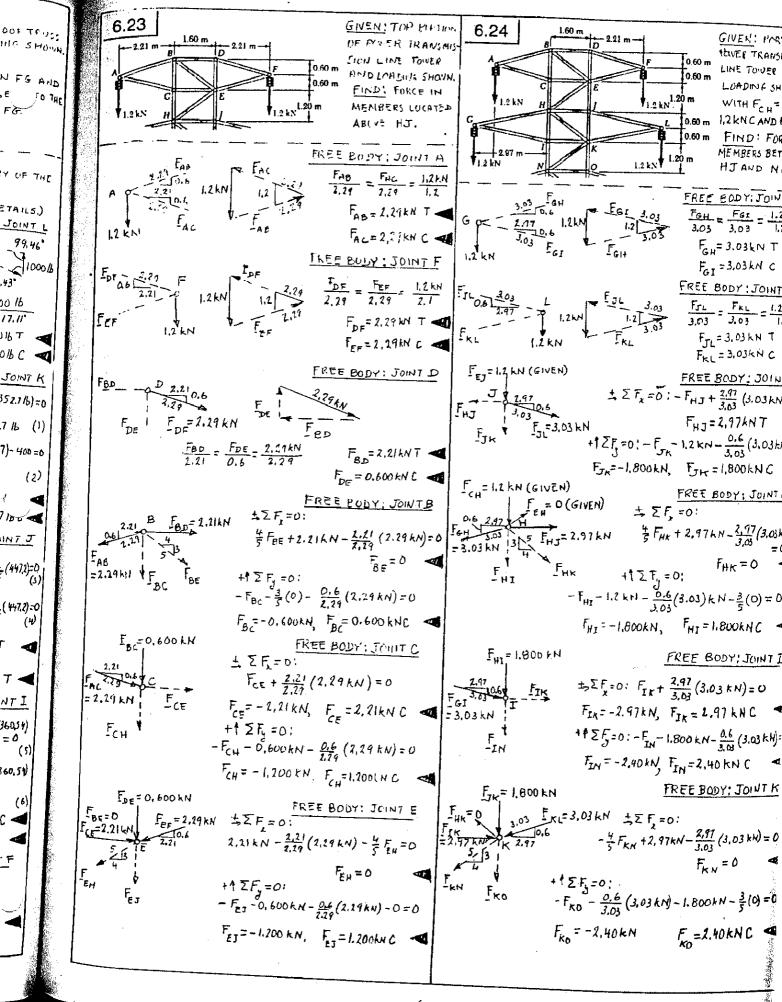
= 7.

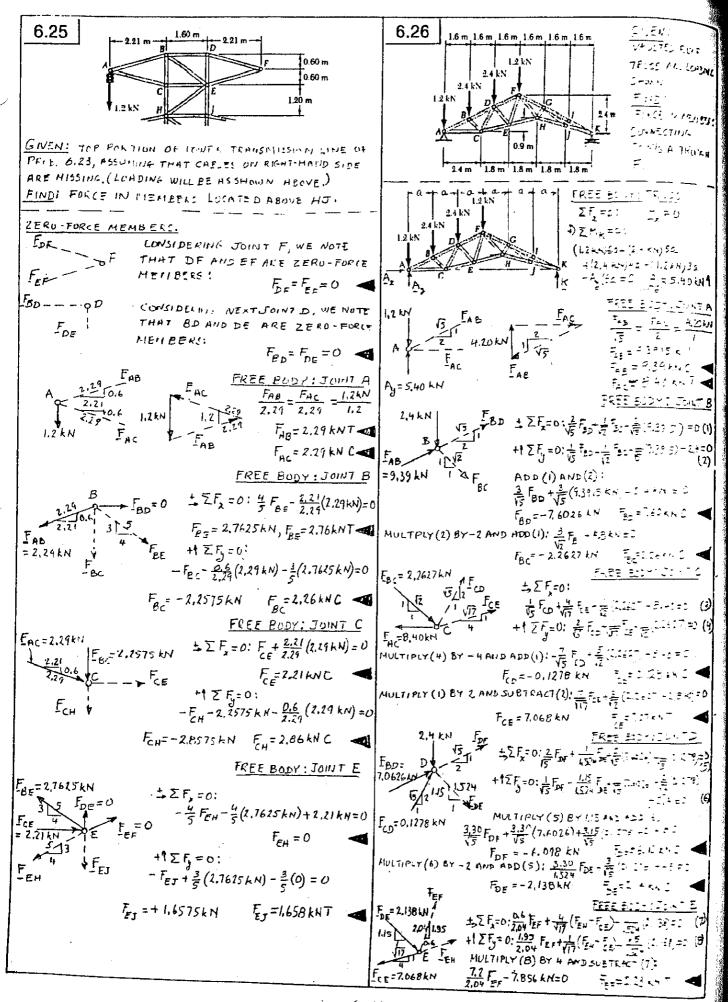
AD

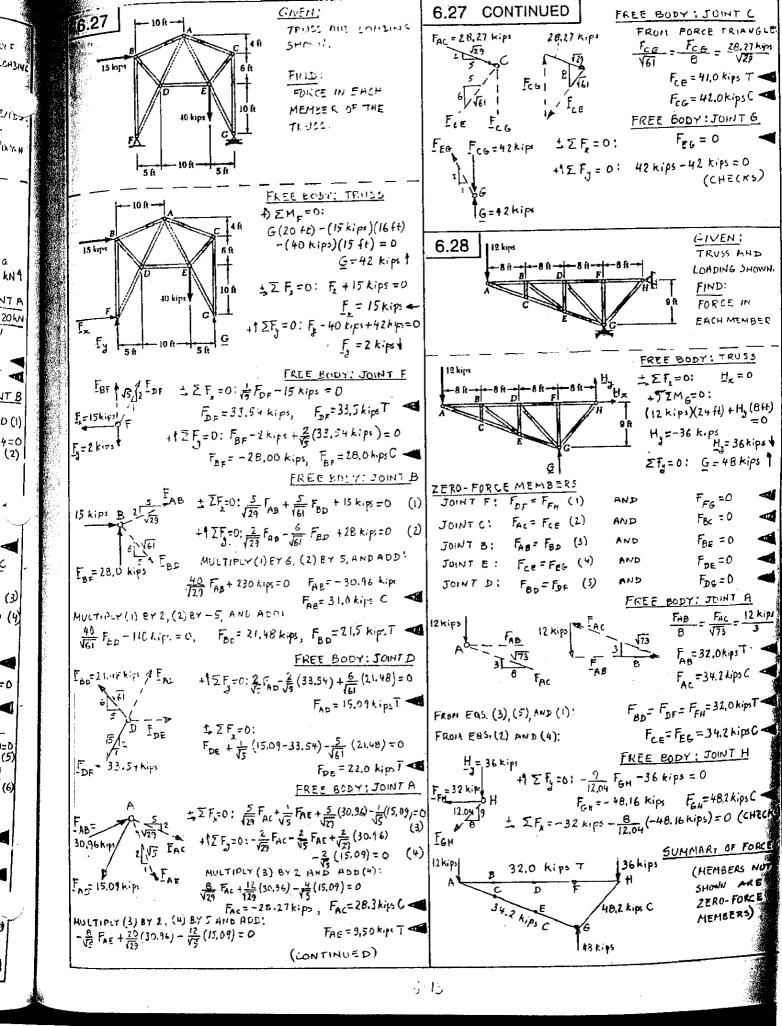








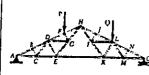




a

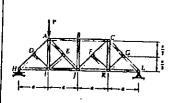
6.29 DETERMINE WHATHER THE TRUMP OF Trobi. 6.31 a, 6.3 [a, And 6 334 ARE BIMPLE 不及けなまたな。

TRUSS OF PROS. 5.310



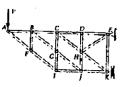
STARTING WITH TURNIGLE ABC AND ADDITION TWO MERICENS AT A TIME, WE OBTHIN TOUTS D. E. G. F. AND H. BUT CHEART GO FILLTHER THUS, THIS TRUS 14 127 A SIMPLE TRUSS

TRUSS OF PROF. 6.32 a



STARTING WITH TRIANGLE HDI AND ADMINE TWO ITHERE AT A TIME, HE CETHIN SUCCES-SIVELY JOINTS A, E, J, MWI P, BUT CANN'I GO FURTHER. THUS, THIS TRUSS IS NOT A SIMPLE TRUSS

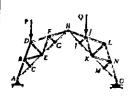
TRUSS OF PROB. 6,33 a



ST WITH WITH THINGLE EHK AND ADDING THE MEMBERS AT A TIME, WE OBTHIN SUCCES. SIVELY JOINTS D. J. C.G. I, B, F, AND A, THEY COMPLETING THE TRUSS. THEREFORE, THIS TRUS IS A SINIPLE TRUS

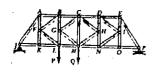
DETERMINE WHETHER THE TRUSPES OF 6.30 PROSLEMS 6.316, 6.326, AND 6.33 & ARE SIMPLE TRUSSES.

TRUSS OF PROB. 6.31 b.



STARTING WITH TRIANGLE ABC AND ADDING TWO MEABERS AT A TIME, WE OBTAIN SUCCES-SIVELY JOINTS E, D, F, G, AND H, PUT CANNOT ON TURTHER THUS, THIS THE 192 IS NOT A SIMPLE TRUSS

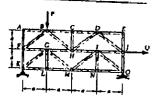
TRUSS OF PLOS. 6.32 b.



STARTING WITH TRIANGLE CGH AND ADDING TWO HENBERS AT A TIME, WE OFTAIN SUCCES-SIVELY JOINTS B.L.F. A.K. J, THEN H, D, N, I, E, O, AND P, THUS COMPLETING THE TRUSS.

THEREFORE, THIS TRUES IS A CHIPLE TRUES

TRUST OF TROP. 6.33 b.



STARTING WITH THINNELS GLM AND ADDING TWO HEARTES AT A TIME WELLTHIN JOINS K AND + BUT CHUMNT CONTINUE, STARTING INSTEAD WITH TEMPORE BCH, WE SETAIN JOINT D BUT CAMECT ONTINUE, THE THE TRUS IS HOT A SIMPLE TRUSS -

6.31

DETERMINE THE ZERO-FORCE MEMBERS IN AF THE THUSSES SHOWN FOR THE SIVEN LUMB

T RU 55(a)

F.B. JOINT B: F6C=0

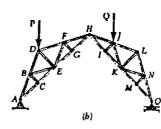
FB: JOINT C: FB: JOINIJ:

FB:JOINT I: F11=0

FB: JUINT N: 1 mu = 0 FB: JOINT M: FLH = D

THE ZERO-POLCE MEMPERS, THEREFORE, ARE

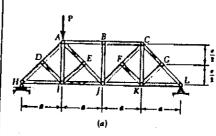
BC, CD, IJ, IL, LM, MN



TRU35 (b) FB: JOINT C: 18c = 0 FB: JOINT B: $F_{BE} = 0$ FB: JOINT G: Fra=o FB: JOINT F: $F_{EF}=0$ TB: JUNT E: FDE = O IB: Javi I: Fir=0 FBIJOINTM: FMN=0

FB:JOINTN: FKN=0 THE ZERO-FURCE MEMBERS, THEREFORE, ARE BC, BE, DE, EF, FG, IJ, KN, MN

6.32 DETERMINE THE ZERO-FORCE HEMBERS IN EACH OF THE TRUSSES SHOWN FOR THE GIVEN LOADING



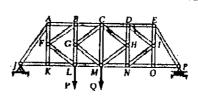
TRUSS (a) FB: JOINT B: FBT = 0

FB: JOINT D: FDI = 0 FB: JOINTE: FET = 0 FB: JONTI: FAT =0

FB: JOINT F: FFK=0 FB: JOINTG: FGK=0

FBIJOINT K: FCK = 0

THE ZERO-FORCE MEMBERS, THEREFORE, ARE AI, BJ, CK, DI, EI, FK, GK



JK077 (P)

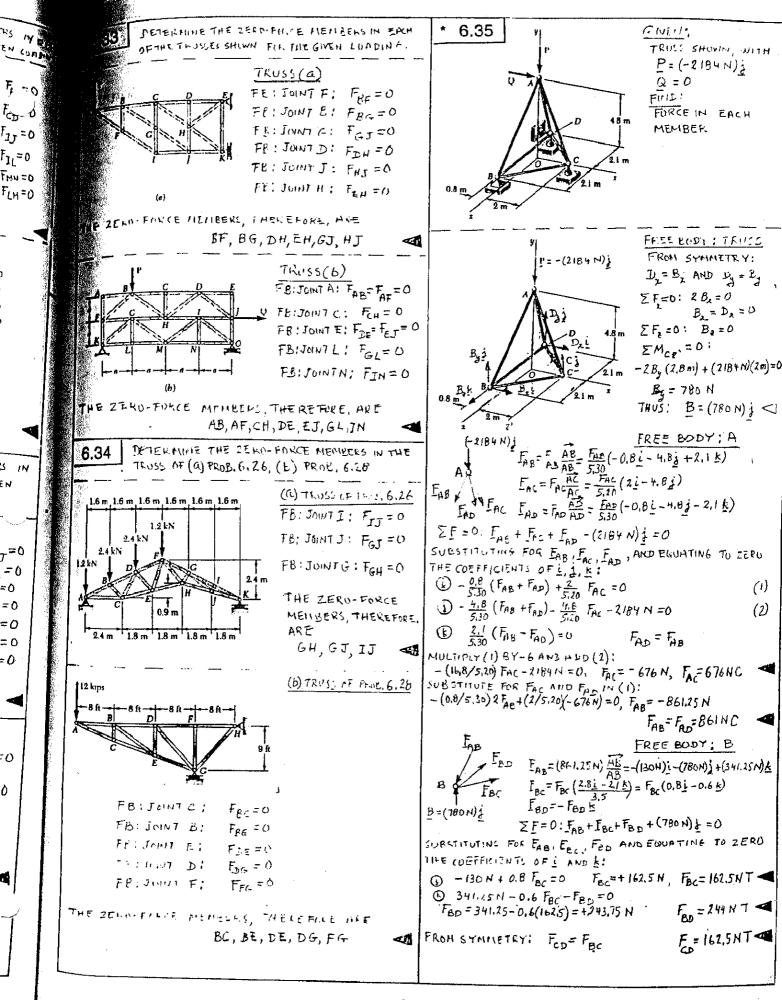
FB : JUINT K: FFK = 0

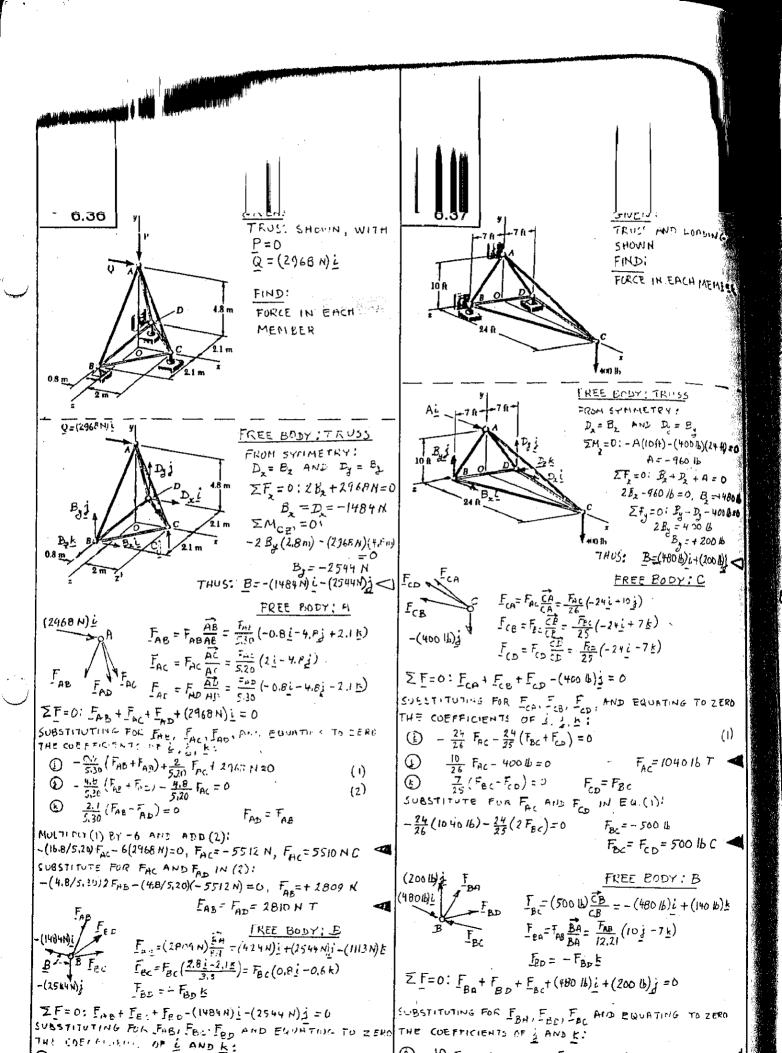
FB: JOINT O: FID=0

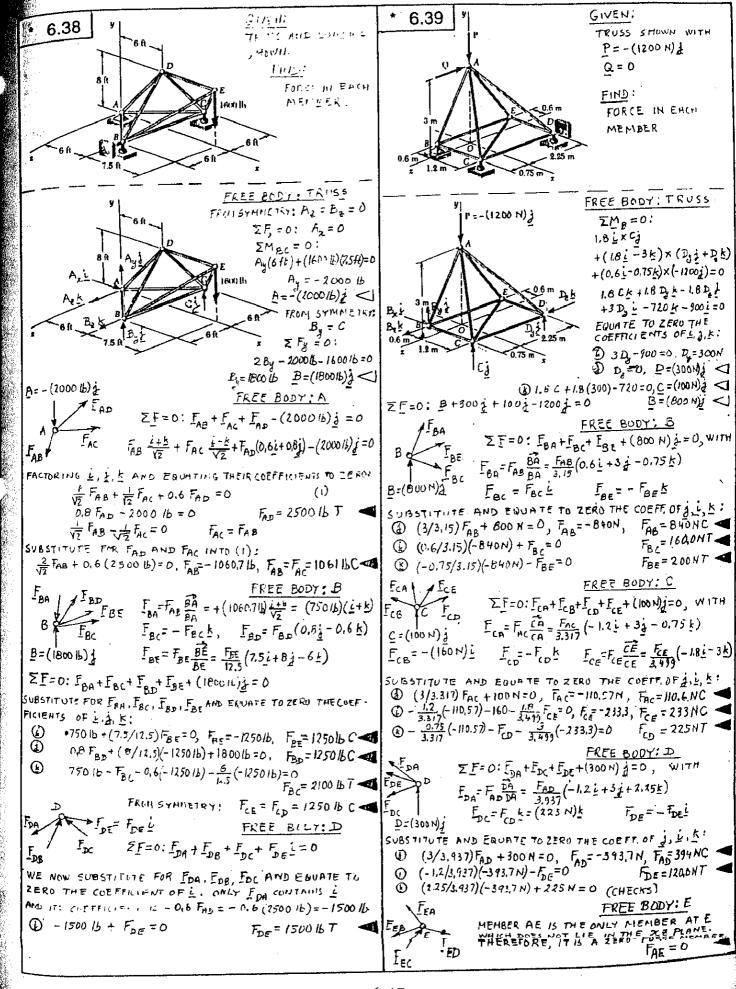
THE ZERD FORCE HENBERS, THEREFORE, ARE FK AND IO

ALL OTHER MEMBERS ARE EITHER IN TENSION OF CONTRESSION .

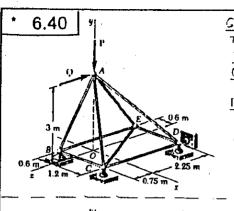
⋖





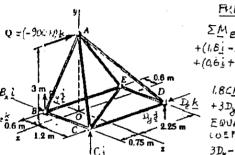


=0



GIVEN :. TRUSS SHOWN WITH P=0 Q=(-90011)}

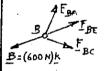
FORCE IN ENCH MEMBER



FREE BODY: TRUSS EMB=0: /ALXC +(1,6; -3K) x(D, ++ D, E) +(0,61+3j-0,75k)x(-90N)k

1.8CK+1.8 D.K-1.8D. +3Dy i +540; -2700 i=0 EQUATE TO ZERO THE LOEFF. OFL, 1, k: 3Dy-1700=0 1=900H -18D +540=0 D=300K 1,8C+181 =0, C=-D, =-900H

THIM: G=-(900N) ; D=1900N) ;+(300 N) K $\Sigma F = 0: B - 900j + 900j + 300k - 900k = 0$ B=(600H)k <



C=-(400H);

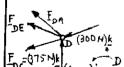
FPLI LODY: B SINCE B IS ALIGNED WITH MENBER BE: FAB = F = D, F = 600NT

ΣF=0: F_{CD}+F+F - (900N)j=0, WITH $F_{CA} = F_{AC} \frac{\overrightarrow{CA}}{\overrightarrow{CA}} = \frac{F_{AC}}{3.317} (-1.2i + 3j - 0.75 k)$ $F_{CD} = -F_{CD} k = F_{CE} - F_{CE} (-1.8i - 6)$

SUBSTITUTE AND EQUATE TO ZERO THE COEFT OF & . L , K:

(3/3.317)FAC-900 N=0, FAE 9951 N. (1) - 1.2 (995.1) - 1.8 FCE =0, FCE= 699.8N, FCE= 700NC

(a) $-\frac{0.75}{3,317}(995.1) - F_{CD} - \frac{3}{3499}(-699.8) = 0$ F = 375NT



THEE BODY: D

Σ (300 N) K Σ F=0: F 36+ F 5+ (375 N) K+ (900 N) 2+ (300 N) E=0 WITH $F_{DA} = \frac{F_{DA}}{9.000} = \frac{F_{AB}}{3.937} (-1.21 + 3.425 k)$ AND $F_{DE} = -F_{DE} \dot{U}$

SUBSTITUTE AND ENGATE TO ZERO THE COEFF OF L. L. K.

(3/3,937) FHE + 900 N = 0, FRE = - 1181.1 N, FAD = 1181 NC

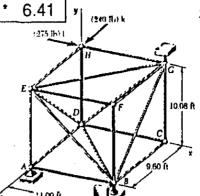
(12/3.937)(-1181,1N)-FDE=0 FDF = 360 N T

(2,25/3,937)(-1181,1H+375 N+300H=0 (CHECKS)



FREE BODY: E MENCER AE IS THE ONLY MEMBER AT E WHICH DOES NOT LIE IN THE XE PLANE, THEREFORE, IT IS A DERO-FORCE, MEMBER.

FAE = 0



GIVEN.

TRUSS AND LOPDING SHIP (a) CHECK THUT THE SIMPLE TRUSS, COMPLETE CONSTRAINED - AND REACTION STATICALLY DETERMINANT (b) FIND:

FORCE IN EIRCH OF THE SIX MEMBERS JOINED

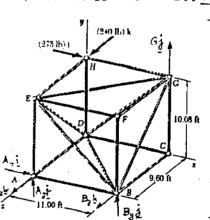
(1) CHECK SIMPLE TRUSS, (1) START WITH TETRAHEDRON BEFG

(2) ADD MEMBER, BD, ED, GD JOINING AT D.

3) ADD MEMBERS BA, DA, EA JOINING AT A. (4) ADD MENDERS DH, EH, GH JOINING AT H

(5) ADD NEMEERS BC, DC, &C JOINING AT C

TRUSS HAS BEEN COMPLETED: IT IS A SIMPLE TRUSS



FREE BODY : TRUSS CHECK CONSTRAINTS AND REALFICHE.

SIX UNKNOWN REACTIONS. OK - MUREOVER SUPPORTS AT A AND B CONSTRAIR TRUSS TO ROTA TE ABOUT AB AND SUPPLAT AT 6 PREVIOUS SUCH A ROTATION . THUS

TRUSS IS COMPLETELY CONSTRAINED AND REACHNI

ARE STATICALLY DETERHANTE

IFTERMINATION OF REACTIONS! ZMA = 0: 11 ix (Ei+ Bk)+(11 i-1.6 k) x 6j+(10.08j-9.6k)x(275i+240k)=0

11 B & - 11 B & + 11 G & + 9.6 G = - (10.08)(275) & + (10.08)(10) i - (9.6)(275) = 0 EQUATE TO ZERO THE COSTS. OF L. T. K.

(E) 9.6 G+ (10.08)(240)=0 G=(-25216)1 <

11 6y + 11 (-252) - (10.08)(275) = 0, By = 504 B

B=(50416)j-(24016)k < EF=0: A+ (504 16) i- (240 16) k-(252 16) j+(275 16) i+(240 16) k=0 A=-(27516) i-(25211) >

ZERD-FORCE MEMBERS

THE DETERMINATION OF THESE MEMBERS WILL FACILITATE

FB: C. NRITING ZF=0, ZF=0, ZF=0 YIELDS F =F=F=0

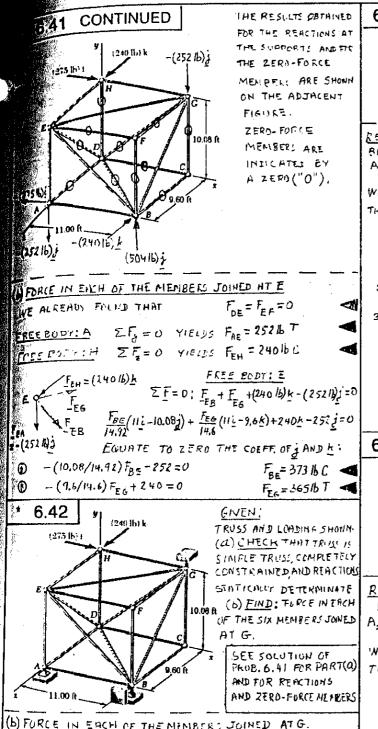
FB: F. WRITING ET=0, ZJ=0, ZF=0 YIELDS FBF=FFF=FF6=0

FB:A: SINCE A=0, WRITING ZF=0 YIELDS

FB:H: WRITING EF = 0 VIELDS FB:D: SINCE FAD FCD = ToH = 0, WE NEED CONSIDER ONLY WEMBERS DB , DE , AND DG .



SINCE FOE IS THE ONLY FORCE NOT CONTAINED IN PLANE BOG, IT MUST BE ZERO. SIMILAR REASONINGS SHOW THAT THE OTHER TWO FBD=FDE=FDE=0 FORCES ARE ALSO ZERO (CONTINUED)



(b) FURCE IN EACH OF THE MEMBERS JOINED AT G. WE ALREADY KNOW (SEE FIG. AT TOP OF PHGE) THAT FCG=FDG=FFG= 0 FREE BUDY: H ZFx=0 YIELD: FGH= 27516 C

FREE BODY : G EGH = (275/6) L $\Sigma F = 0$: $F_{6B} + F_{6F} + (27516)i - (25216)j = 0$ FBG (-10,081+9.61) ¥ G=-(25216);i + 275 i - 252 i = 0

ERIMITE TO SEND THE COEFF, OF L. S. K.

(11/14.6) FEG +275 = 0 😰 - (10,08/13,92) F_{B 6}- 252=0

(9.6/13.92)(~348)+(9.6/14.6)(369)=0

FEG = 365 /b T -FBG=348/6C (CHECKS)

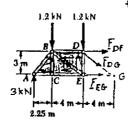
6.43 1.2 PN 1.2 kN 1.2 kN 1.2 kN

GIVEN' MAHSARD RUOF TRUSS AND LOADING SHOWN. FIND: FORCE IN MENTERS DF. DG, AND E4.

REACTIONS AT SUPPORTS

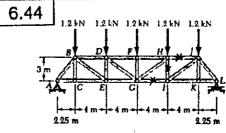
BECHUSE OF THE SYMMETRY OF THE TRUSS AND LOHDING A = 0, A = L = = (TOTAL LOAD) = = (6kN) A = L = 3kn 1

WE PASS A SECTION THROUGH DF DG AND EG AND USE THE FREE BODT SHOWN



+3 EMc=0: (1.2 kN)(8m) + (1.2 kN)(4m) -(3KN)(10.25m)-FDF (3m)=0 FDF = -5.45 KM, FDF = 5,45 KN C +1 E Fy = 0: 3kN-1.2kN-1.2kN-3 FDG=0 FDG=+1.00kN, FDG=1.00kN7 ◀

+) \(\Sigma M_D = 0 \) (1.2 kN)(4m)-(3 kN)(6,25m)+FEG(3m)=0 FEG=+4.65kN, FEG= 4.65kNT ◀

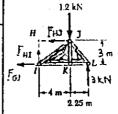


GNEN: MANSARD ROOF TRUSS AND LOADING SHOWN FIND: FORCE IN MEMBERS GI HI AND HJ

REACTIONS AT SUPPORTS

BECAUSE OF THE SYMMETRY OF THE TRUSS AND LUADING, A = 0, A = L= = (TOTHE LOAD) = = (6 KM) A=L=3 KN1

WE PHSS A SECTION THROUGH GI, HI AND HI AND USE THE FREE BODY SHOWN



♪코MH = 0: $(3kN)(6,25m) - (1.2kN)(4m) - F_{G1}(3m) = 0$

FGt = + 4.65 kH, FGI = 4.65 kNT +1 ZF.=0:

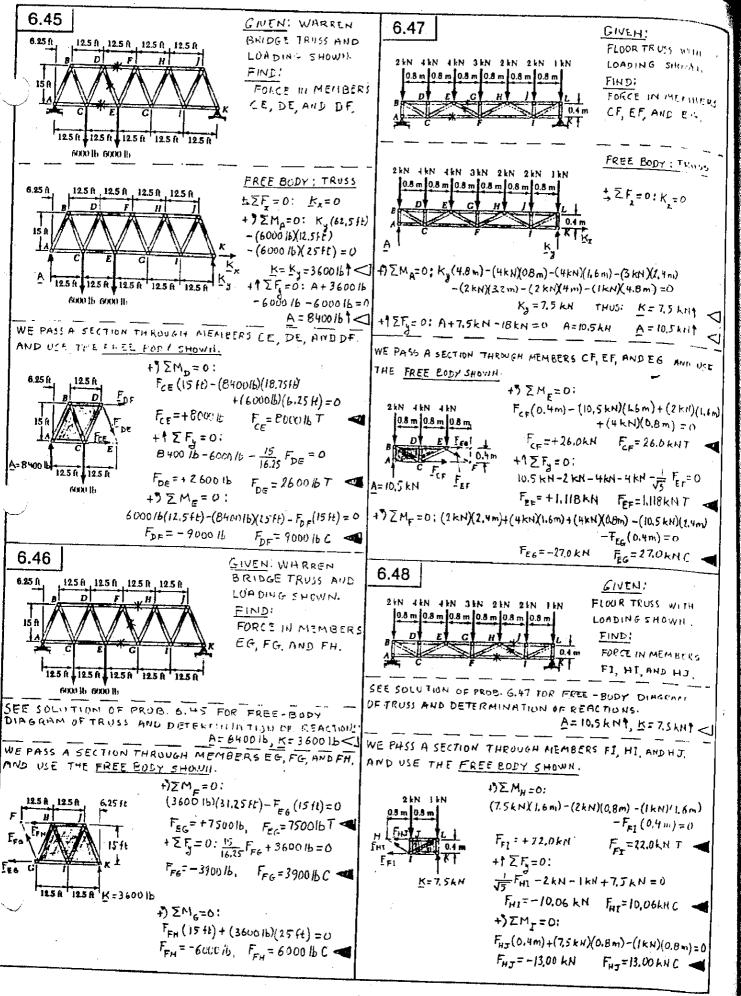
FHI - 1.2 KN +3 KN = 0

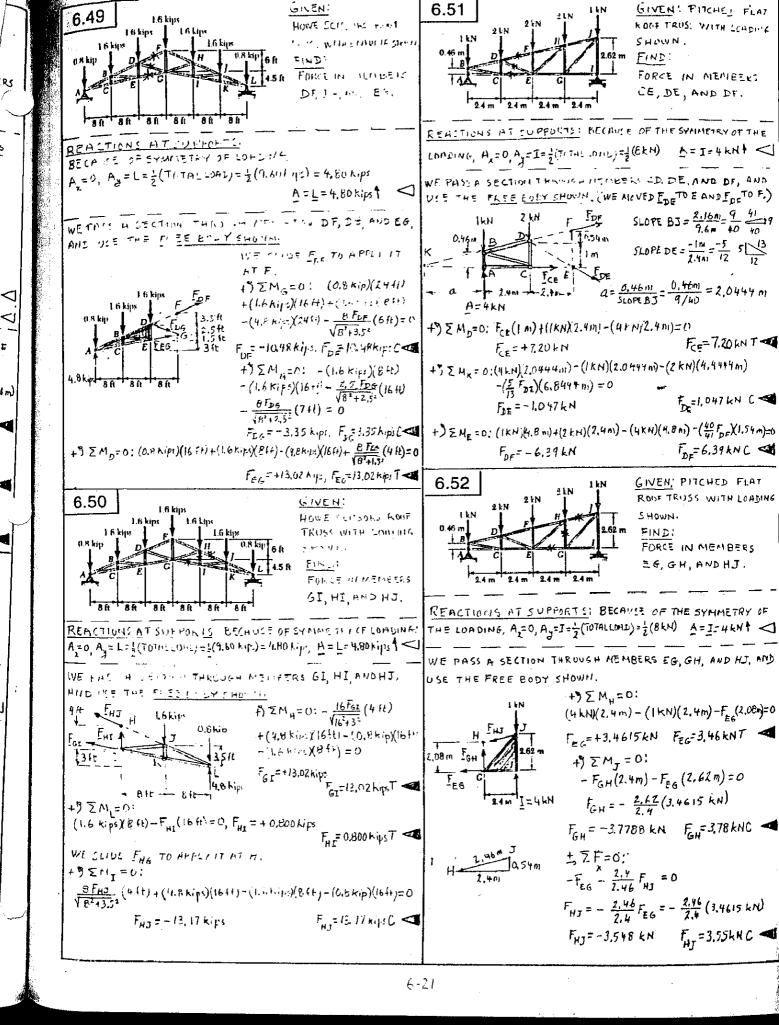
FH:= 1.80 KN [4 FH1 = - 1.80kH

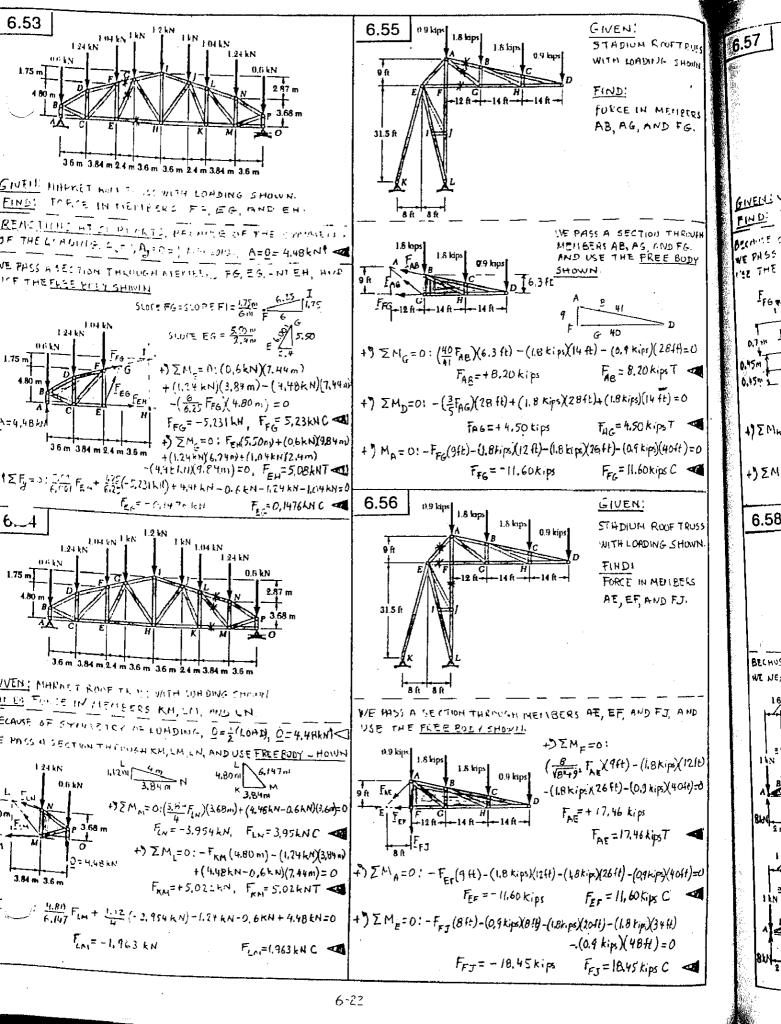
4) 2 M = 0:

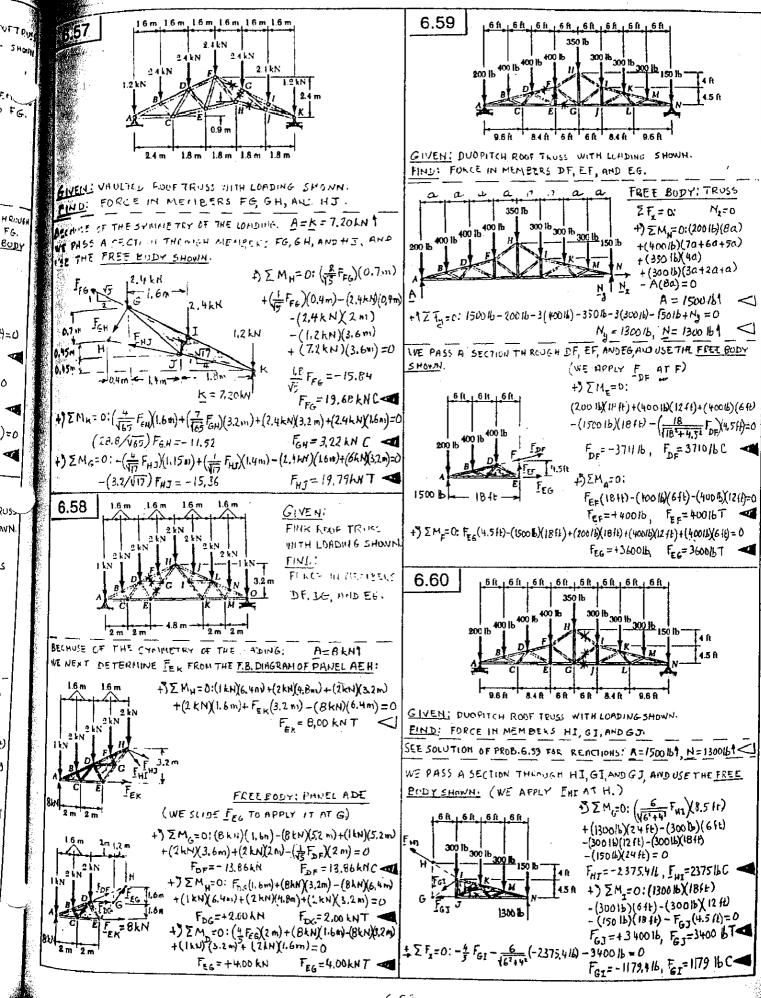
FHO (3m) - (1.2 KN)(4m) + (3 KN)(6,25 m)=0 FHJ = 4.65 KNC FHJ = - 4.65 KN

CHECK: 12 Fx = 4.65 kN - 4.65 kN = 0









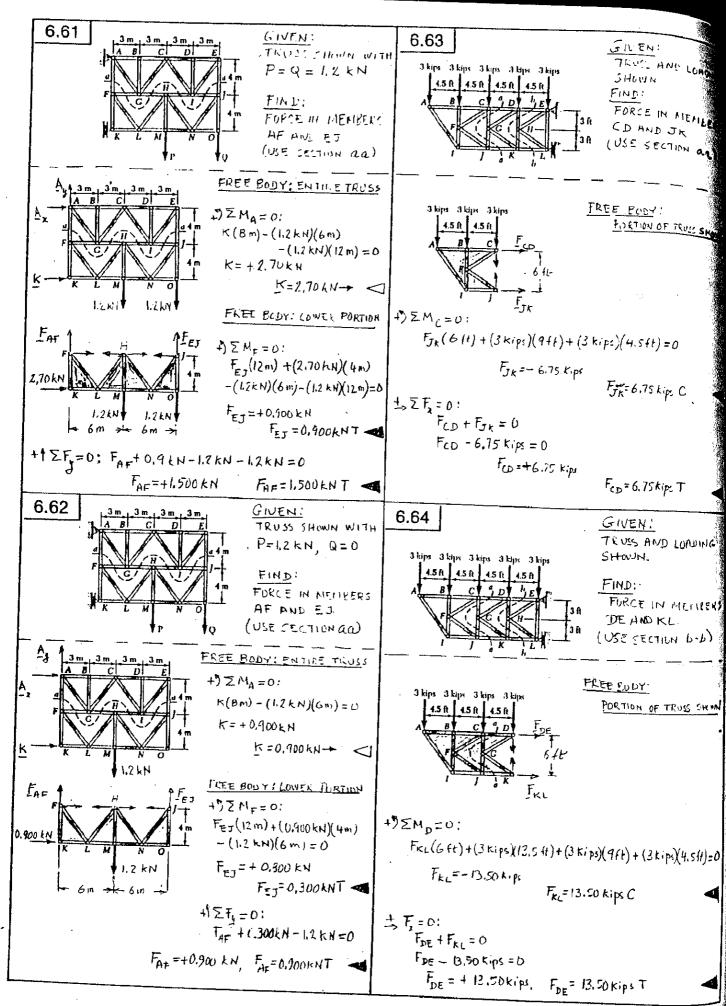
FG.

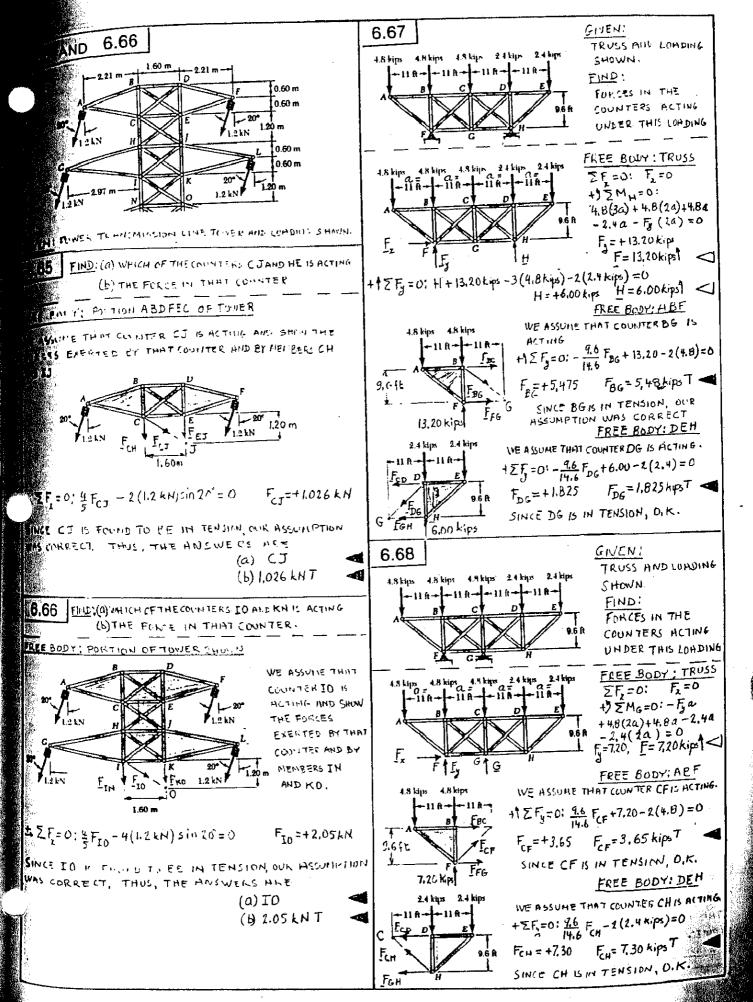
Вору

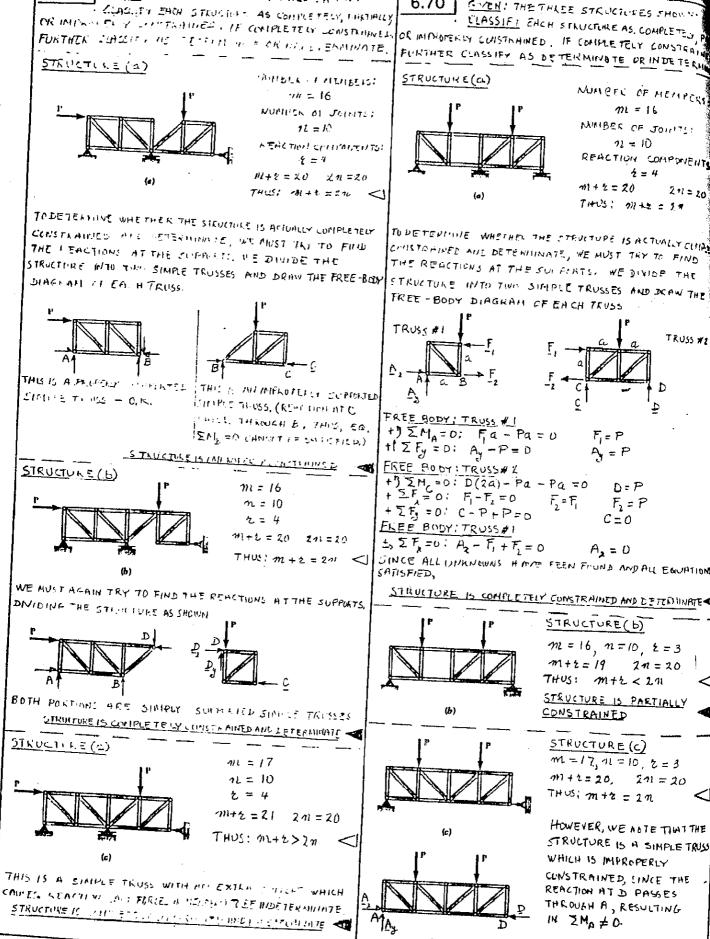
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FURTHER CLASSIFY AS DETERMINATE OR INDETERM NUMBER OF MEMPERS 11 = 16 MINIBER OF JOINTS! 12 = 10 REACTION COMPONENTS 2 = 4 111+2=20 211 = 203 THUS: 11/4 = 3# TO DETENUINE WHETHER THE STRUCTUPE IS ACTUALLY CHIP CHISTORINED AND DETERMINATE, WE MUST TRY TO FIND FREE - BODY DIAGRAH OF EACH TRUSS TRUSS #2 +) Inc=0: D(2a) - Pa - Pa =0 + 5 F = 0: F1-F2 =0 F2=F D=P F₂ = F₁ $F_2 = P$ SINCE ALL DIKNOWNS HAVE FEEN FRUND AND ALL EQUATION STRUCTURE IS COMPLETELY CONSTRAINED AND DETERTINATE STRUCTURE (b) m = 16, n = 10, 2 = 3 m+2=19 21 = 20 THUS: M+2 < 211 STRUCTURE IS PARTIALLY CONSTRAINED STRUCTURE (c) M=17, 11=10, 2=3 $m + t = 20, \quad 2m = 20$ THUS; m+2 = 2n HOWEVER, WE NOTE THAT THE STRUCTURE IS A SIMPLE TRUS WHICH IS IMPROPERLY

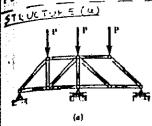
CONSTRAINED, SINCE THE REACTION AT D PASSES

THROUGH A, RESULTING

IN ZMA + O.

STRUCTURE IS IMPROPERLY CONSTRAINED

SIVEN: THE THEEE HITE KINDS SHOWN. CLASS IF EACH STRUCTURE AS COMPLETELY, PARTIALLY. PARTIN MARGOERLY CONSTRAINED, IF CHIPLETE Y CONSTRAINED, PURTHER CLASSIEY AS DETERMINATE ME INCETEL THINATE.



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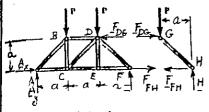
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THE

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NUMBER OF MEMERICS 717 = 12 MUMBER OF JOINTS: n = 6REACTION COLUMNERIALS 2=4 111+2=16 22=16 THUS: 11+2 = 212

TO DETERMINE WHETHER THE STUNTILLE & ACTUALLY COMPLETELY CONSTITUINED AND DETERMINATE, WE MUST TRY TO FIND THE RENCTIONS AT THE SUPPLICTS. INTE PASS A SECTION AND DETAIN THE SIMPLE TRUS! ABODEF AND MINEER GH.



FREE BIDY : GH 1) Z M = 0: Pa - FDG a = 0 FDG = P ZF,=0: FFH=FDG=P 2F = 0. H= P

FREE BODY: TRUCE ABODE F 15 F2 = 0; A2 + FFH - FDG = 0 Ax+ P-P=0 +9 2MA=0! F(3A)+FA-PA-P(21)=0 +1 ZF = 0: Ay - P-P+3 P=0

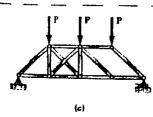
SINCE ALL ONKHOURS HAVE FELH FRANCE AND ALL EDURTIONS

STRUCTURE IS CUMPLETELY CONSTRUINTS AND DETERMINATE

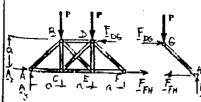
STRUCTURE (b) m= 13, n=8, 2=4 71+2=17 21=16 THU: M+2>29

MOLEOVER, WE NOTE THAT STRUCTURE IS A SINPLE TRUSS CPOLLOW LETTERING TO CONSTRUCT)

STRUCTURE IS CONSTRUCTED AND INDETERMINATE



STRUCTURE (c) 71 = 13, 71=8, 2=3 m+6=16 2m=16 すけいら つりナと ニ 2ル WE PASS A SECTION AND C'BTAIN THE TWO FREE BODIES SHOUN.



FREE BUDY : FG WE RECALL FROM PARTICO) FDG= FN = H=7

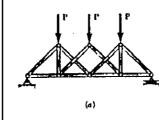
FREE BODY: ABLDET 2ΣHA = Inga - Pa-P(20) = Pa - 3Fa = 2Pa ≠0 THIS ENUMBER ON EQUITION IS NOT SATISFIED THEREFOR STRUCTURE IS IMPROPERLY SUNSTRAINED

6.72

HINEN: THE THREE STRUCTURES SHOUN ELASSIFY EHCH STRUCTURE AS COMPLETELY.

PARTIALITY OR INTPROFFER IT CONTRAINED, IF LOTIFIED TILLY CONTRAINED, FURTHER CLASSIFY AS DETERMINATE OK INSETERMINATE

STRULTURE (a)



NUMBER OF MEMBERS! nl = 12NUMBER OF JOINTS: n=8 REACTION CLASSON WESTS! そころ 211:16 1911 = 15 THUS: 11)+E < 21

STRUCTURE IS PART HELY CONSTRAINED

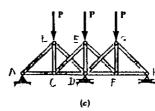
STRUCTURE (b)

m = 13, 11 = 82=3 211 = 16 111+2= 16 THU: 11112=12

TO VERIFY THAT THE STRUCTURE IS ACTUMLLY COMPLETELY CONSTRAINED AND DETERMINATE, WE DESERVE THAT IT IS A SIMPLE TRUSS (FOLLOW LETTERING TO CHECK TAIS) AND THAT IT IS SIMPLY SUPPORTED BY A PIN-AND-BRACKET AND A ROLLER. THUS!

STRULTURE IS COMPLETELY CONSTRAINED AND DETERHINATE.

STRUCTUPE (C)



2=4 11112=17 211=16 THUS: M+2>21

m = 13, n=8

STRUCTURE IS COMPLETELY CONSTRAINED AND IN DETERMINATE

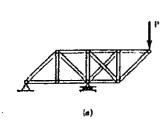
THIS RESULT CAN BE VERITIED BY OBSERVING THAT THE STRUCTURE IS A SIMPLE TRUSS (FOLLOW LETTERING TO CHECK THIS), THEREFIXE RIGID, AND THAT ITS SUPPERTS INVOLVE 4 UNKNOWNS.

6.73

GIVEN: THE THESE STEVETURES SHOWN CLASSIET EACH STRUCTURE AS CONTRASTRE

PARTHALLY, OR IMPROPERLY CONSTRAINED. IF CONFICTELY CONSTRAINED, FURTHER CLASSIFY AS DETERMINATE OR IMPETERMINATE

STRUCTURE (a)



NUMBER OF HEMBERS: ME = 14

NUMBER OF JOINTS:

m = e

RENCTION SOMPONENTS:

t=3 m+t=17 2m=16

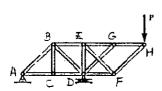
(.te.)

TAUS: かりャンノ2カ

STRUCTURE IS COMPLETELY COUSTRAINED AND INDETERMINATE

THIS RESULT CAN BE VERITIED BY OBSERVING THAT THE STRUCTURE IS AN OVERRIGID TRUSS (ONE EXTRA MENIBER),

STRUCTURE(b)



m=13, m=8 2=3

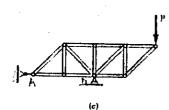
m+2=16 2n=16

THUL: m+t = 2m

WE OBSERVE THAT THE STRUCTURE IS A SIMPLE TRUSS (FOLLOW LETTERING TO CHECK THIS) AND THAT IT IS DIMPLY SUPPORTED BY A PIN AID BRACKET AND A RULLER, THUS:

STRUCTURE IS COMPLETELY CONSTRAINED AND DETERMINATE

STRUCTURE(4)



m = 13, m = 8

と=3

1111 = 16 211 = 16

7HOS: 11+2=212 <1

WE OBSERVE THAT THE STRUCTURE IS A SIMPLE TRUSS, BUT THAT IT IS IMPROPERLY CONSTRAINED, SINCE THE RENCTION AT A PASSES THRUGH THE SUPPORT D THE EQUATION EM =0, THEFEFORE, IS NOT SATISFIED.

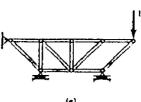
THUS: STRUCTURE IS IMPROPERLY CONSTRAINED

6.74

GIVEN: THE THREE STRUCTURES THON CLASSIFY EACH STRUCTURE AS CORNER

CONSTRAINED, FUNTHER CLASSIFY AS DETERMINED OF CHIPTER CLASSIFY AS DETERMINED OF MATER

STEUCTION Elaj

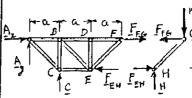


NUMBER OF MEMBERS: m=12NUMBER OF JOHNS: nt=8REACTION COMMUNICIAL

2=4 111+2=16 2n

711+2 = 16 2n=16 THUE: 181+2 = 2n

TO VEKIF, WHETHER THE INT THE STRUCTURE IS CONFIDENT CONSTRAINED AND DETERMINENTE, WE PASS A SECTION AND CONSIDER THE PECE BODIES ABODEF (A SIMPLE TRUSS) AND



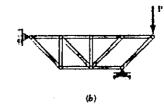
FREE GODY: GH +) ZMH=0: FGA-PA FF6 = P 5 ZF=0: FEH-FF6

FREE BODY: TRUSK ARCNEF +) $2M_{H}=0$: $Ca-F_{EH}a=0$ $C=F_{EH}=P$ $\pm 2F_{s}=0$: $A_{s}+F_{FG}-F_{EH}=0$ $H_{s}=0$ $1^{2}2F_{y}=0$: $A_{y}+C=0$ $A_{y}=-C=-P$

SINCE ALL UNIKHOWNS HAVE REEN FOUND AND ALL EQUATIONS

STRUCTURE IS CONFLETELY CONSTUAINED AND DETERMINATE

STRUCTURE (b)

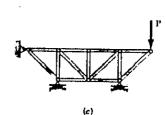


m = 12, n = 8 t = 3m + t = 15 2n = 16

THUS: m+2 <211

STRUCTURE IS PARTIALLY
CONSTRAINED

STRUCTURE (C)



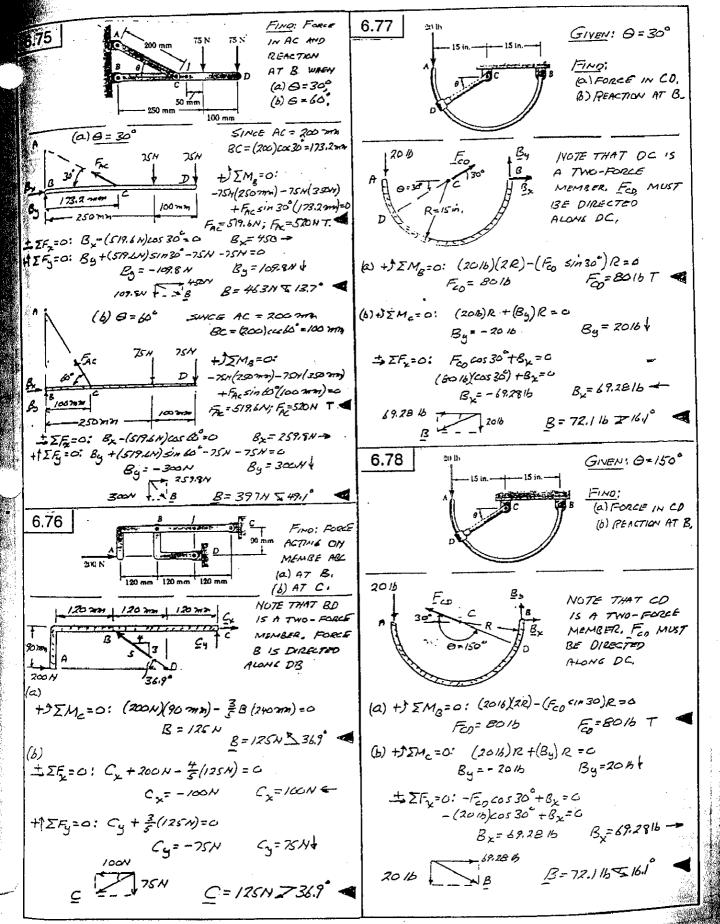
M1=13 , 11=8

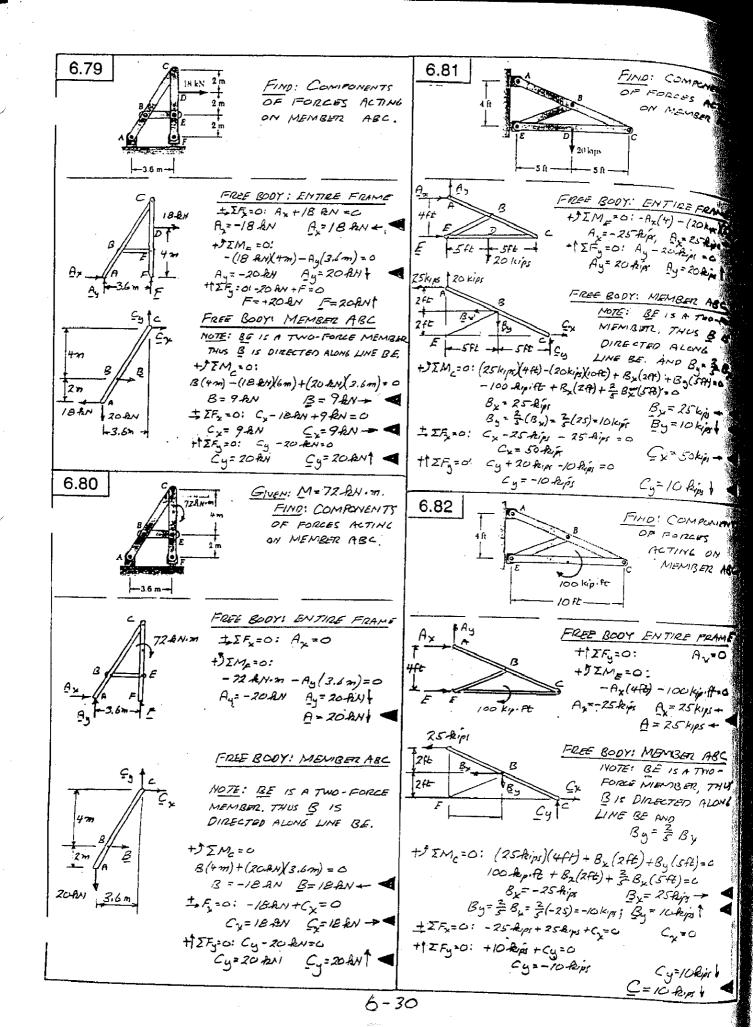
カリーシェ 17 2 カ = 16

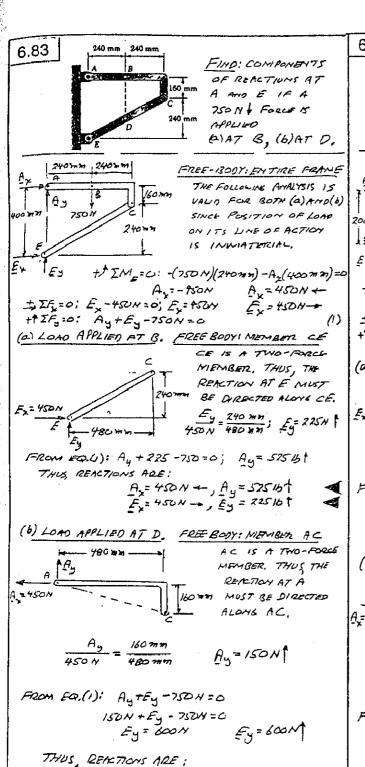
THUS: 11+2 > 271

WE OBSERVE THAT THE CTPUCTURE IS A SIMPLE TRUSS AND THAT ITS SUPPORTS INVOLVE 4 UNKNOWNS (INSTEAD FR. 3 FOR A SIMPLY SUPPORTED TRUSS), THUS

STRUCTURE IS CONTRETELY CONTRAINED AND INDETERMINATE

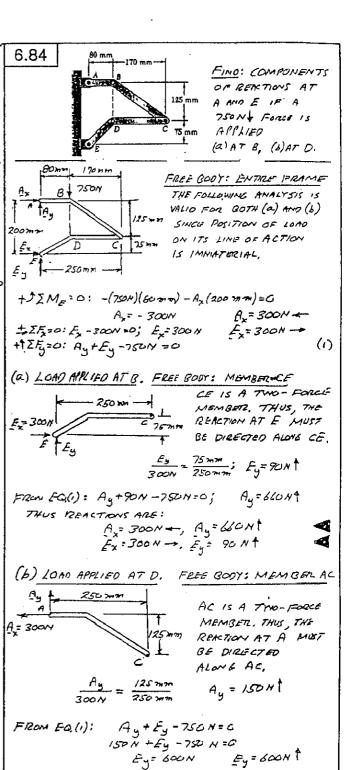




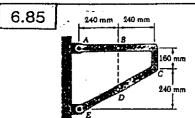


A = 450 N - Ay = 150 N

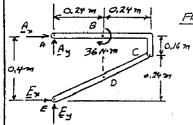
Ex= 450 N->, Ey = 6001



THIS, IZEACTIONS ARE: A = 300N-, Ay= 150Nt Ex= 300N →, Ey= 600N+



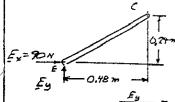
FIND: COMPONENTS OF REALTIONS AT A my E IF A 36 Nim 2 COUPLE IS APPLIED (a) AT B, (b) AT D.



FREE BODY: ENTIRE FRAME THE FOLLOWING ONEM. AMALYSIS IS YAUD FOR BOTH (a) AND (b) SINCE THE POINT OF APPLICATION OF THE COURT IS IMMATERIAL.

+3
$$IM_{E}=0$$
: $-36Nm-A_{2}(a+m)=0$
 $A_{2}=-90N$
 $A_{2}=90N-4$
 $\pm \Sigma F_{2}=0$: $-90+E_{2}=0$
 $E_{2}=90N$
 $E_{2}=90N$
 $E_{3}=90N-3$
 $E_{4}=90N-3$
(1)

(a) COUPLE APPLIED AT B. FREEBODY: MEMBER CE



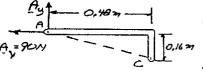
AC IS A TWO-FORCE NIEMBER. THUS, THE REACTION AT E MUST BE DIRECTED ALONG EC.

From ED(): Ay + 45N =0 Ay = - 45N

Ay = 4546

THUS, REACTIONS ARE

(b) COUPLE APPLIED AT D. FREE BODY: MEMBER AC

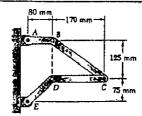


AC IS A TWO-FORES MEMBER. THUS, THE REACTION AT A MUST BE DIRECTED ALONS AC.

FROM EQ(1): Ay+Ey=0 30N+Ey=0 Ey=-30N

THUS, REACTIONS ARE:

6.86

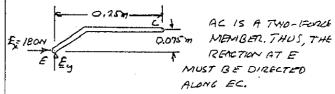


FIND: COMPONENTS OF REACTIONS AT A AND E IF A 36 N.m) COUPLE IS APPLIED (a) AT B, (b) AT D.

0.172 FREE BOOY: ENIRE FRAME THE FOLLOWING ANALYSIS IS VALID 0.12537 0.20 FOR BOTH (a) AVO (b) SINCE THE PONT OF C 1 0,075 => APPLICATION OF THE COUPLE IS IMMATERIAL, 0.25

+) EM=0: -36N·m -Ax(0.2m)=0 Ax=-180H Ax=180N -+ IF =0: -180N+Fx=0 Ex = 1804 Ex=180N-Ay+ Ey =0 ††Σ*F*₃=0:

(a) COUPLE APPLIED AT B. FREE BODY: MEMBER CE

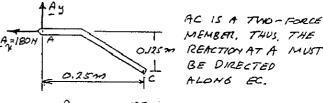


$$\frac{E_g}{180N} = \frac{0.075m}{0.25m} \qquad E_g = 54N$$

FROM EQ.(1): Ay + 54 N=0 Ay = -54N THUS, REACTIONS ARE

Ax= 180N-, Ay=54N+ Ex= 180N->, Ey= 544

(6) CCUPLE APPLIED AT D. FREE BODY MEMBER AL

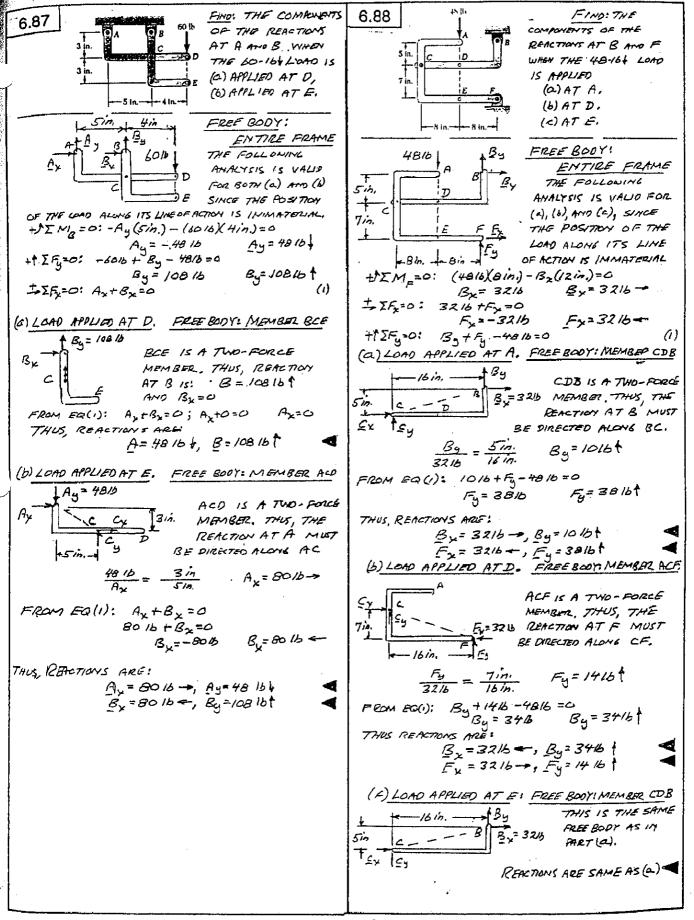


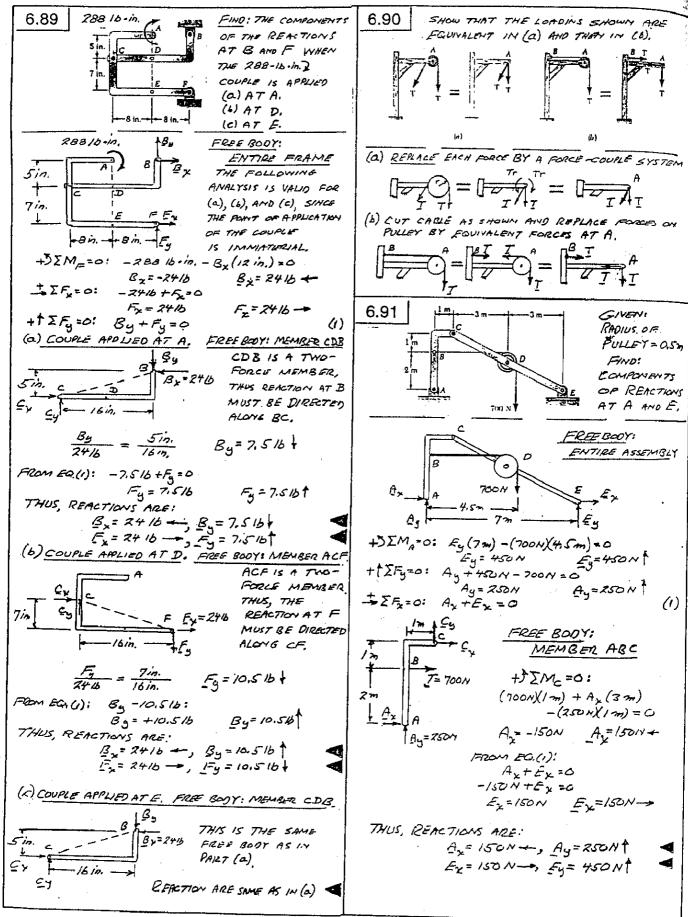
From Ea,(1):

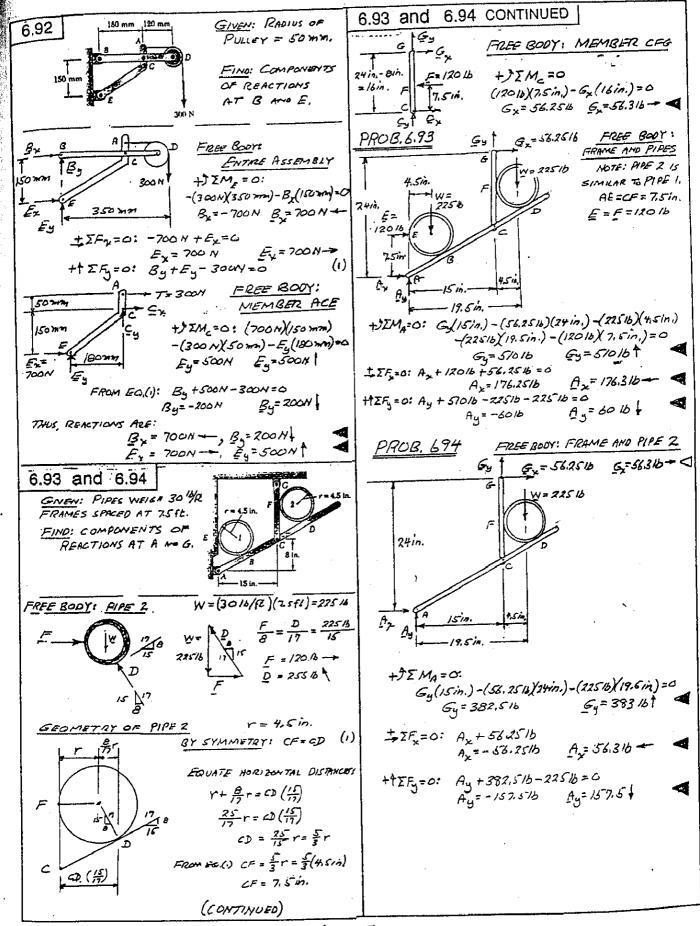
Ay+ Ey = 6 90N + Ex = 0 Ey=-901

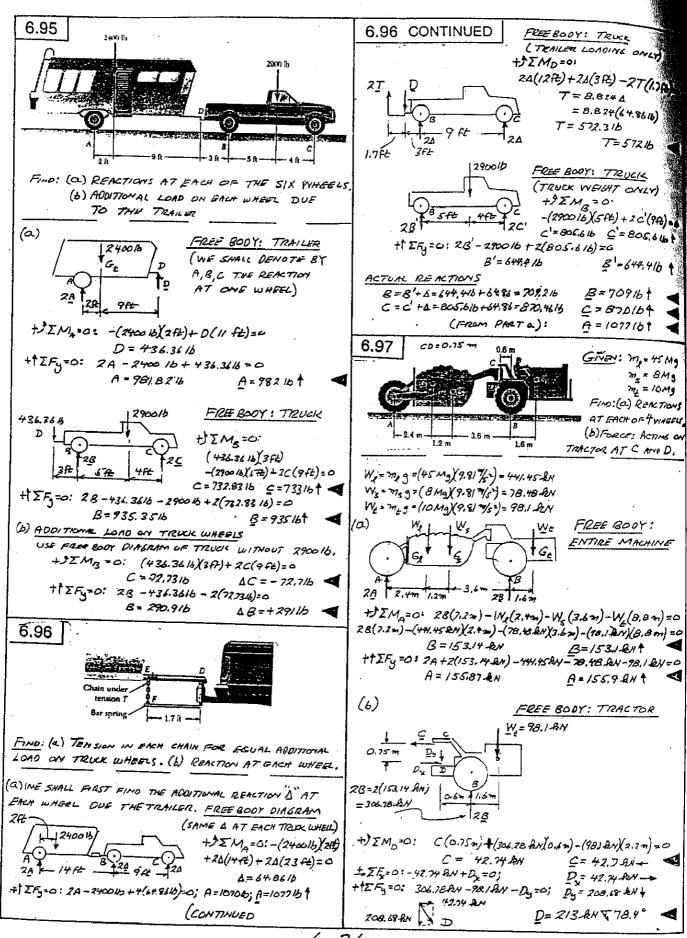
Ey= 90M

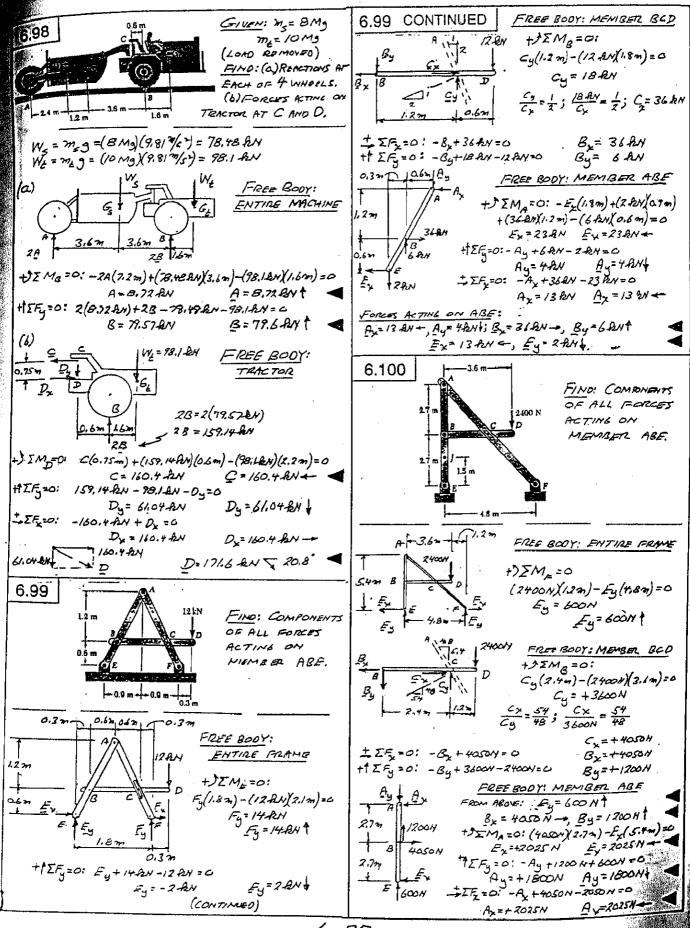
THUS, REACTIONS ARE

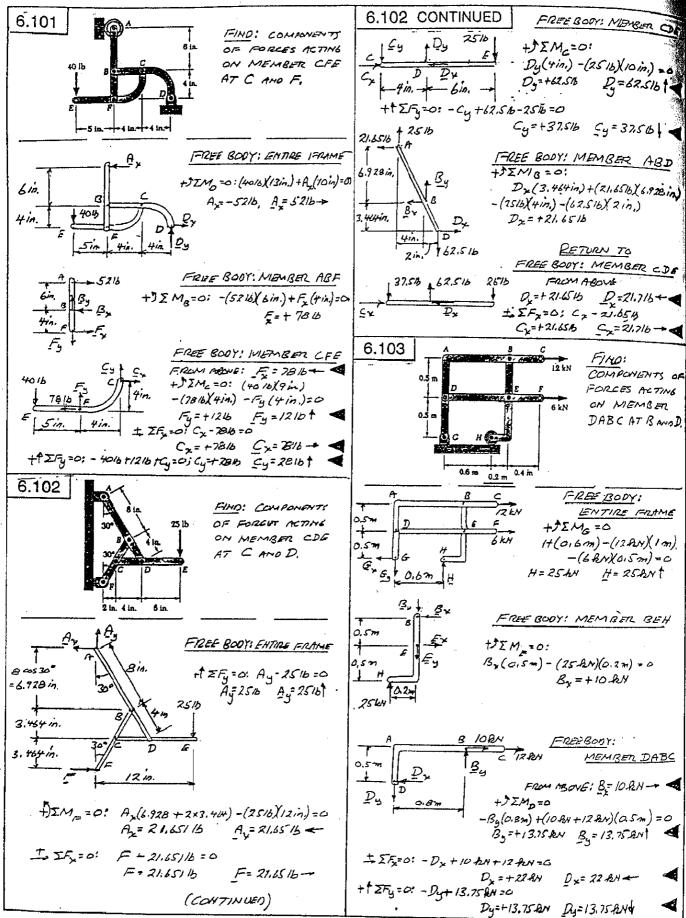


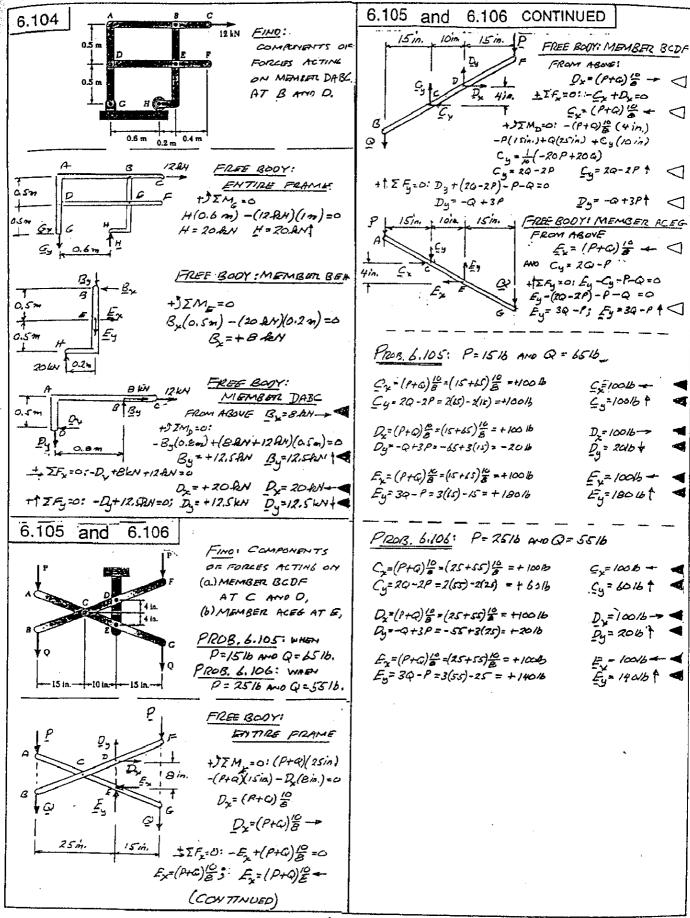


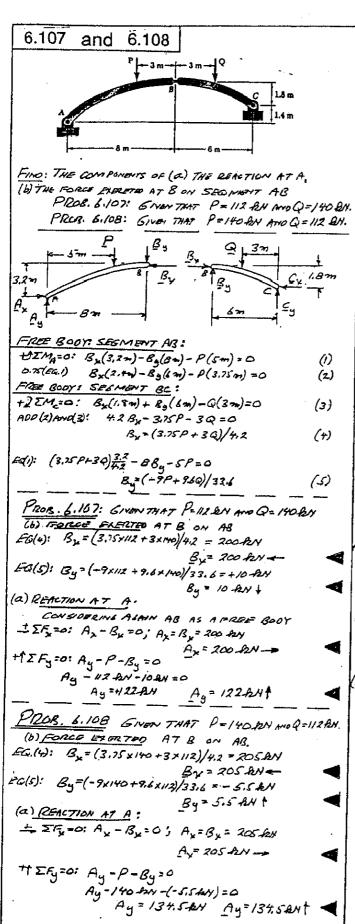


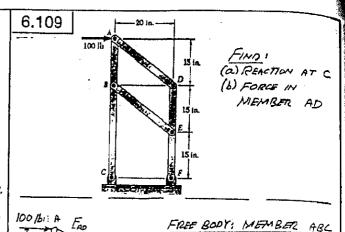








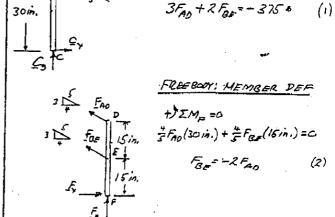




FREE BODY: MEMBER ABL

+) IM = 0: + (100 16) (45 in.)

+ \$ FAO (45in) + \$ F (30in) = 0



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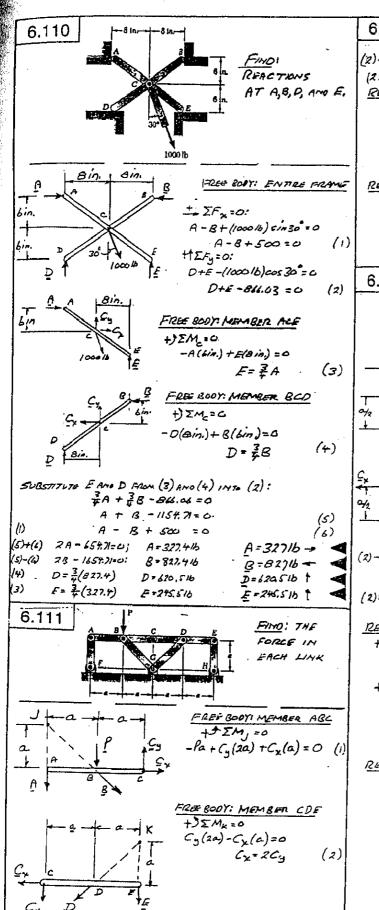
(a) 5185717675 FROM (2) INTO (1) 3 FAD +2 (-2FAD) = -37516 -Fo=+375B FAO = 375 16 Len,

Fa= - 2 FAD = - 2(3751) (2) FBF= - 750 16 F8 = 750 1b comp.

(6) RETURN TO FREE GODY OF MEMBER AGE + IFx =0: C2+10016+ \$ FAD+ \$ FBE = G Cx + 100 + \$ (375) + \$ (-750) =0 C= 20016-Cx = +200/6

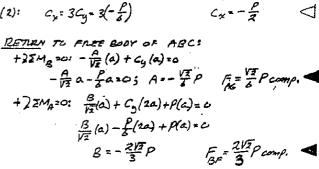
+ 1 IF = 0: Cy - 3 Fm - 3 Fm = 0 Cy - 3(375) - 3-(-75)=0 Cy= -225 B Cy=225 16 1

X = 48.37° C = 301.015 C=30116 V 48.4°

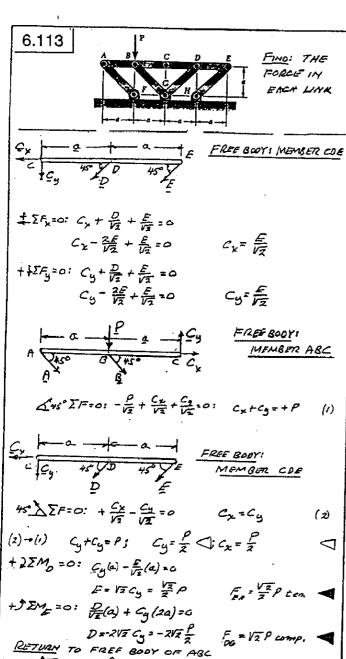


ı)

6.111 CONTINUED Cy=+ 1/2 P Cy=+ 1/2 P ✓ (2)-(1): -Pa+(1(2a)+2Cy(a)=0; Cx = 2 Cy = 2(4P); RETURN TO FREE BOOT OF ABC! + IFx=01 Cx+ 1/2 B=0; 1P+ 12 B=0; B=- 1/2 F= P comp. +) IM8=0; Cy(a)+A(a) = Ly(a) + H(a) P = +Pa+Aa=0; A=-4 FAF = P comp. RETURN TO FREE BOOT OF COE: + ΣFx=01 - Cx-1/2 D=0 +) IM0=01 Cy(0)-E(0)=0 \$Pa-Fa=0; E= +; FEF 4 ton. ◀ 6.112 FIND: THE FORCE IN EACH LINK. Cy 64 FREE BOOY! MEMBER ABC 0= UMZ (+ $C_{y}(\frac{1}{2}a) + C_{y}(\frac{3}{4}a) + P(\frac{2}{1}) = 0$ Cx +3Cy+P=0 (1) FREE BOOT: MEMBER CDE + 3 5Mx = 0 Cx(学)-Cy(学)=0 Cx=+3C4 (z)(2)-(1): +3Cy+3Cy+P=0: $C_g = -\frac{P}{B}$ 6 Cy + P = 0



RETURN TO FREEBOOT OF COE
+)
$$\sum M_{c} = 0$$
: $\frac{D}{V_{2}}(a) - C_{y}(2a) = 0$
 $\frac{D}{V_{2}}(a) - (-\frac{\rho}{a})(2a) = 0$
 $0 = -\frac{\sqrt{2}}{3}P$ $\int_{D_{1}} = \frac{\sqrt{2}}{3}P comp$.
+) $\sum M_{0} = 0$: $\int_{V_{2}} (a) + C_{y}(a) = 0$
 $\int_{V_{2}} (a) - \int_{0}^{\rho} (a) = 0$
 $\int_{V_{2}} (a) - \int_{0}^{\rho} (a) = 0$



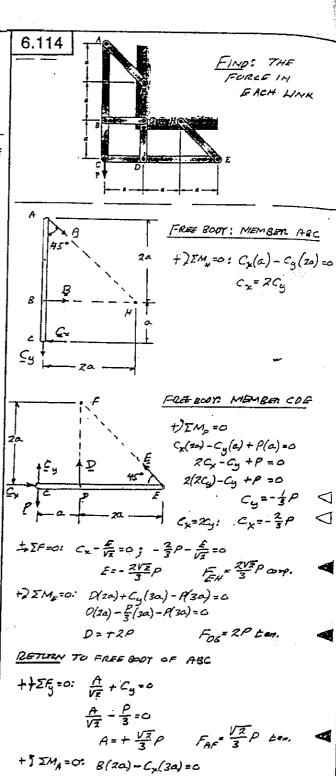
+) IMg=0: A(a) + Cy(a)

+) EM = 0: $\frac{B}{\sqrt{2}}a + Pa - Cy(2a) = C$

B=V2(P- = 2)=0

A= VZ Cy = \frac{\sqrt{2}}{2}P \quad F_{AF} \frac{\sqrt{2}}{2}P \ten.

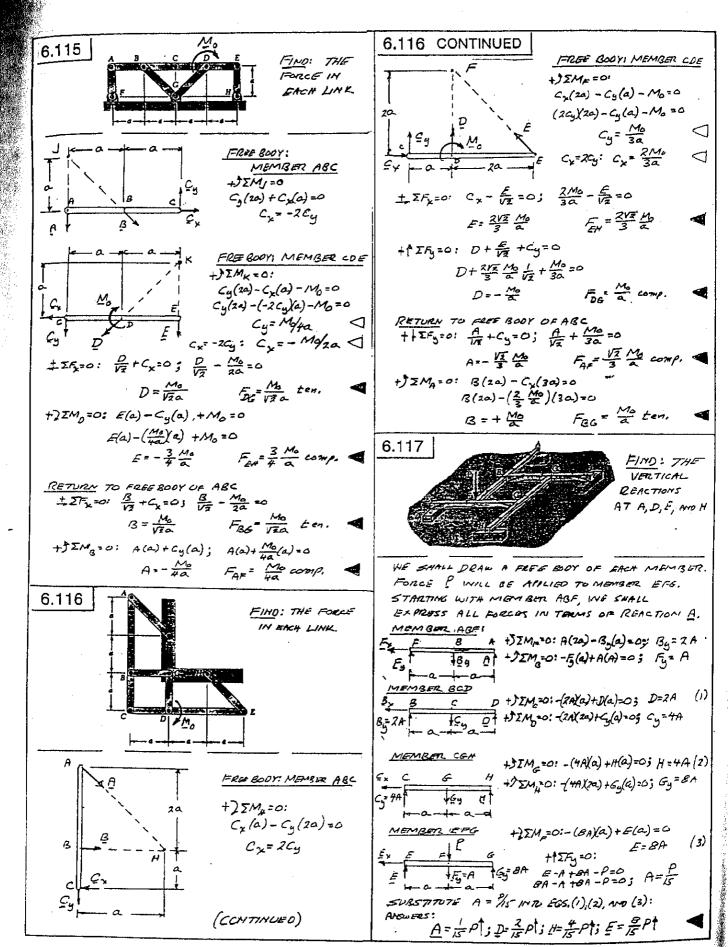
FBG=0

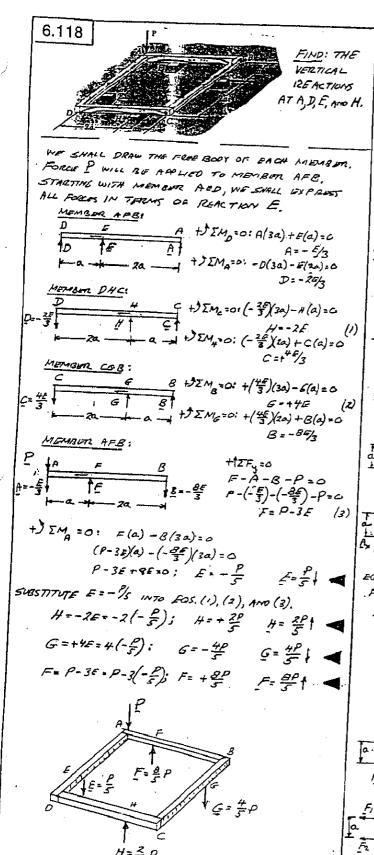


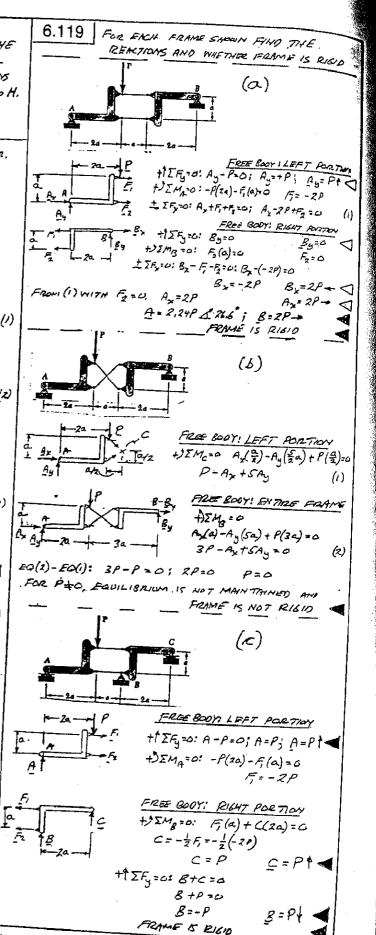
B(2a) + = P(3a) =0

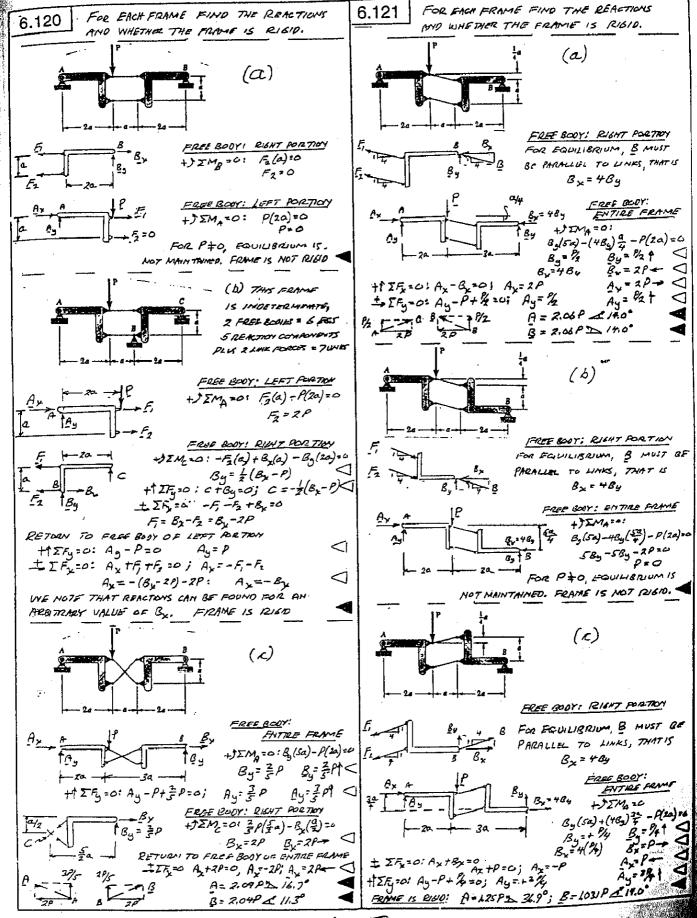
B = -P

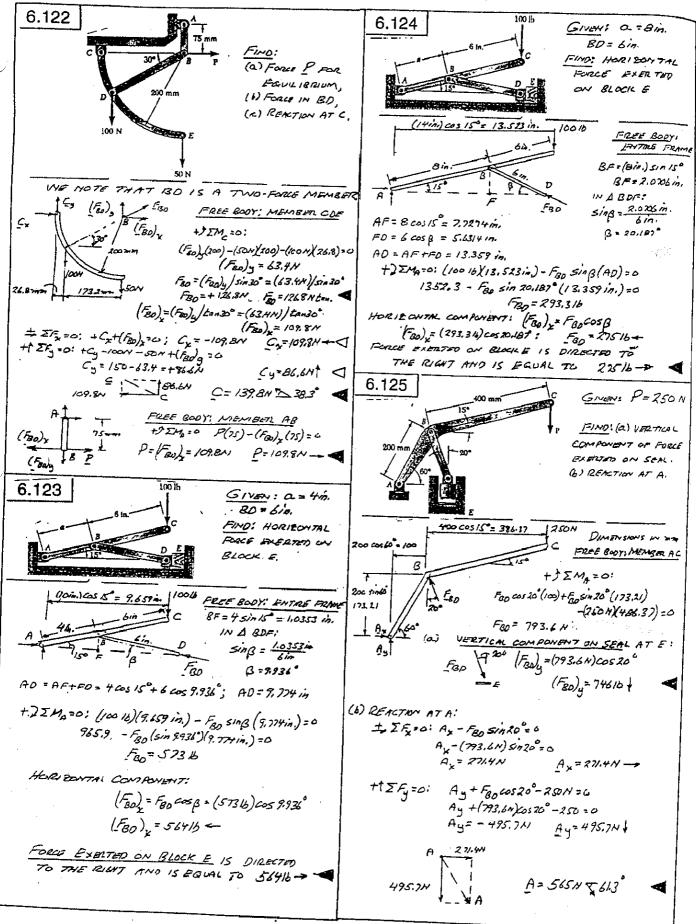
F86 = P 00 mp.

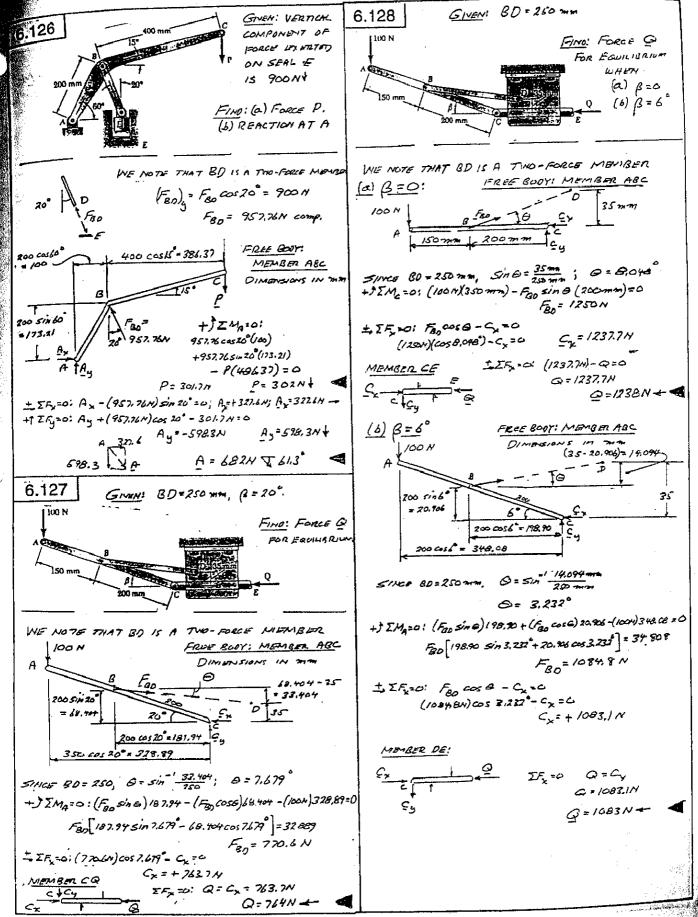


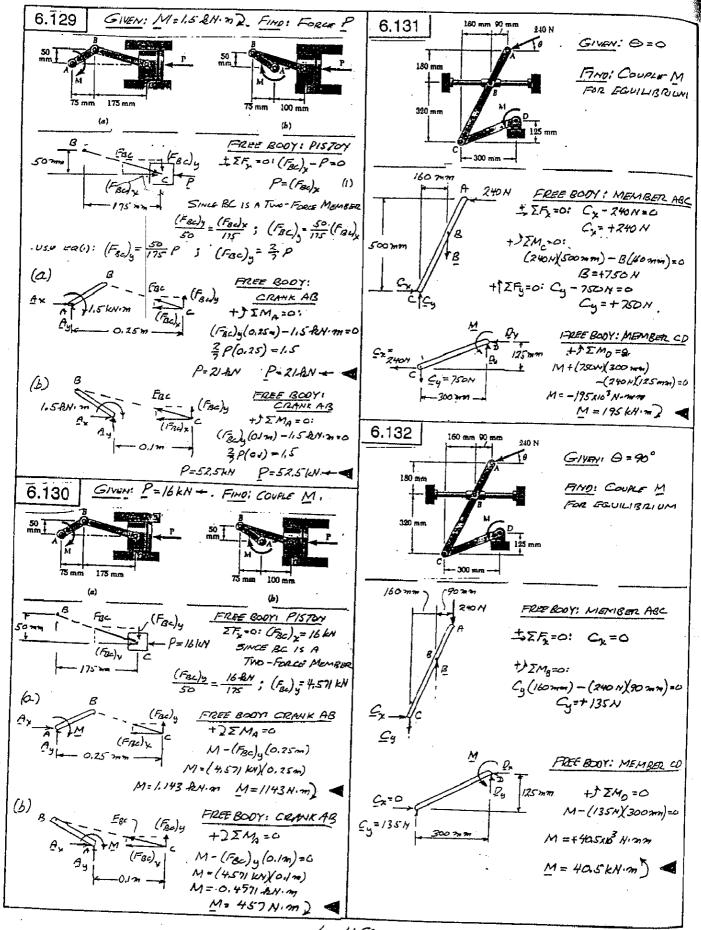


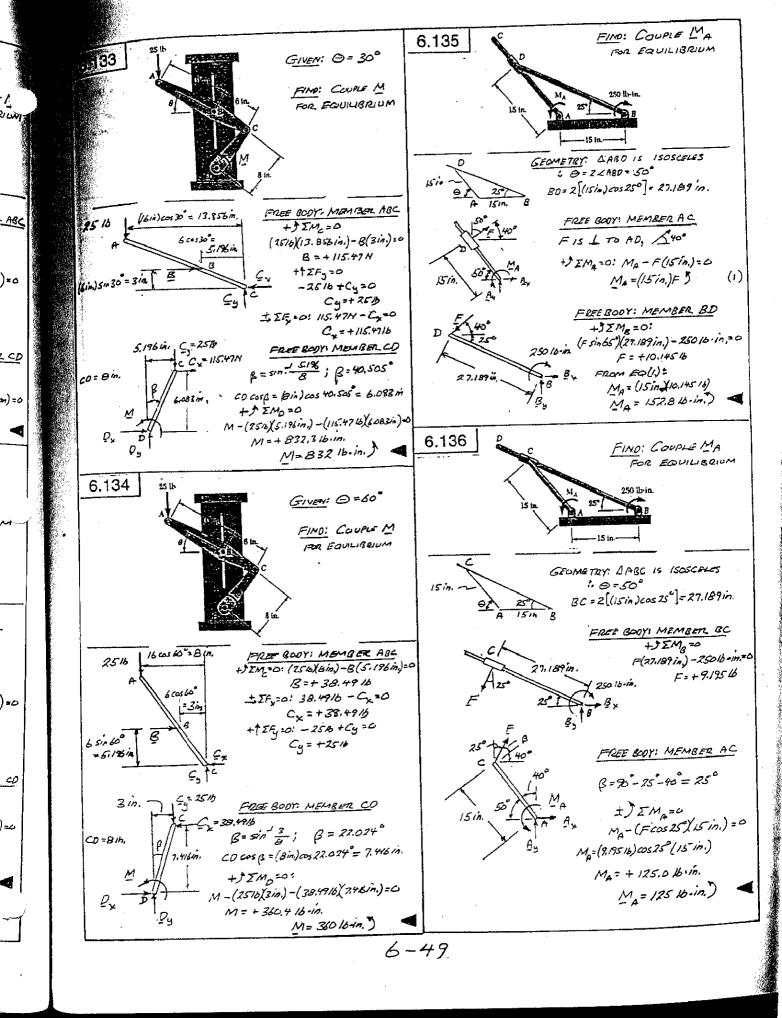


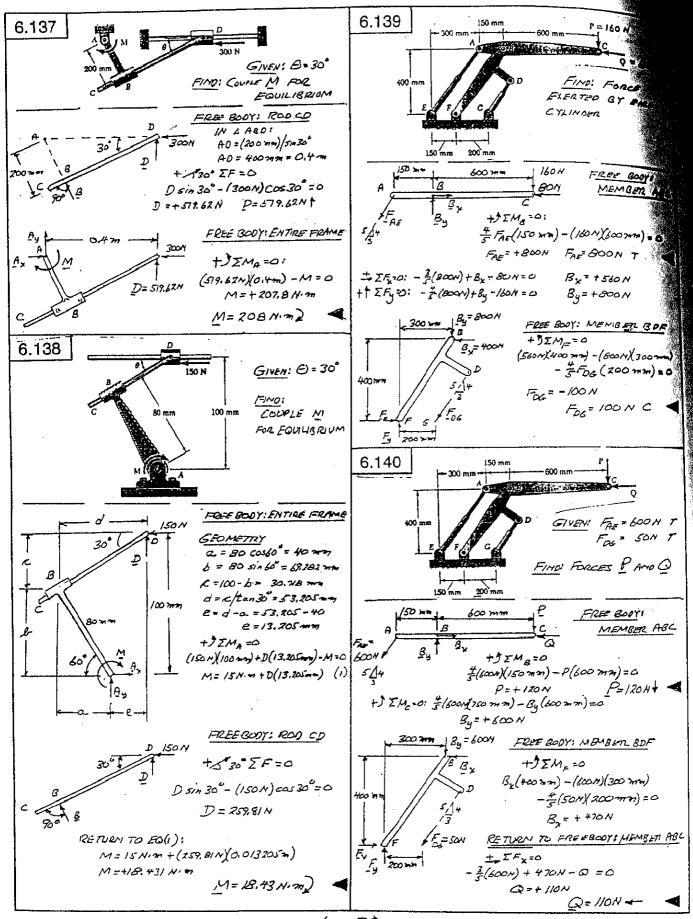


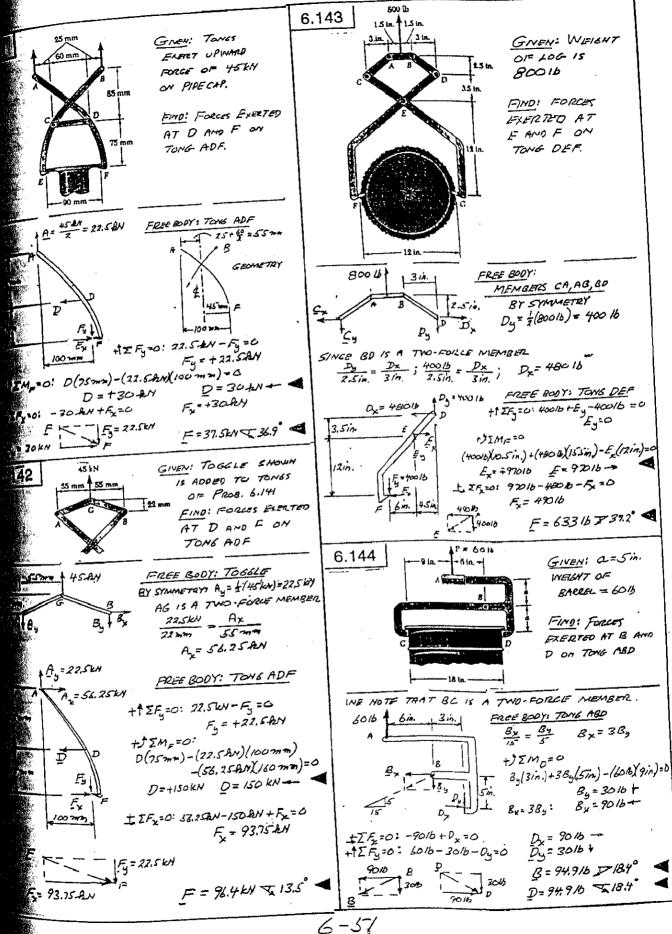


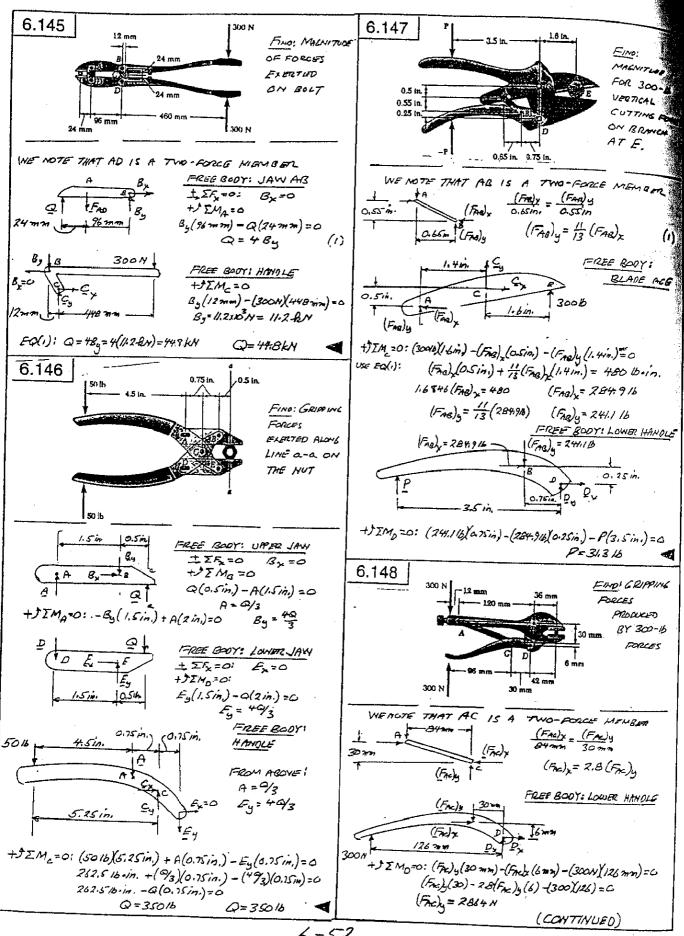


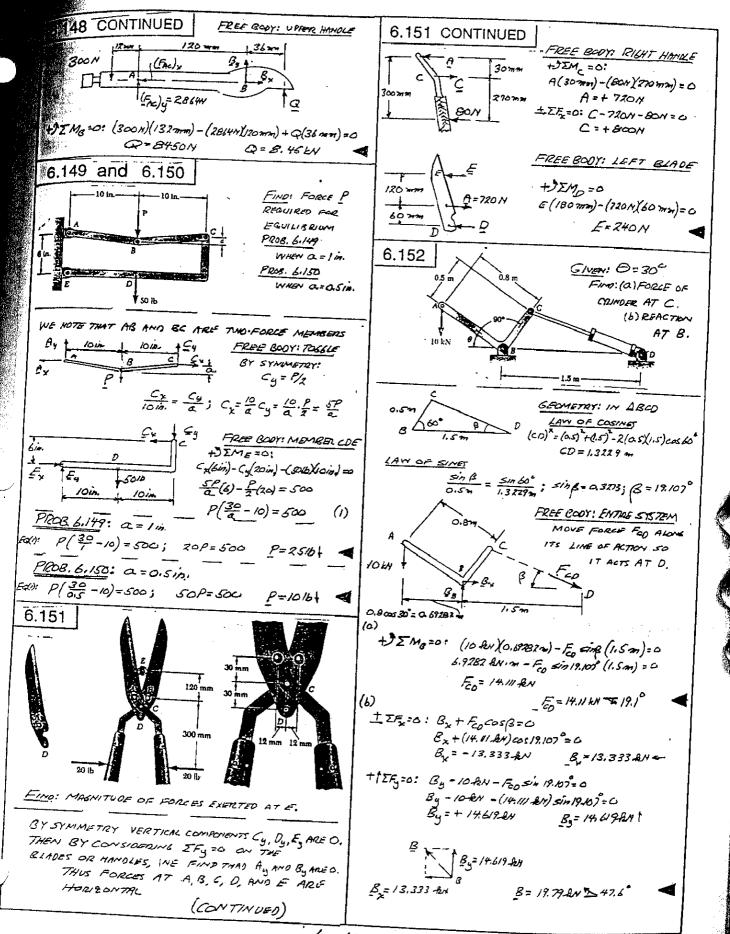


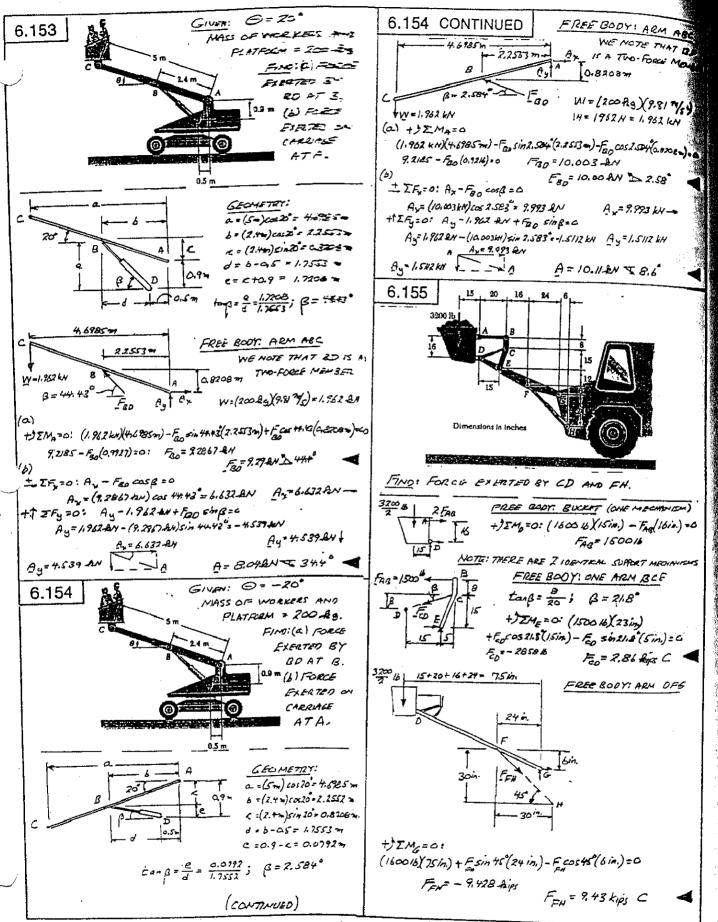


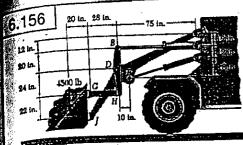








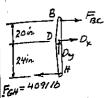




FINO FORCE EXERTED BY 6) CYLMORR BC (b) CYLINDER EF

450016 22 in

FREE BOOK BUCKET +12M1=01 (4500 16) (20in.) - Fee (27in)=0 FGN = 4091 16

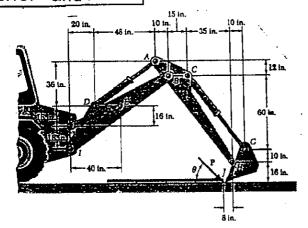


FREE BOOT: ARM BOH + > EM0=0. -(409) 16)(24 in.) - FBc(20 in.)=0 FBC=-490916 FBC=4.91 kip C €

FREE BOOY: ENTIRE METHONISM (TWO ARMS AND CYLHAGES AFJE) 20+28+75=123V+ ~ 2.Fer 4500 lb NOTE: TWO ARMS THUS 2 FEF

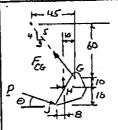
tong= 18in.; B= 15.48 +) IM= co: (450016)(123 in)+FBC(12in)+2FEF COSES (24in)= (4500/b)(13in) - (49094)(12in.) + 2 Fecos 15.46(24in.)=0 FEF=10.69 kin C ◀ FEP= -10,69016

and 6.158 6.157



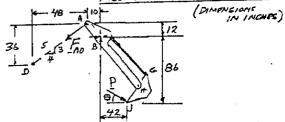
GIVEN: P= 2 kips FIND: FORCE PYENTYD BY EACH CYLINDER PROB. 6.157 WHEN @=45° PROB. 6.158 WHEN G=0

6.157 and 6.158 CONTINUED



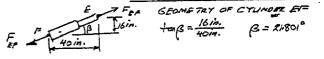
FREE BODY: BUCKET + TIMH = 0 (DIMENSIONS IN INCHES) \$F_CG(10) + 3F_CG(10) + Pcos 0(16) + Psino (8) = 0 F= - P(16 cos 0 + 0 sin 6) (1)

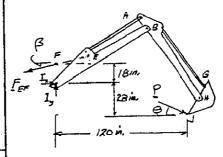
FREE BOOT ARM ABH AND BUCKET



+) IM8 = 0: 4 Fro(12)+ 3 Fro(10) + Prose(Bb) - Psin @(42) = 0 FAD = - P (86 coso - 42 sing) (2)

PEFE BOOT: BUCKET MY ARMS IEE+ABH





FEE COSB (18in) + PCSB (28in) - PSin B (120 in) = C

 $\frac{P(120 \sin \theta - 20 \cos \theta)}{\cos 21.6^{\circ}(18)} = \frac{P}{16.7124} (120 \sin \theta - 20 \cos \theta) (2)$

PROB. 6.157 P= 2 Rips, 0=45°

FO(1): Fa = - 2 (16 cas 45 + 8 sin 45") = -2.42 popt

Fac= 2.42 kys C Ea(2): Fac= - 2 (86 cos 45 - 42 si 45) = -3.99 Kys

FAD= -3.99 Kips C

EC(3): FEF= 2 16.7126 (120 50.45 - 2800545) = +7.79 KM

F= 7.79Kp T

PROB. 6.158 P= 2 & p, G=0

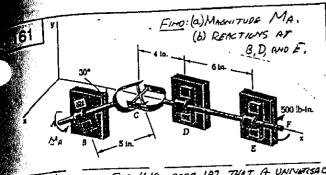
ED(1); FG= - 2/4 (16 cos 0 + 8 sin 0) = - 2.29 - E.A. Fe6 = 2,29-Peps C

EO(2): FAO = - 2 (860050 - 425100) = -11.03 Pers

FAD = 11.03 Leips C

FC(3): FEF 16.7126 (120 500 - 28 cas 6) = - 3.35 Dups

FEF = 3.35 Ris C



WE RECALL FROM FIG. 4.10, page 187, THAT A UNIVERSALL DINT EXECTS ON MEMBERS IT CONNECTS A FORE OF WENDERN DIRECTION AND A COUPLE ABOUT AN AMS WERDEN OILULAR TO THE CROSS DIRECE.

IM=0: Mc cas 20 - 500lb.11.20 Mc= 577,3546 vin

ENER BOOY: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con STREET BOOY: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WITH Z' ALONG BC

Con Street Booy: SHAPT BC

WE USE HERE X, 3, 2

WE USE HERE BOOY: SHAPT BC

WE USE HERE X, 3, 2

WE USE HERE BOOY: SHAPT BC

WE USE HERE X, 3, 2

WE USE HERE BOOY: SHAPT BC

WE U

EME = 0: -M, L' -(577.3516.10)L' +(-512)L'X(8, 3+8.1)=0

FOURTE COEFFICIENTS OF UNIT VECTORS TO ZETLO:

MA -577.3516.10.

D B==0 7 MA=577 b.in. ◀

By=0 5 8=0 B=0

IF-0: B+C=0, SINCE B=0, C RETURN TO FREE BODY OF EMAPT DF

EM =0 (NOTE THAT C=0 AND M= 572.35/6.11.

[577.35 b-in](cos 30 i + sin 20 i) - (500 /b-in)i

(577.3516-10)(COS 50 2 - 510 2 3) + (610)(+x(E, L+E, 1+E, 1+E, 2+E, 2)=0 (500/10-10)(+(288168/10-10)); -(500/10-10)(

FOLATE COEFFICIENTS OF UNT VECTORS TO 2000;

1 258.58 16 in, - (6 in,) E = 6 E = 48.1 16

(₹) £3=0

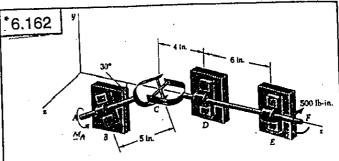
ΣF=0: C+D+E=0 0+0, +0, ++ 6, + +(48.116) &= 6

(Fx=0

(1) Dy 20

3 De +48.16=0 De=-48.16

REACTIONS ARE: B=0 D=-(48.14) & E= (48.14) &



GIVENI ROTATE SHAFT WITH CROSSPIECE ATTACHED TO SHAFT OF IS VERTICAL, THEN

FIND: (a) MAGNITUDE MA. (b) REPORTIONS AT B.D. AND E.

Czł Dzł Ezł (500 16-in) 2 Ezł M=500 16-in.

EM = 0; M_-500 16. In. = 0 M=500 16. In.

FREE BOOT: SHAFT BC

Sin. -C.;

Sin. -C.;

Sin. -C.;

WE USE HERE 7, 4, 7

WITH 2' ALDHE BC

Mai'

WE RESOLVE - (500 16.10.) L 11.70 COMPONENTS E ALONE 12 AND Y AXES: -M= - (500 16.10.) (cos30 L'+ sin30 j') IM=0: M, L' - (500 16.10.) (cos30 L'+ sin30 j) + (510.) L'X (By j'+ B2B) = 0

Mai' - (433 10 1/4) L' - (250 10 - 1/4) J' + (5/1) By & - (5/1) By J'=0
EQUATE TO ZERU COEFFICIENTS OF UNIT VECTORS:

(1) = 433 lb·in = 0 MA = 433 lb·in.

(3) - 250 16-in. - (Sin.) Bz=0 Bz=-50 16

REACTION AT B: B = - (5016) &

IF=0: B-C=0 -(5016) R-C=0 C=-(5016) R

RETURN TO FREE BOOY OF SHAFT DF: IMD=0: (6in)!x(Ex!+Ex++Ex)-(4in)!x(-5016)& -(50016.in)! +(50016.in)! =0

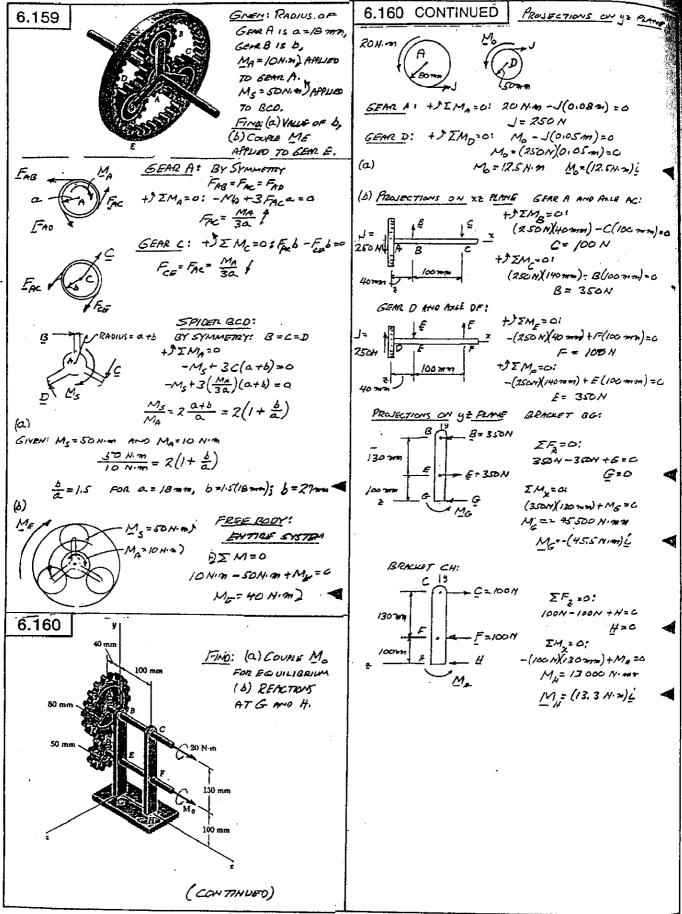
(lin) Ey & - (bin) Ez & - (200 16 in) 1 = 0 (bin) Ey = 0

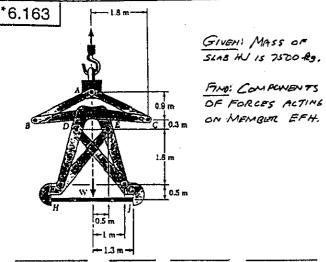
(1) $E_2 = 200 \text{ (b. in. = 0)}$ $E_2 = -33.316$

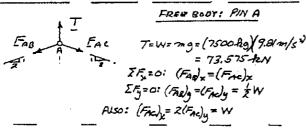
Σ F = 0: C + D + E = 0 -(50 16) & + D = 1 + D = 1 + E = (33.316) & = 0

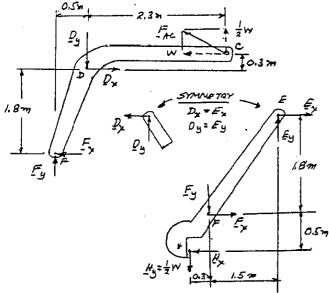
> (1) -5016 -33.316 + D₂=0 D₂=83.316

QEACTIONS ARE: B= -(5016)& D= (83,316)& E=-(33,316)&









FIZEE BOOY: MEMBER COE +) [Mp=0: W(0,3) + 1/2 w(2.3) - Fx(1.8) - Fx (0.5m)=0 (i)OR: 1.8 Fx + 0.5 Fx = 1.45 W Dx - Fx - W=0; OR Fx - Fx = W $\pm \sum F_{\kappa} = 0$: (z)

+1 E==0: F= Dy++++0; OR F4-F= +W (3) FREE BODY: MEMBER EFH

+) \(\TM_{10} = 0: \F_{\sigma}(1.8) + F_{\sigma}(1.5) - H_{\sigma}(2.3) + \frac{1}{2}W(1.6m) = 0 (4) OR 1.8Fx + 1.5Fy = 2.3Hy -0.9W (5)

I Sty=0: Ex+Fy-Hy=0 OR Fy+Fy=Hy

(CONTINUED)

* 6.163 CONTINUED

2/5,= H2-W SUBTEMT (2) FROM(5): SUB TRACT (4) FROM 3x(1): 3.4Fx=5.25W-2.3Hx 1. 8.25 = 2.95W A00(7) 70 23x(6); Fy = 0.35976 W

SUGSTITUTE 1=ROM (B) INTO (1):

(12)(0,3592W) + 05Fg = 1.45W a5/==1.45W-0.64758W=0.80244W Fy = 1.6049 W

SUBSTITUTE FROM (8) INTO (2):

Ex= 1.3597644 Ex-0,359XW=W;

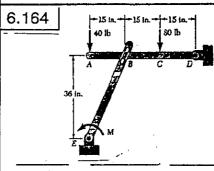
SUBSTITUTE FROM (9) IN TO (3):

Ey = 2.1049W Ey-1.6049W= +W

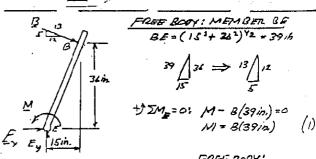
FROM (5) = H=E+F=1.359XW+0.359XW=1.71952W Hy= えい RECALL THAT:

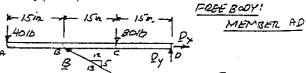
SINCE ALL EXPRESSIONS OB THING MEG POSITIVE, ALL FORCES ARE DIRECTED AS CHOWN ON THE FREE-BODY DINGRAPAS.

SUBSTITUTE W= 73.575-RN:



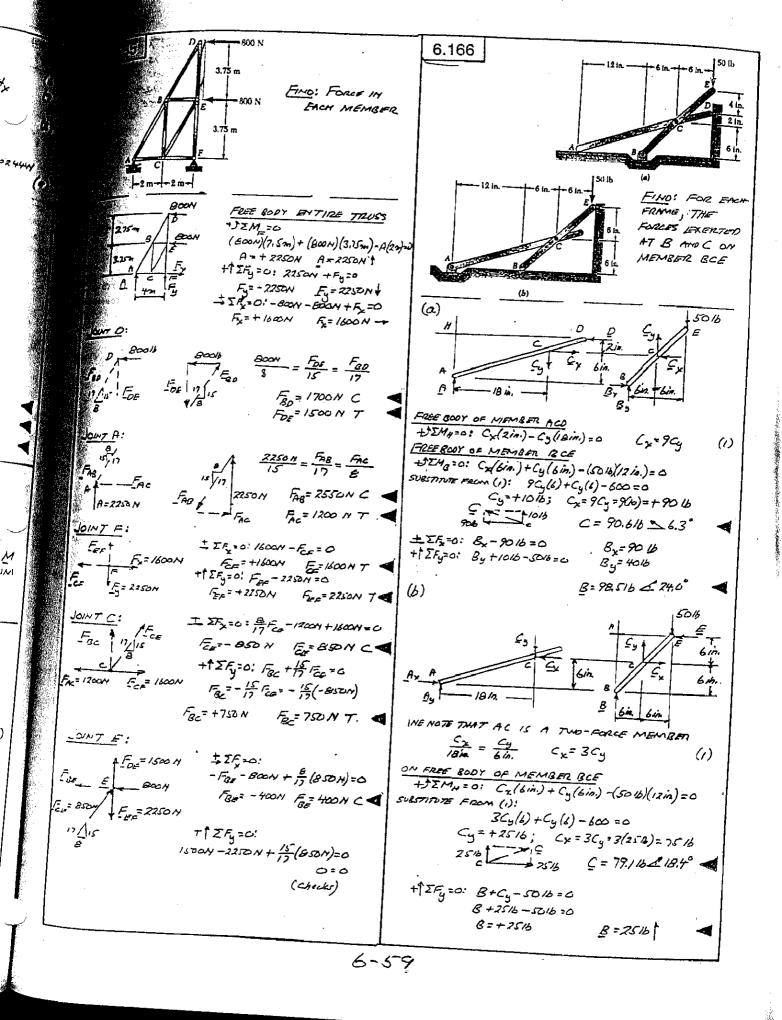
FINO: COUPLE M FOR EQUILIBRIUM

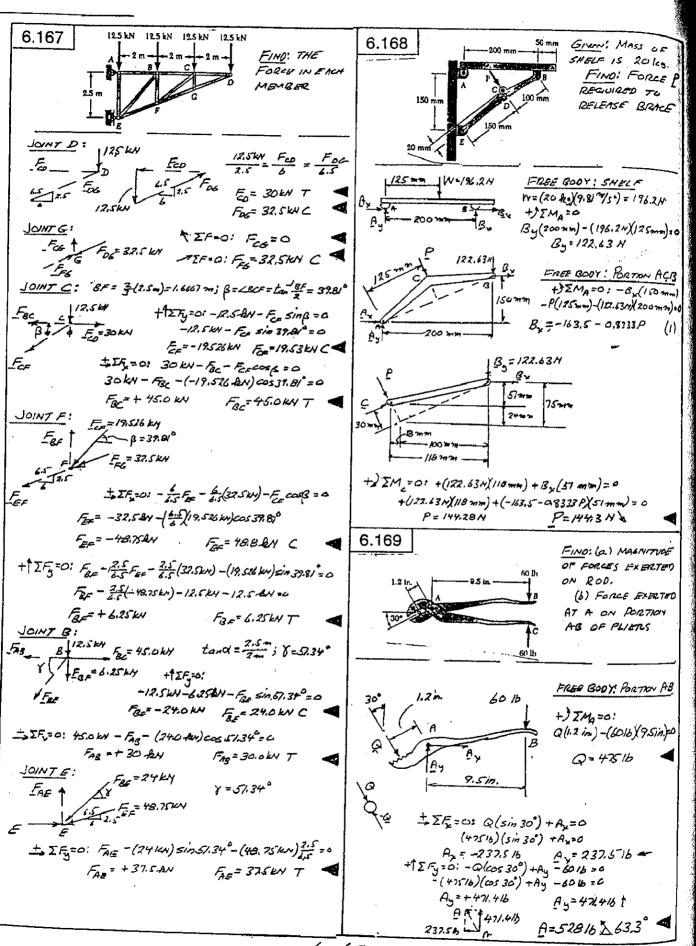




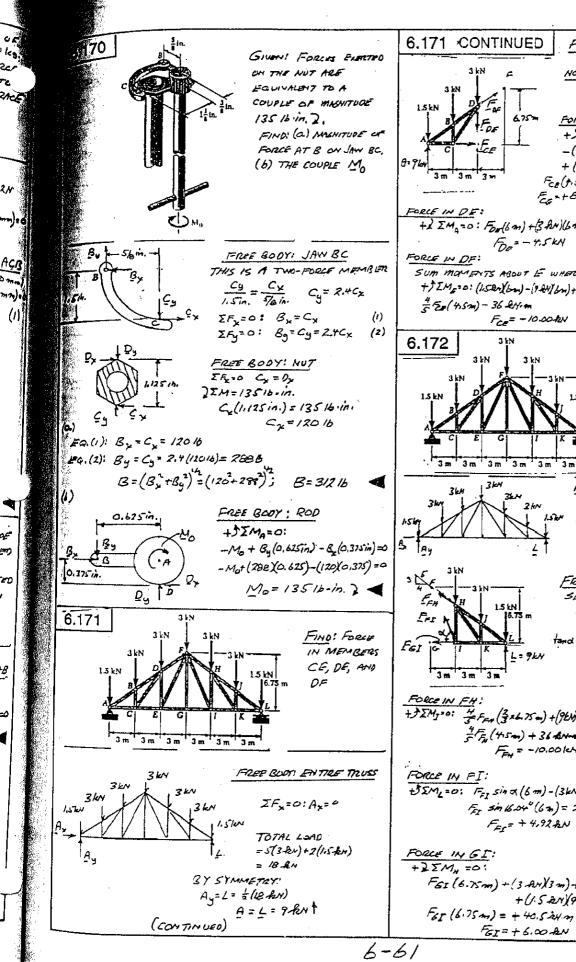
+) IMD=0: (4010)(45in.)+(6010)(15in.)- = B(30in.)=0 B = 26016

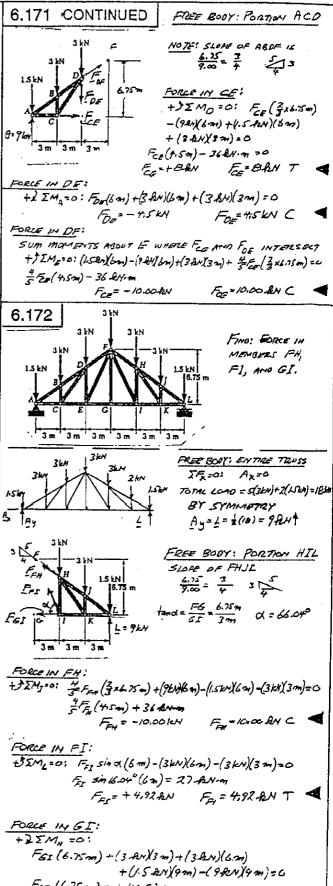
EG(1) M=B(39in)=(2601)(39in)=10,14016-11. M = 10. 4 kip in.)



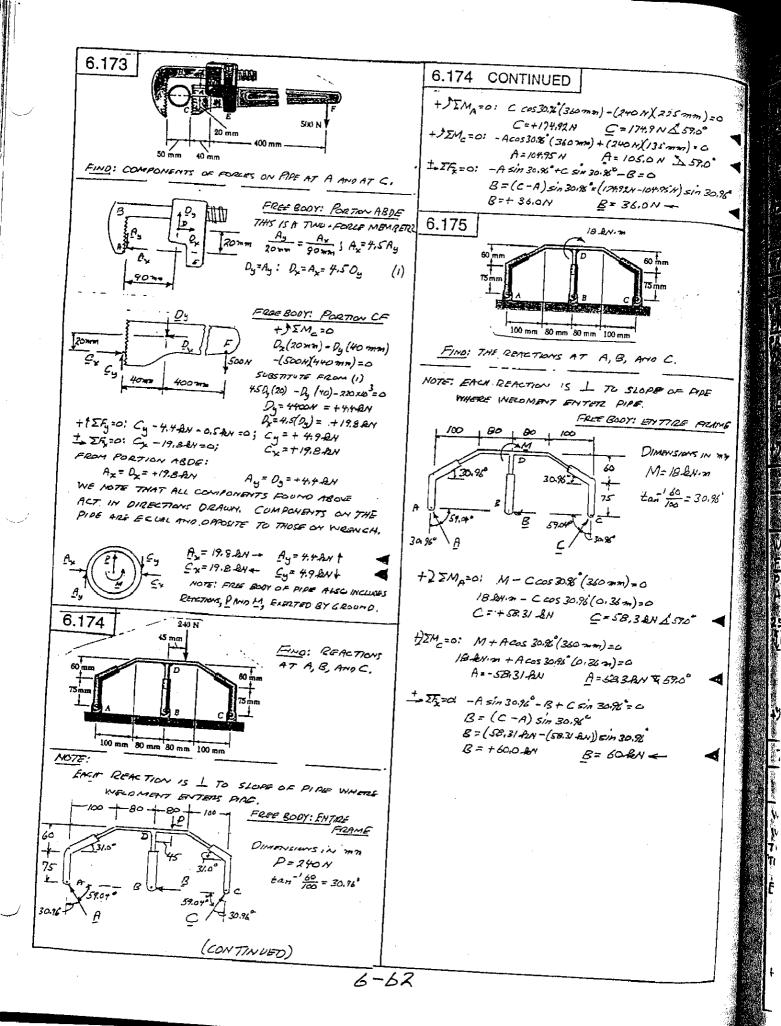


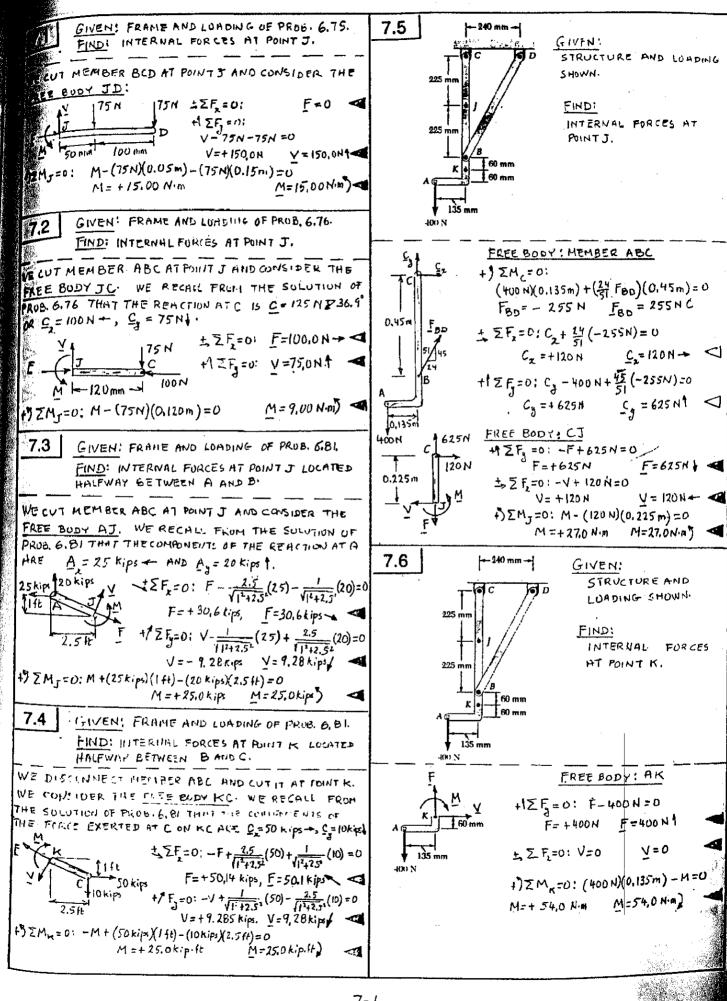
6-60





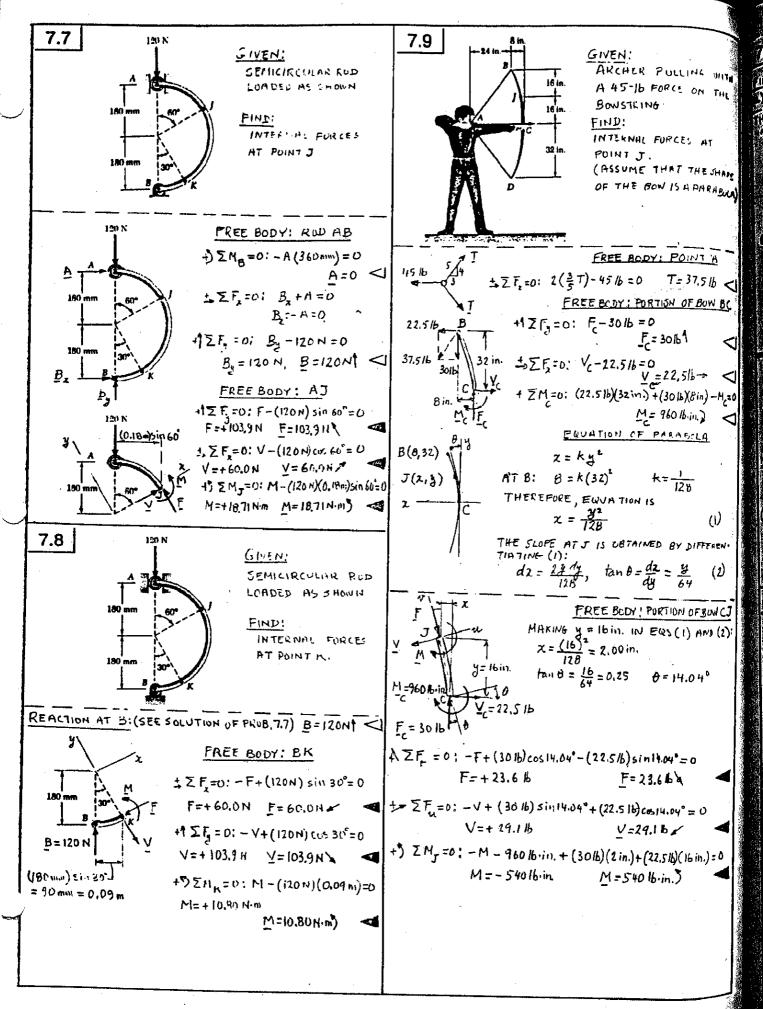
FET = 6,00 PM T

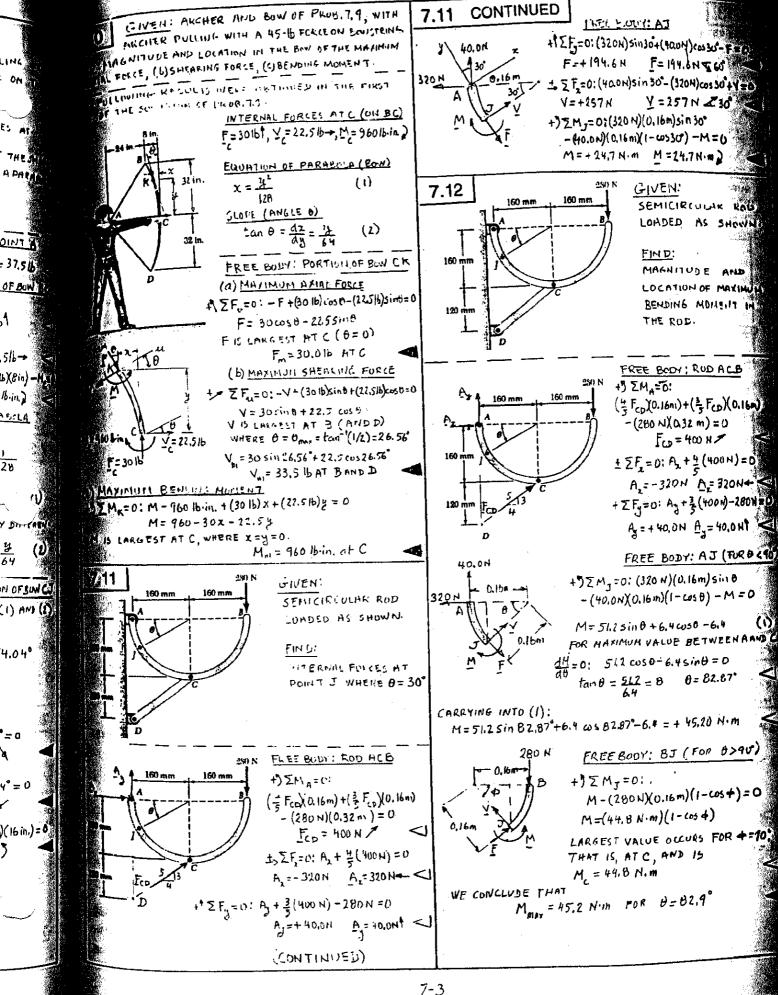




30,80

1116





DINT TO

: 37.5 🖟

5/6-

16 m.

SCL4

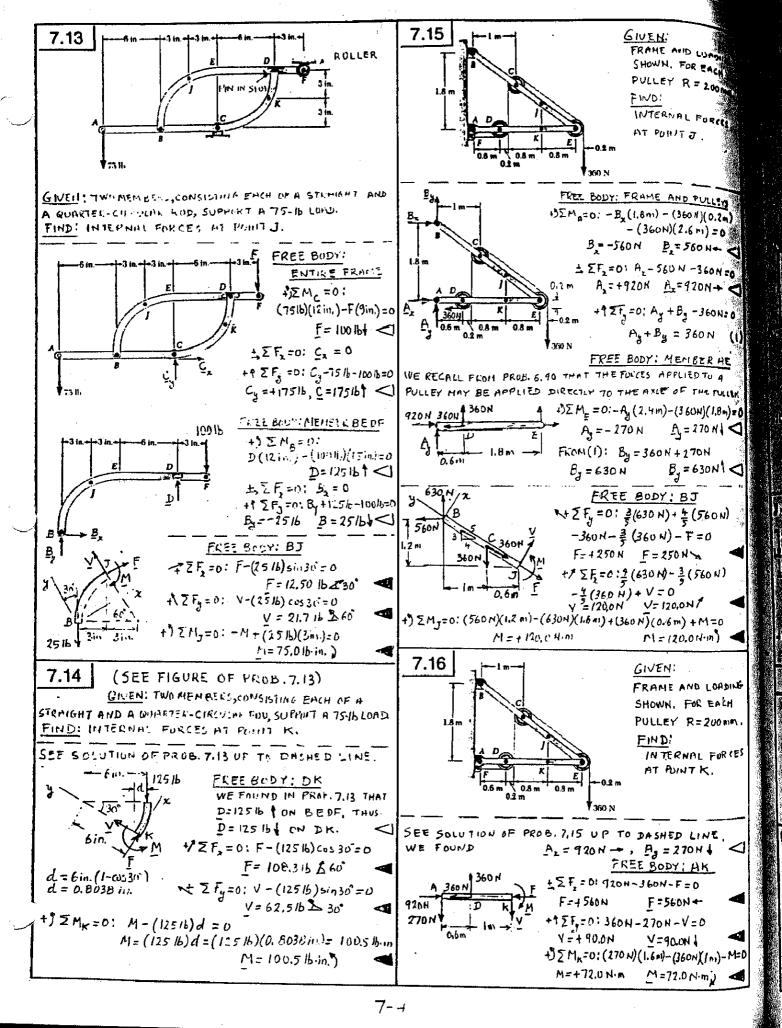
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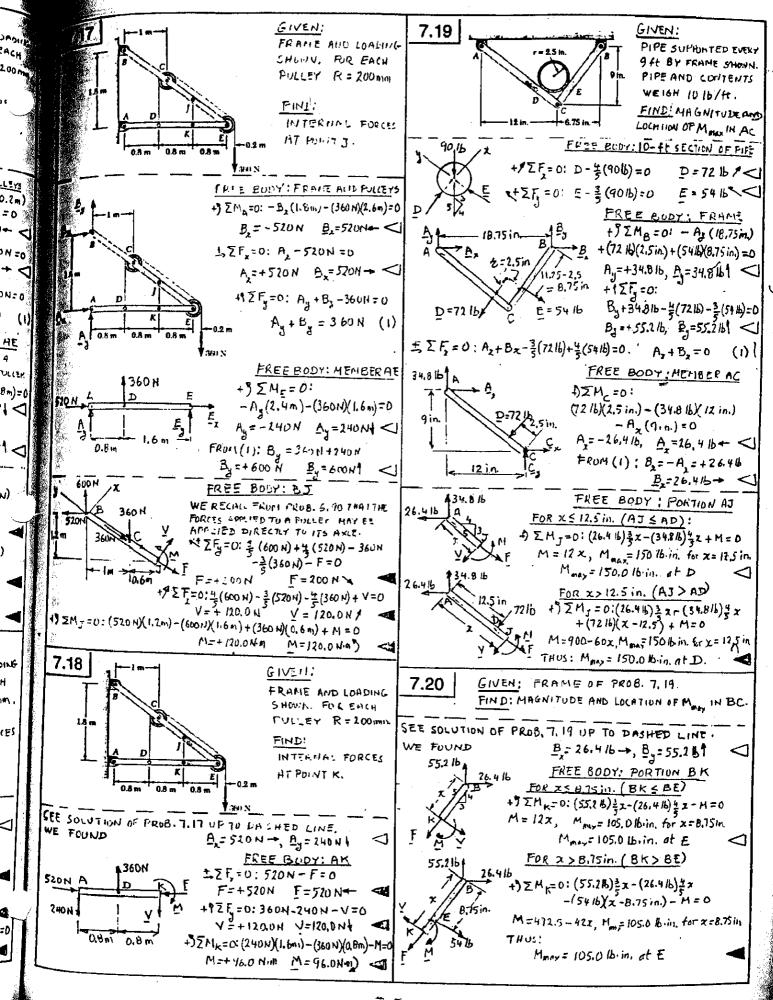
64

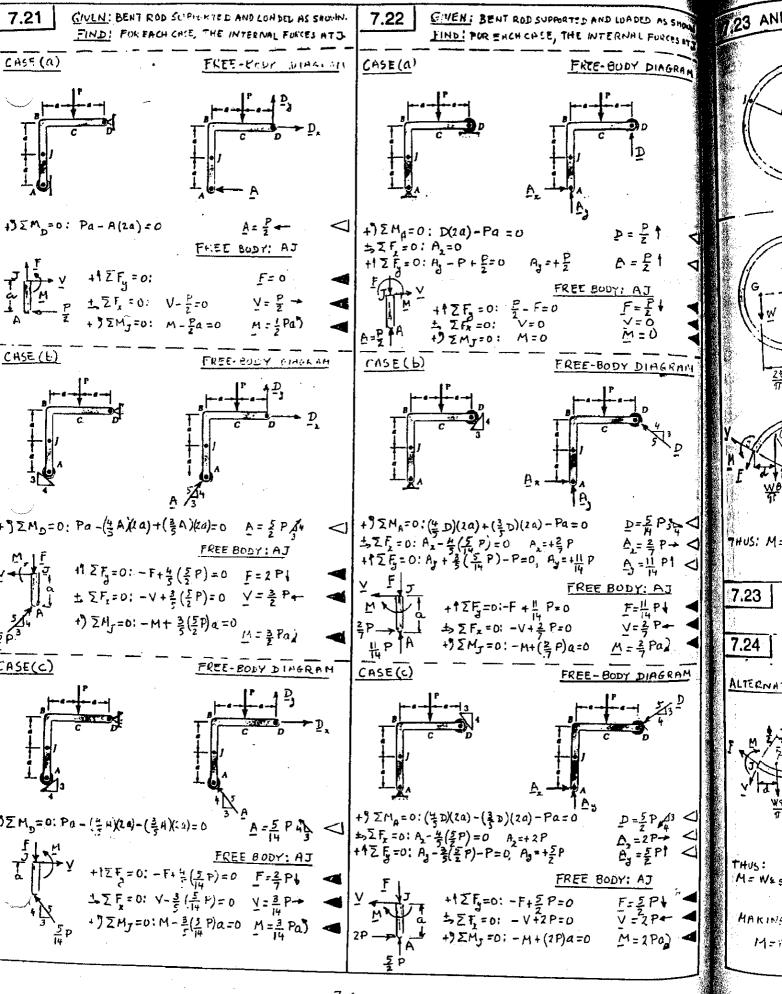
4.040

)(16 in.)=

b)(8in}**-Ĥ**



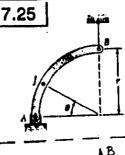




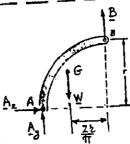
AND 7.24 GIVEN: SEMICIRCULAR RUD OF WEIGHT W AND UNIFORM CROSS SECTION SUPPURTED AS SHOWN. BENDING MUNENT AT J WHEN 0=60° (PROB. 7.23) 0=150 (PROB. 7.24) FREE BODY: ROD +) $\sum M_A = 0$: $W\left(\frac{2t}{11}\right) - B(2c) = 0$ 1ΣF=0; #-A=0 A=#-+ + E Fy = 0: Ay - W = 0 Ay = W1 FREE BUDY: IDETION BJ RAN + 3 2 Mz = 0: $M - \frac{W}{\pi} 2 (1 - \cos \theta) - \frac{W\theta}{\pi} d = 0$ M = # + (1-cost) + Wod BUT d= 2 sin 8 - 2 sin = = 2 sin 8 - 1 25 in 2 = 2 sin + - 2 (1-cost) ₩2(1-6050)+ ₩2 + sint - ₩2 (1-600) M= WE & Sin 8 (1)MAKING $\theta = 60^\circ = \frac{\pi}{3}$ IN Eq.(1): M=0.289WE) M = W2 Isin 60 = WE 511160 MAKING 8=150" = 5H IN EQ.(1): M= 0.417W2) ◀ M= W 51 sin 150 = 5 W2 RAM ALTERNATIVE SOLUTION TO FROB. 7.24: PREE BODY: AJ +7) ZN +=0: -M+W2sind-W2(1-60st)-Wd d=0 M= Wesind - #2 (1-ws 4) - ## d BUT d=もsin中·元sin号 =tsinサーセンsin2生 = tsind - 主 (1-105 d) M= WESING - # & (1-6054) - #2 + sin + + * (1-654) $\Lambda = 1 V_{\xi} \left(1 - \frac{\Phi}{17} \right) \sin \Phi$ MAKINE # = 180°-150° = 30° = 17/6 IN EQ. (2)1 M=0.417WE) M=Wz(1-左)sin30= まが (ON HJ)

J

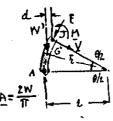
<u>3</u> D



GIVEN: CHARTER CIRCULAR ROD OF WEIGHT W AND UNIFORM CROSS SECTION SUPPORTED AS SHAUN BENDING MOMENT AT J WHEK $\theta = 30^{\circ}$.



FREE BODY : ROD ±5F,=0: $A_{r} = 0$ 45 ZMB=0: W(30) - Ay 2 = 0



PREE BUDY ! PORTION AT 4) ZM, =0: M+W'd- 2W+(1-cos +)=0 M = 2W 2 (1-605B) - W'd (1)BUT $W' = W \frac{\theta}{\pi l/2} = \frac{2W\theta}{\pi}$ (2)

AND
$$d = \overline{z} \cos \frac{\theta}{2} - t \cos \theta$$

$$= z \sin \frac{\theta}{2} \cos \frac{\theta}{2} - t \cos \theta$$

$$= t \frac{2 \sin \frac{\theta}{2} \cos \frac{\pi}{2} - t \cos \theta}{d = z \left(\frac{\sin \theta}{\theta} - \cos \theta\right)}$$
(3)

SUBSTITUTING FROM (2) AND (3) INTO (1); $M = \frac{2W}{\pi} 2(1-\cos\theta) - \frac{g\psi\theta}{\Omega} 2\left(\frac{\sin\theta}{\theta} - \cos\theta\right)$ M = 2 W2 (1-cos 0 - sin 8+0 cos 0) MAKING 8=30 = 1 IN EQ (+);

M = 2W& [1-cos 300 - sin 300 + 1 cos 30] M=0.0557 WE)

THE SOLUTIONS OF PROBS. 7.26 AND 7.27 ARE GIVEN ON THE NEXT PAGE

GIVEN: ROD OF PROB. 7.25. FIND: MAGNITUDE AND LOCATION OF MAXIMUM BENDING MUNIENT.

WE RECALL EQ. (4) OF PROB. 7.25: (4) $M = \frac{2Wt}{\pi} \left(1 - \cos \theta - \sin \theta + \theta \cos \theta \right)$

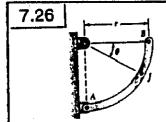
 $\frac{dH}{d\theta} = \frac{2We}{TT} \left(\sin\theta - \cos\theta + \cos\theta - \theta \sin\theta \right)$

SETTING AM = 0: $sin\theta (1-\theta) = 0$

THE ROOTS OF THIS ENUNTION FOR OSES # HRE 0=1 RAD=57.3* B=D AND

FOR 0 = 0, M = 0. FOR 0 = 1 RAD = 57.3°, EW. (4) YIELD M = 2WE (1-cos 57,30 - sin 57,30+ 1 x cos 57,30) = 2Wt (1- sin 57.5") = 0.1009 Wi

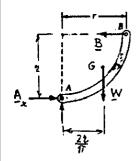
May = 0.1009 Wz for 8 = 57.3° THUS:



GIVEN:
QUARTER CIRCULAR RUD OF
WEIGHT W AND UNIFORM CROSS
SECTION SUPPORTED AT SHOWN.
FIND:

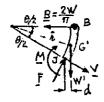
FINE:
BENDING MONENT HT J WHEN
0 = 30"

FREE BODY: RUD



+)
$$\Sigma M_A = 0$$
:
 $Bt - W(\frac{2t}{\pi}) = 0$
 $B = \frac{2W}{\pi}$

FREE BODY: PORTION BJ



$$\frac{2W}{\pi} z \sin \theta - W'd - M = 0$$

$$M = \frac{2W}{\pi} z \sin \theta - W'd \qquad (1)$$

BUT W'= W
$$\frac{\theta}{\pi/2} = \frac{2W\theta}{\pi}$$
 (2)

AND
$$d = \frac{2}{2}\cos{\frac{\theta}{2}} - 2\cos{\theta}$$

$$= 2\frac{\sin{\theta/2}}{\theta/2}\cos{\frac{\theta}{2}} - 2\cos{\theta}$$

$$= 2\frac{\sin{\theta/2}\cos{\theta/2}}{2\sin{\theta/2}\cos{\theta/2}} - 2\cos{\theta}$$

$$d = r\left(\frac{\sin\theta}{\theta} - \cos\theta\right) \quad (3)$$

SUBSTITUTING FRUM(2) AND(3) INTO (1): $M = \frac{2N}{\pi} 2 \sin \theta - \frac{2N\theta}{\pi} 2 \left(\frac{\sin \theta}{\theta} - \cos \theta \right)$

 $M = \frac{2Wh}{T}\theta \cos\theta \qquad (4)$

MAKINE $\theta = 30^{\circ} = \frac{\pi}{6}$ IN Eq. (4):

$$M = \frac{2Wt}{\pi} \left(\frac{\pi}{6}\right) \cos 30^\circ = \frac{Wt}{3} \cos 30^\circ \qquad \underline{M} = 0.289 \ Wt_{N}$$

7.27 GIVEN: ROD OF Phus. 7.26.

FIND: MAGNITUDE AND LOCATION OF MAXIMUM BENDING MOMENT.

WE RECALL EU. (4) OF PRUB. 7.26 ;

$$M = \frac{2W^2}{\Pi}\theta \cos\theta \tag{4}$$

 $\frac{dH}{db} = 0$

$$cos\theta - \theta sin\theta = 0$$

 $tan\theta = \frac{1}{2}$

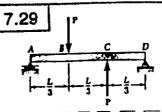
SOLVING BY SUCCESSIVE APPROXIMATIONS: \$\text{\theta} = 49.293^ = 0.86033 RAD

SUBSTITUTING INTO EQ. (4):

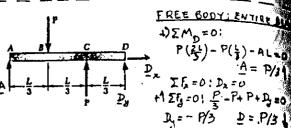
M = 2W1 (0.86033 RAD) COS 49.293 = 0.3572 W1

THUS: Mmax = 0.357 WE for 0=49.3°

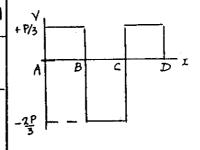
THE SOLUTION OF PROB. 7.28 IS GIVEN ON THE PRECEDING PAGE

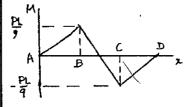


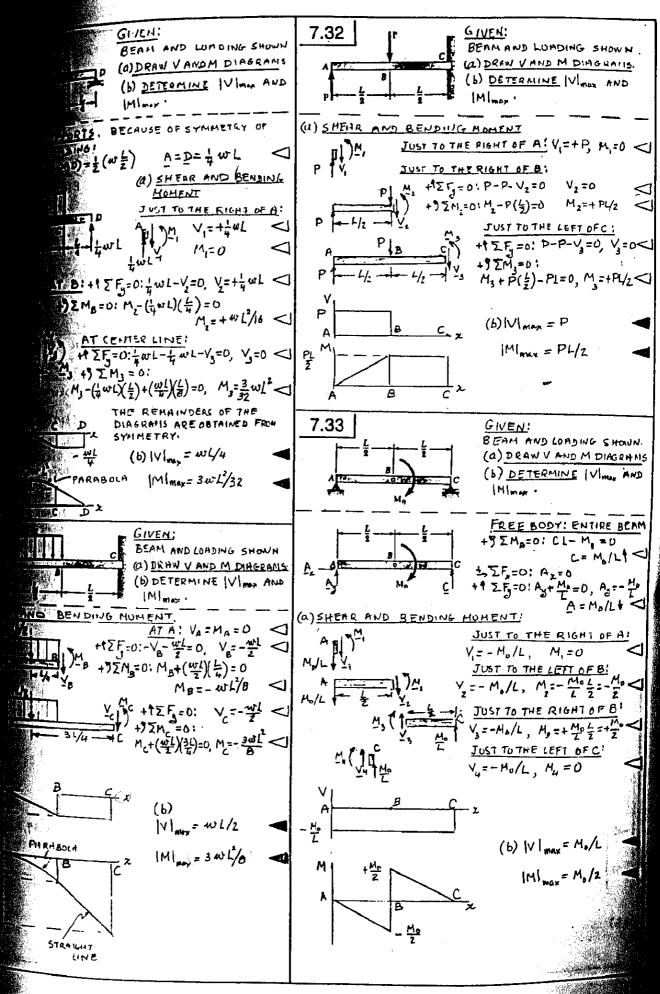
GIVEN:
BEHM AND LOADING
(a) DRAW VAND M DILL
(b) DETERMINE [V]

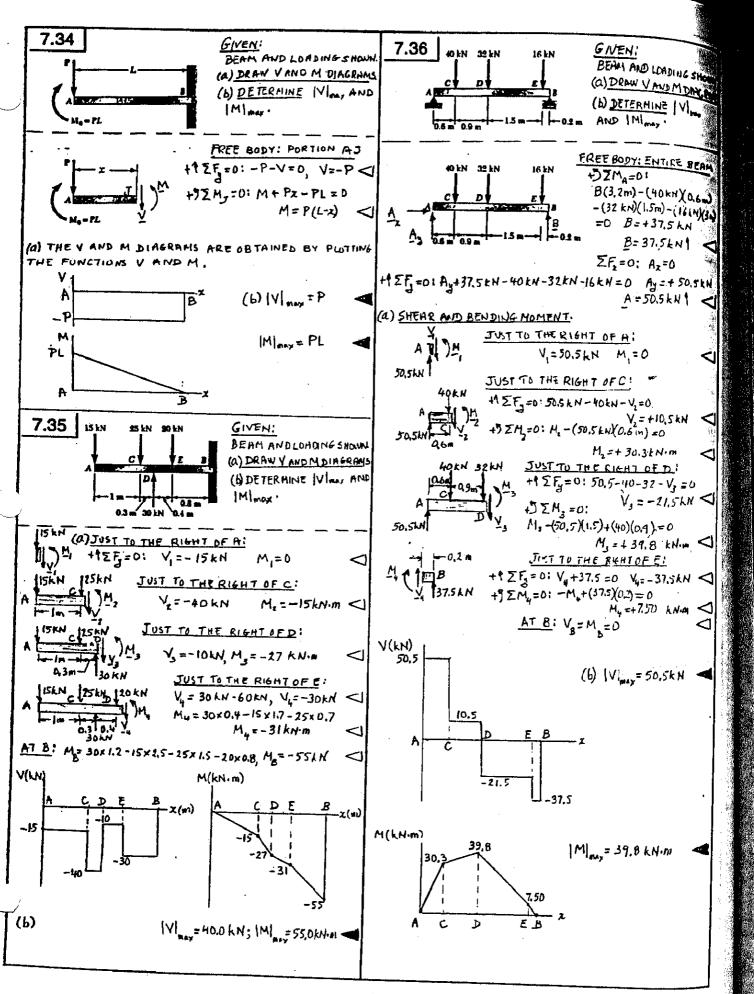


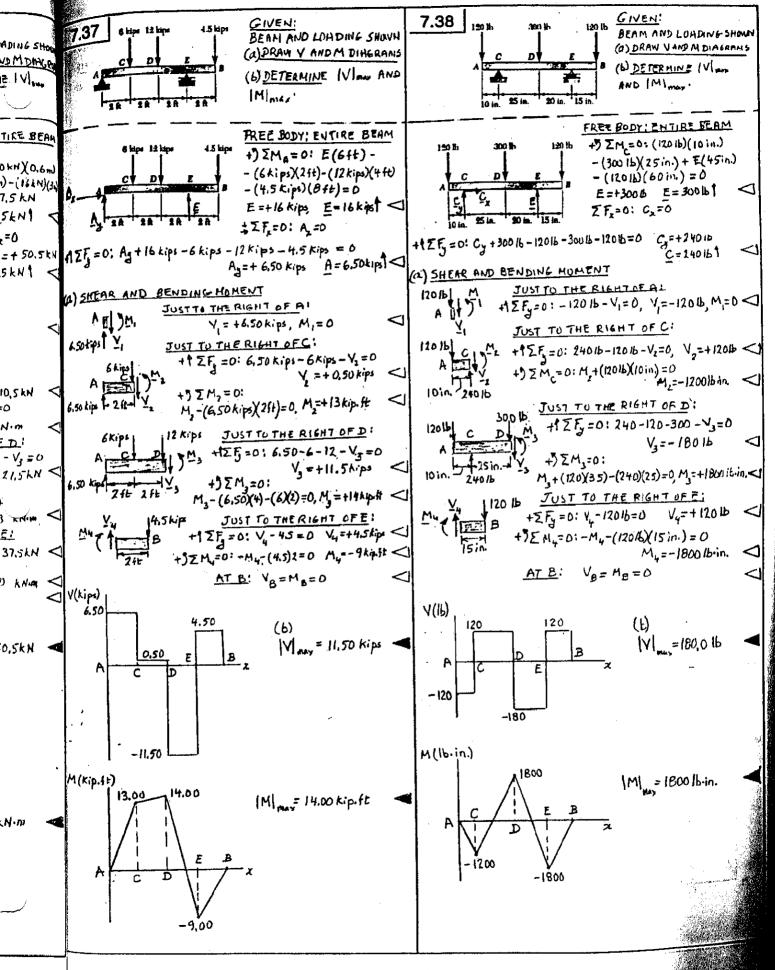
OF CONCENTRATED LUMBS, THE SHEAR DIAGRAM IS MAN HORIZONTAL STRAIGHT-LINE STEMENTS AND THE B.M. JIANA IS MADE OF OBLIQUE STRAIGHT-LINE SEGMENTS. WE SAME DETERMINE V AND M JUST TO THE RIGHT OF A, B, AND C

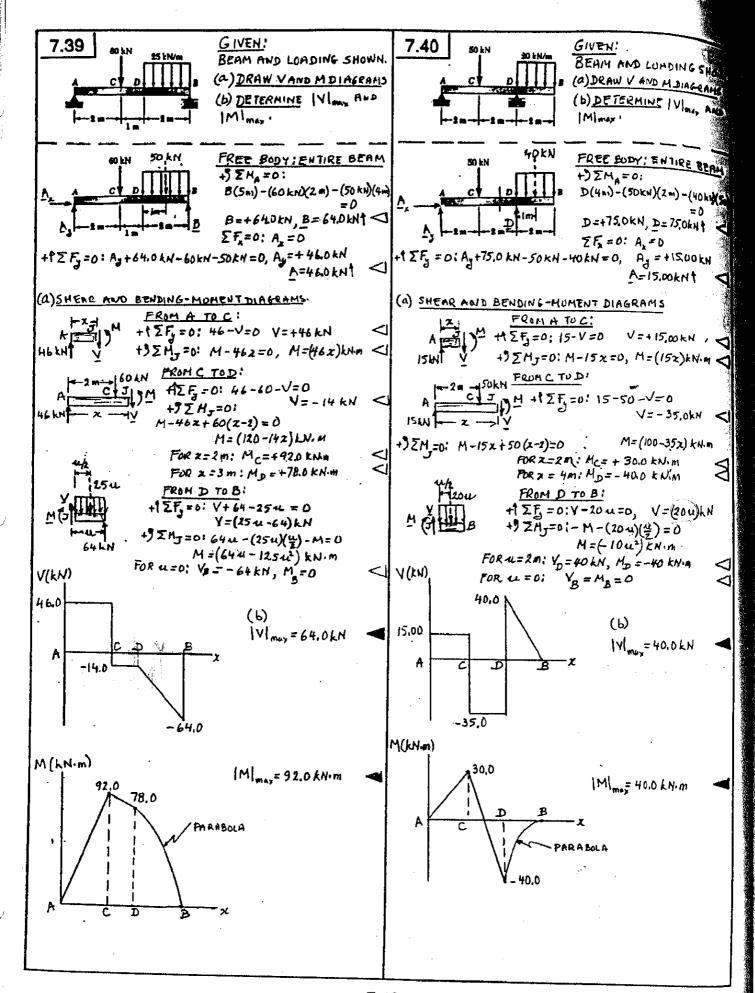


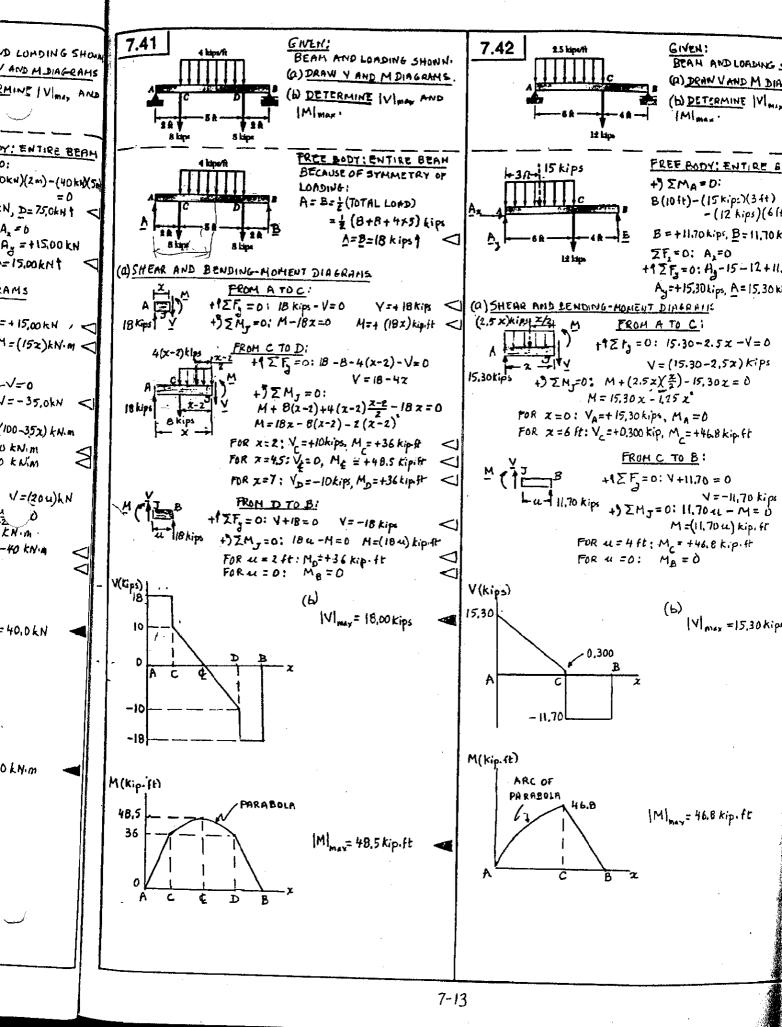


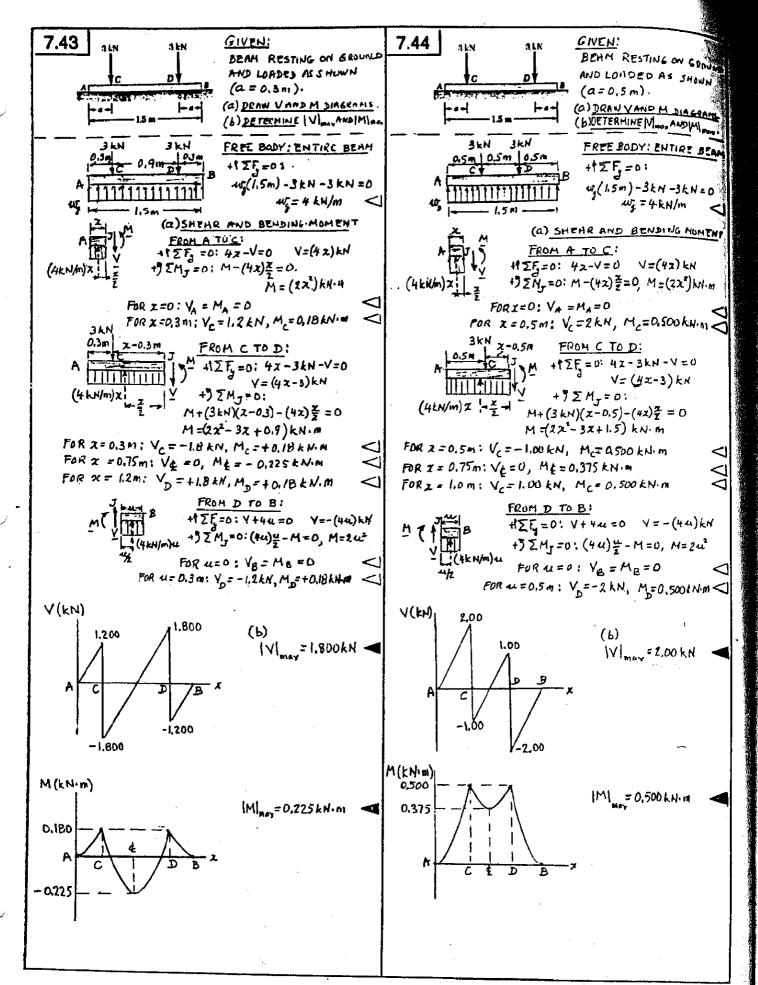


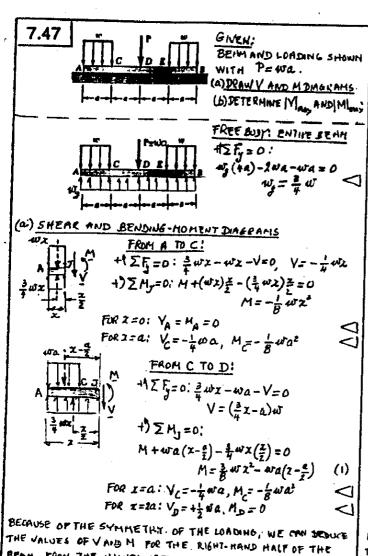




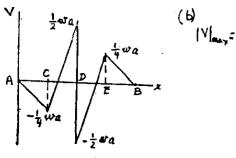




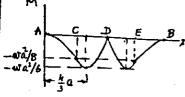




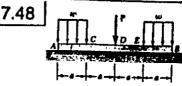
THE VALUES OF VAND M FOR THE RIGHT-HAND HALF OF THE BEAM FROM THE UNLUES OBTAINED FOR ITS LEFT-HAND HALF.



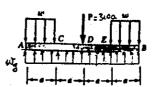
TO FIND IM MAY, WE DIPPERENTIATE ED. (1) AND SET dH =0: $\frac{dN}{dx} = \frac{3}{4} wx - wa = 0, \quad x = \frac{4}{3}a, \quad M = \frac{3}{8}w(\frac{4}{3}a)^2 - wa^2(\frac{4}{3}-\frac{1}{2}) = -\frac{wa}{6}$ IMmx=1 waz



B.H. DIAGRAH CONSISTS OF FOUR DISTINCT ARCS OF PARABOLA.

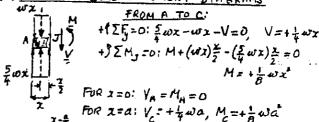


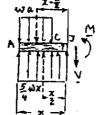
GIVEN: BEAM AND LONDING 3 WITH PE 3 Wa. (0) DRAY VAND M DIRERA (b) DETERMINE |V| AND



FREE BODY: ENTIRE +12 F, =0: Wg (44)-2WA-3WA

(a) SHEAR AND BENDING - MOMENT DIA FRAMS



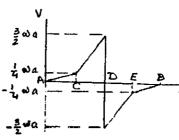


FROM C TO D +1 IF, =0: Zwx -wa-V=0 $+3\Sigma M_T = ot$ M+wa(x-4)- 2 wz(3) =0 M=== wx - wa(z-a)

(P)

FOR x = a: $V_c = +\frac{1}{4}\omega a$, $M_c = +\frac{1}{8}\omega a^2$ FOR z = 2a: $V_0 = +\frac{3}{3} \omega a$, $M_0 = + \omega a^2$

BECAUSE OF THE SYMPLETRY OF THE LOADING, WE CAN DEM. THE VALUES OF VANDM FOR THE RIGHT-MAND HALF OF THE EEAN FROM THE VALUES OPTAINED FOR ITS LEFT-HAND HALF

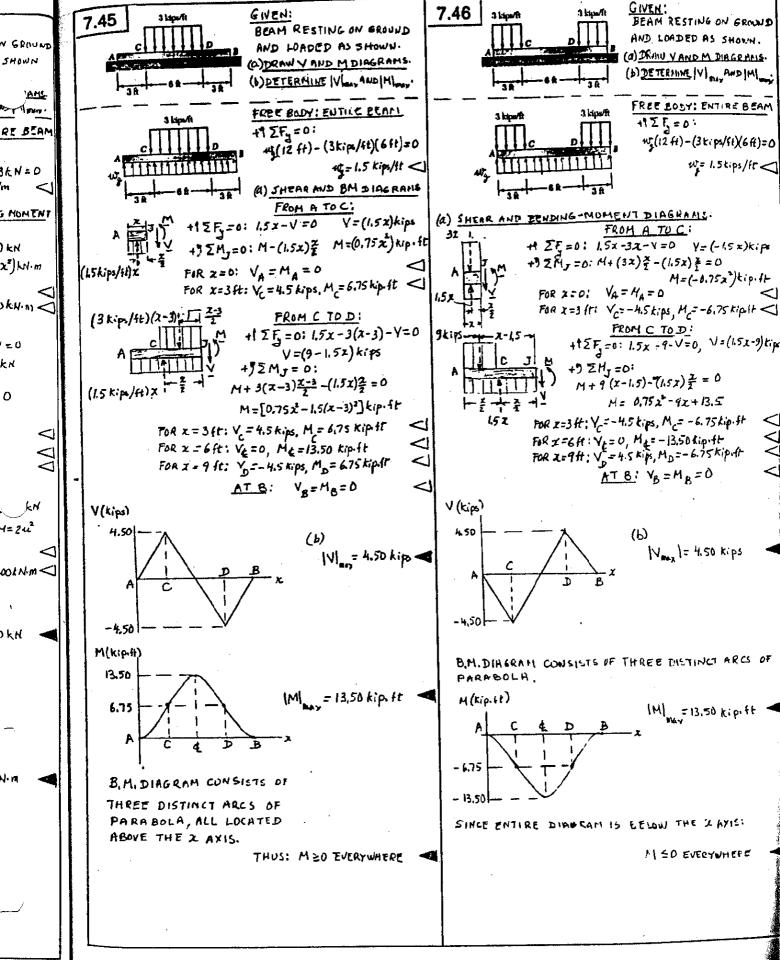


TO FIND IM MAN, WE DIFFERENTIATE EU.(1) AND SET AM = 0:

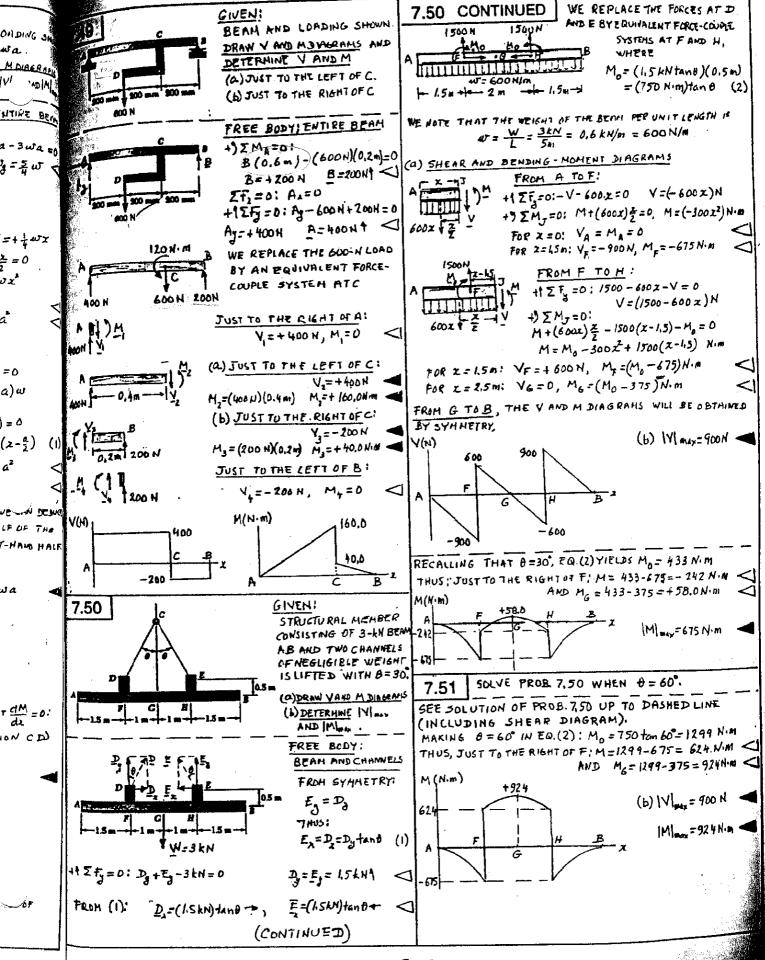
dH = 5wx-wa=0, x=4a <a (OUTSIDE PORTION CD) THE HAX. VALUE OF M OCCURS AT D:

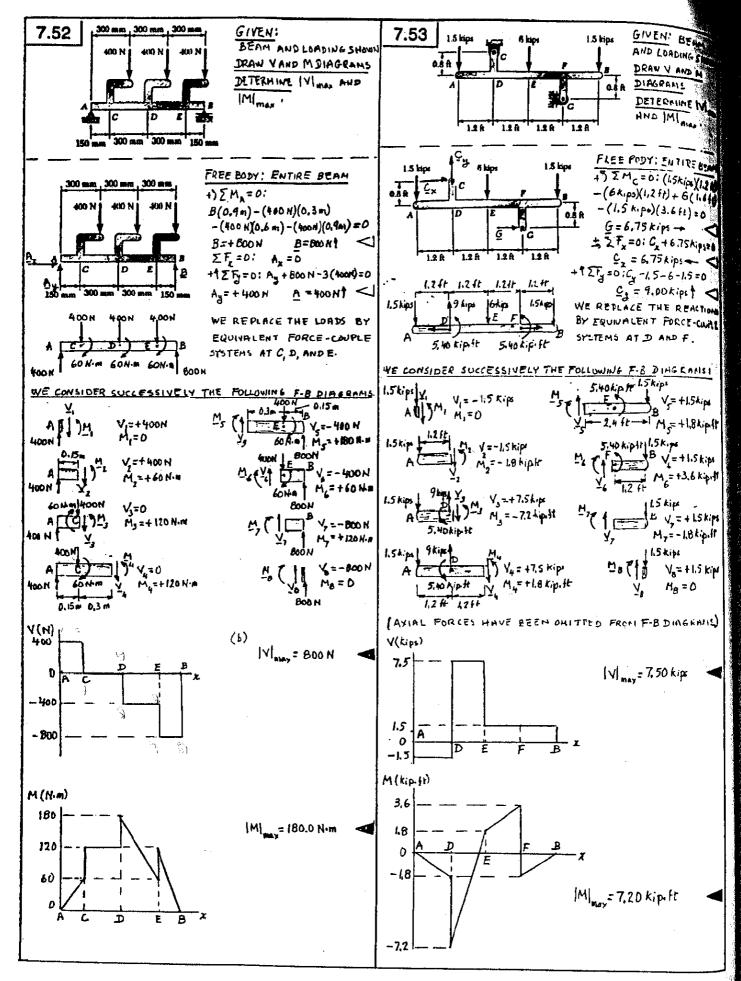
MIMAY = wa

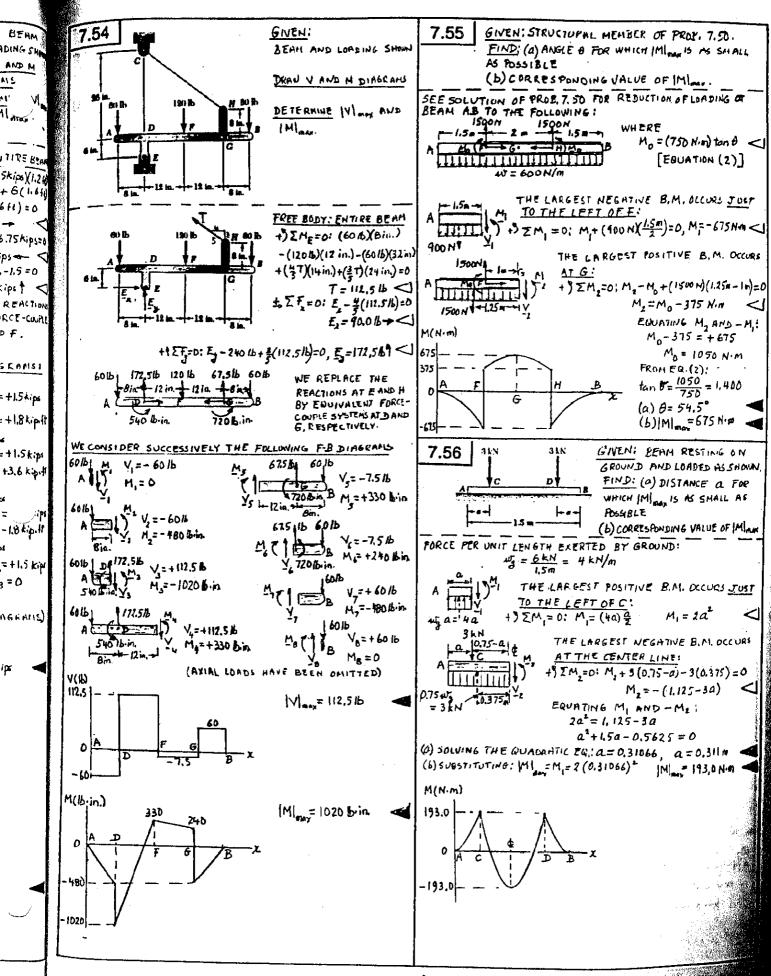
B.M. DIAGRAM CONSISTS OF FOUR DISTINCT ARCS OF PARA BOLA.



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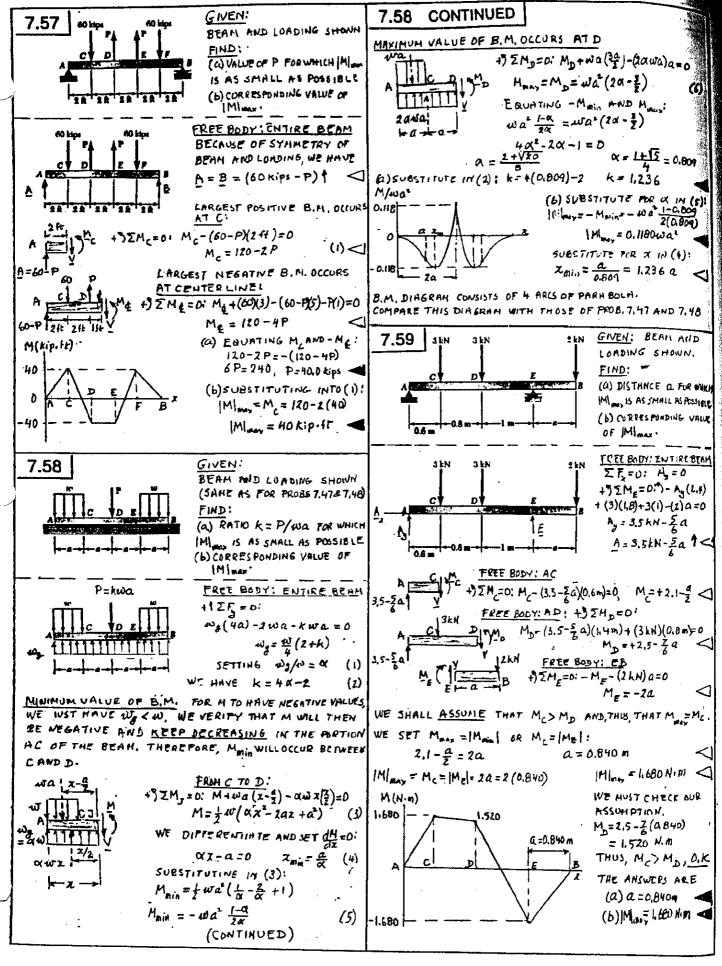


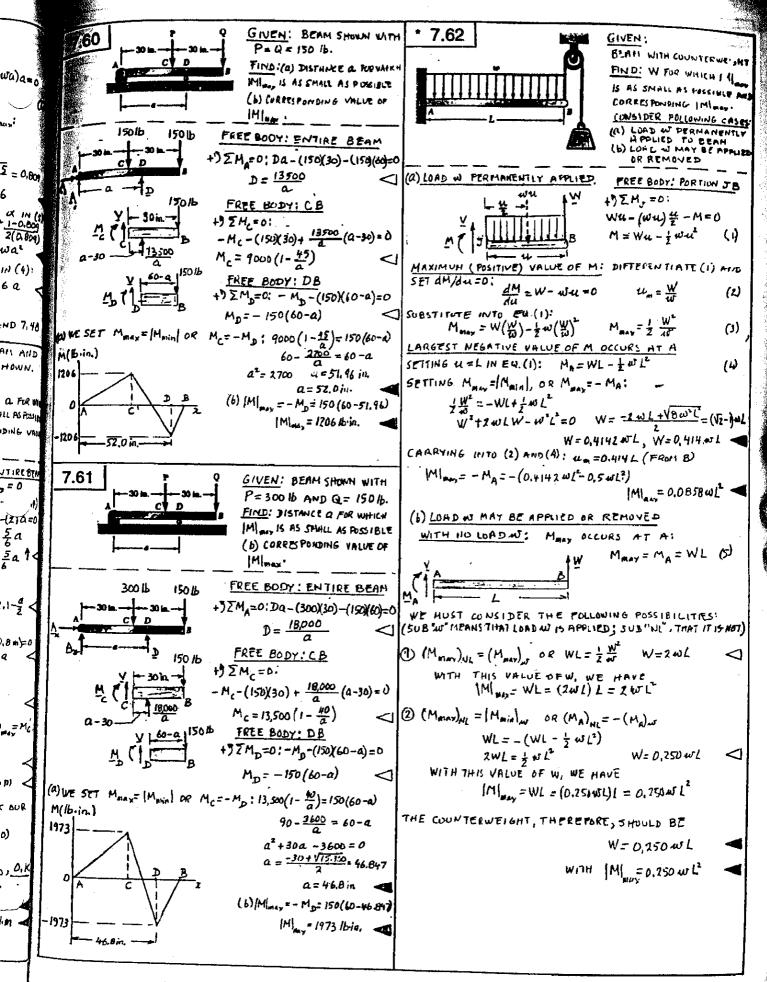


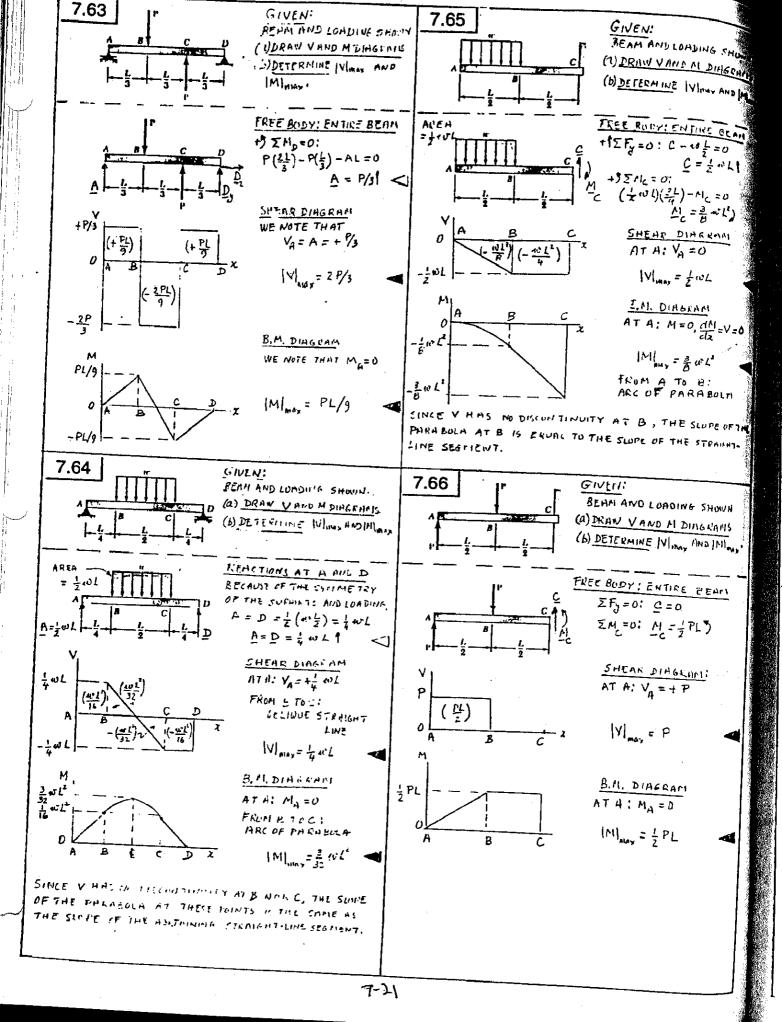
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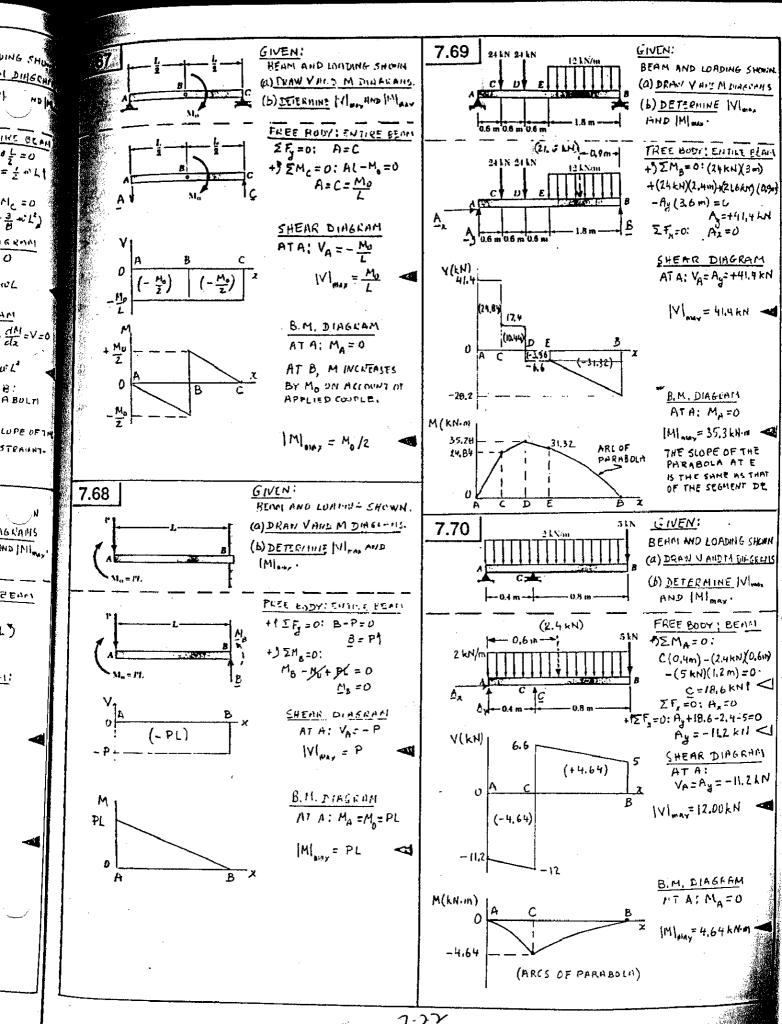
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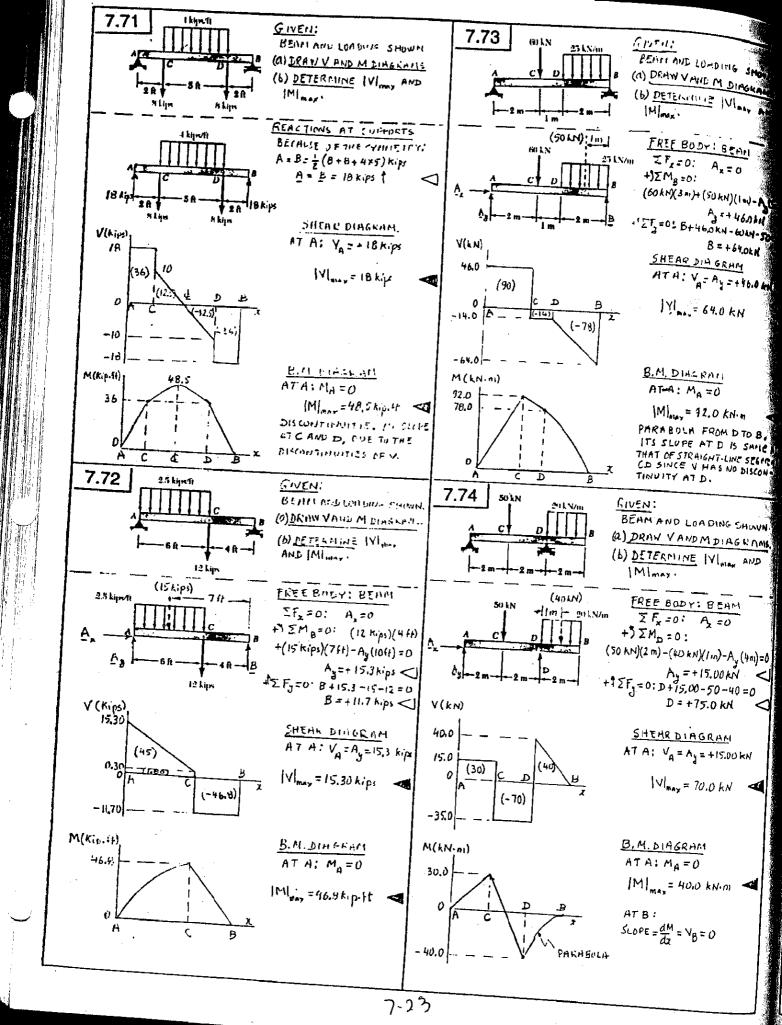
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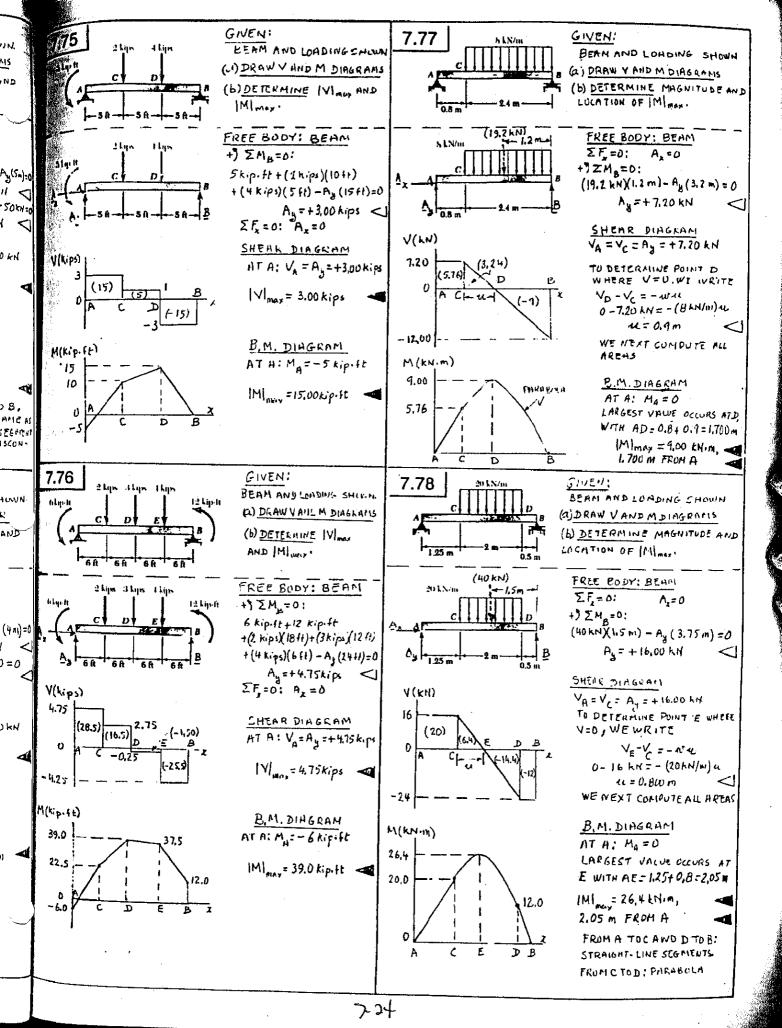


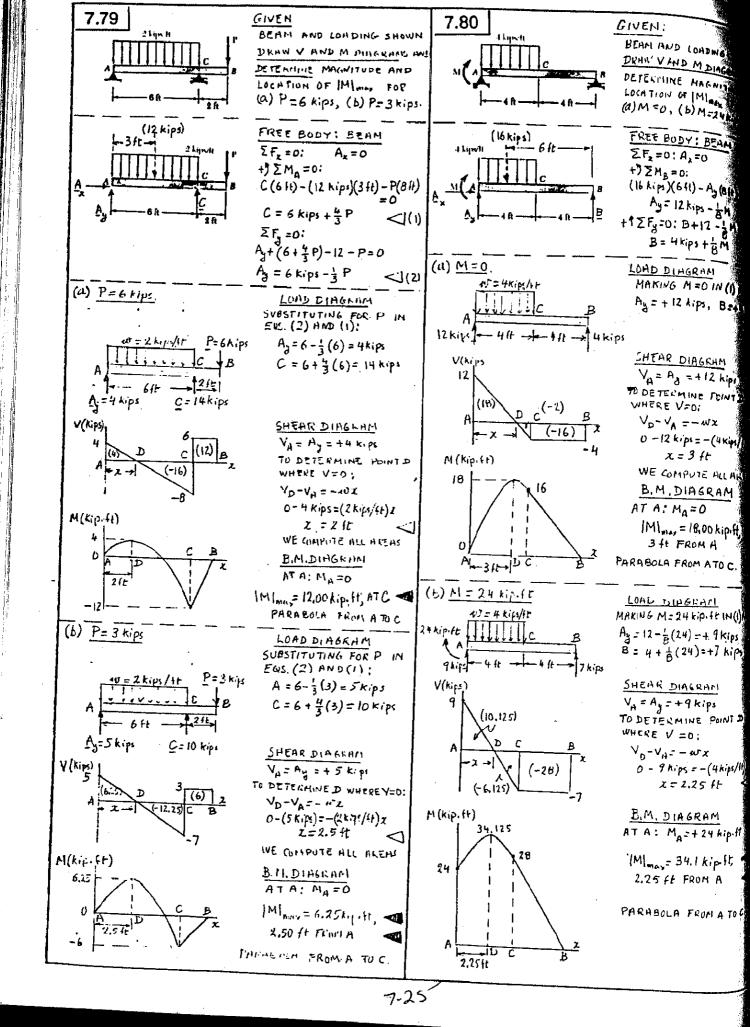


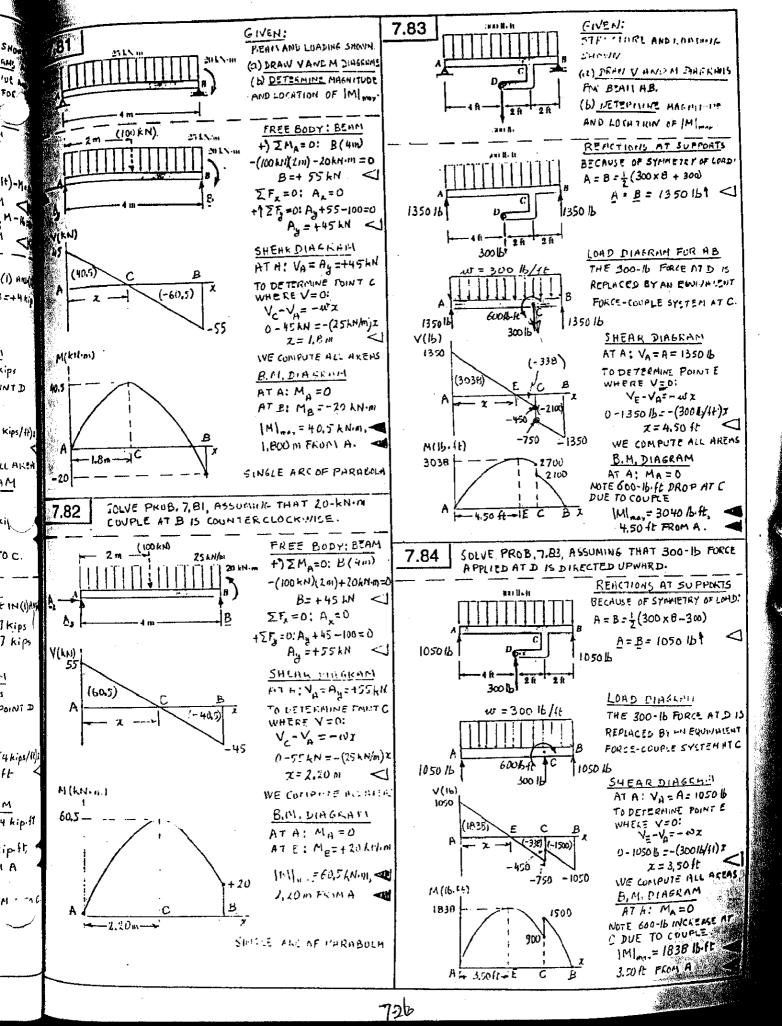


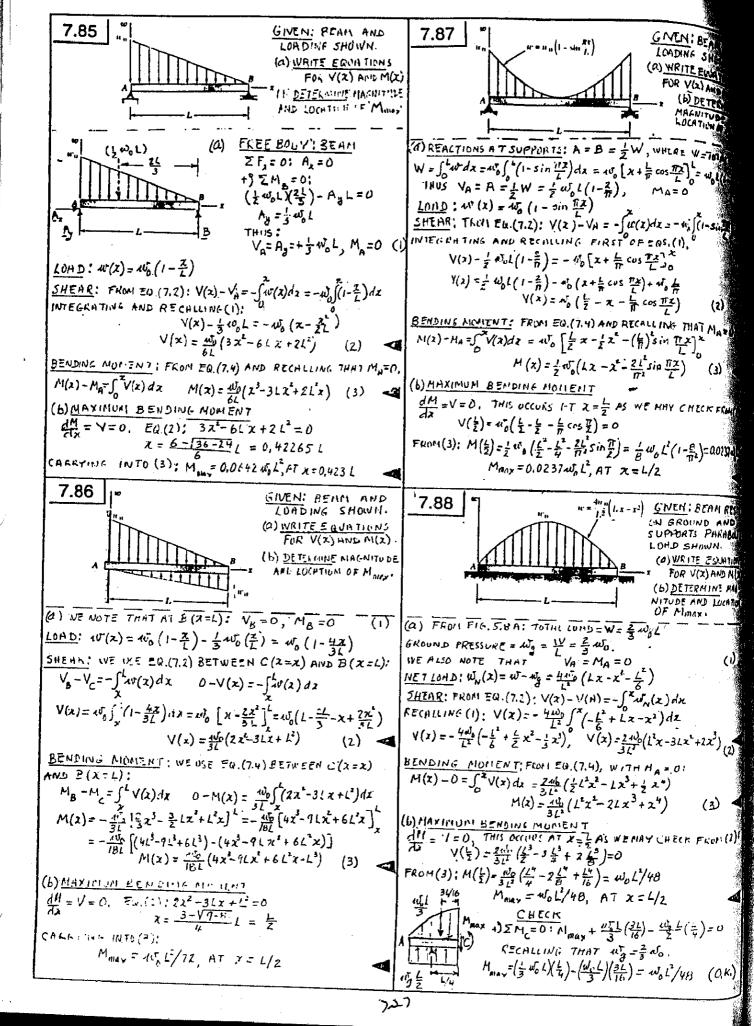


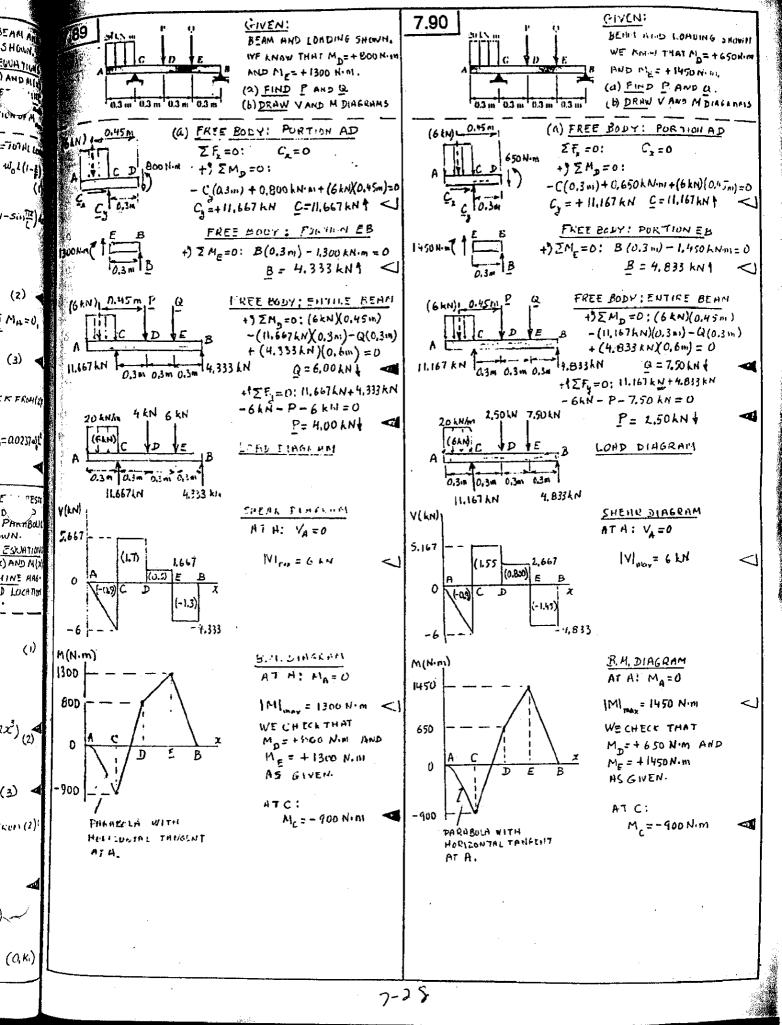


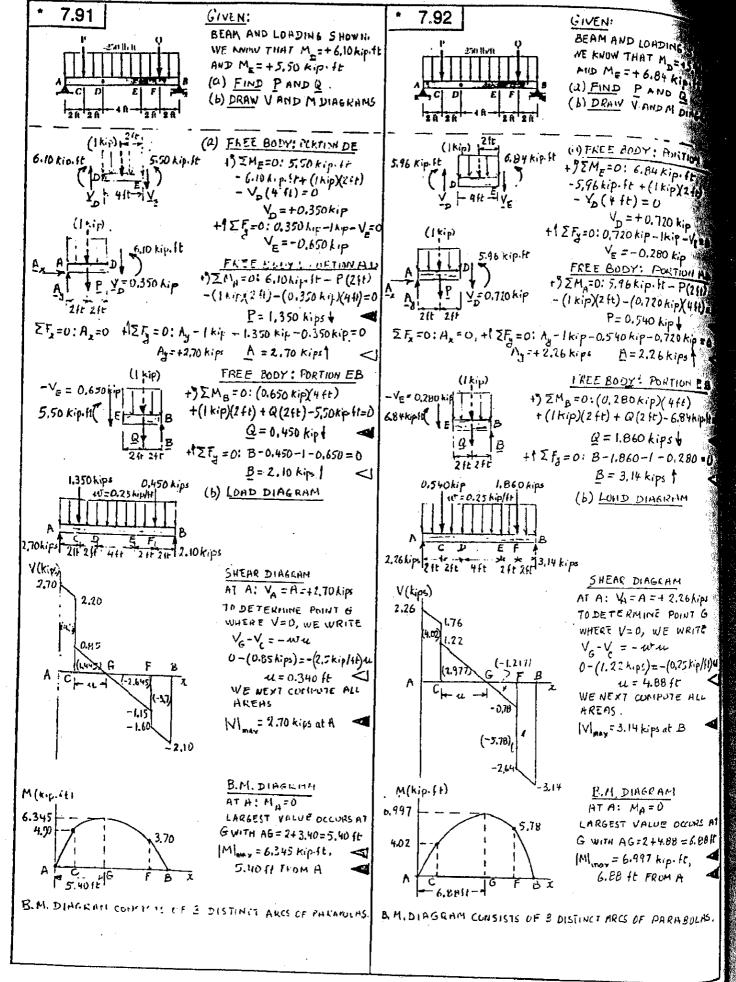


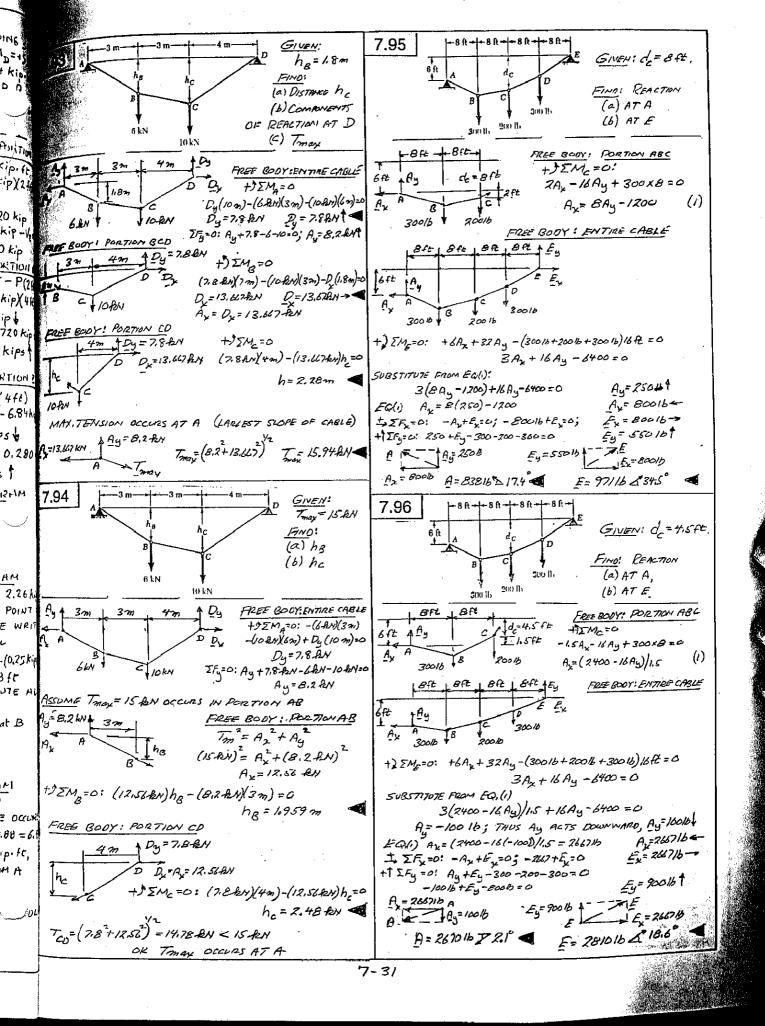


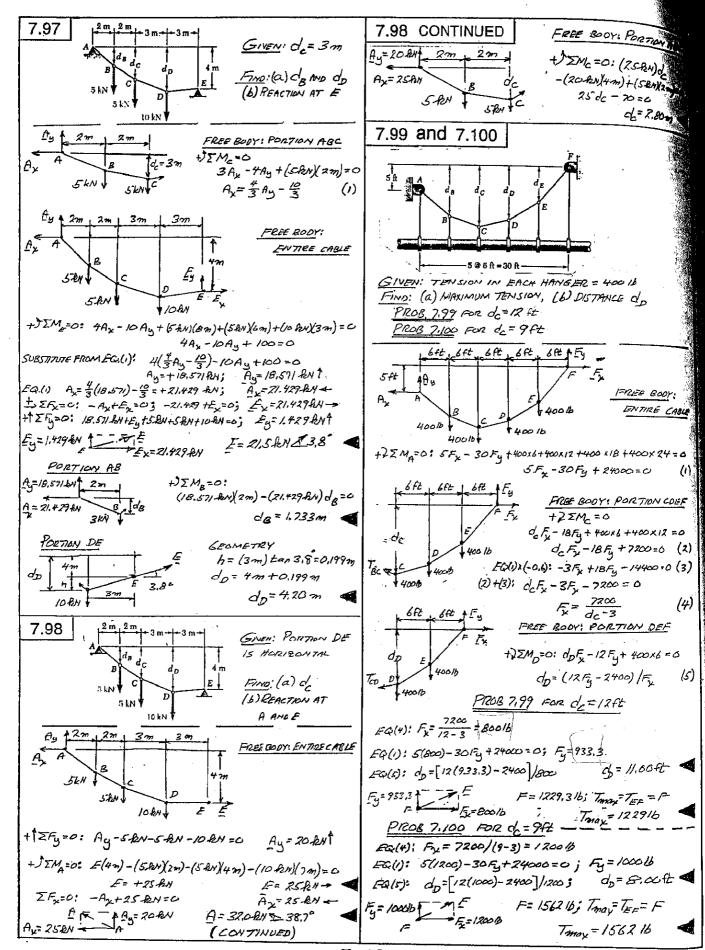


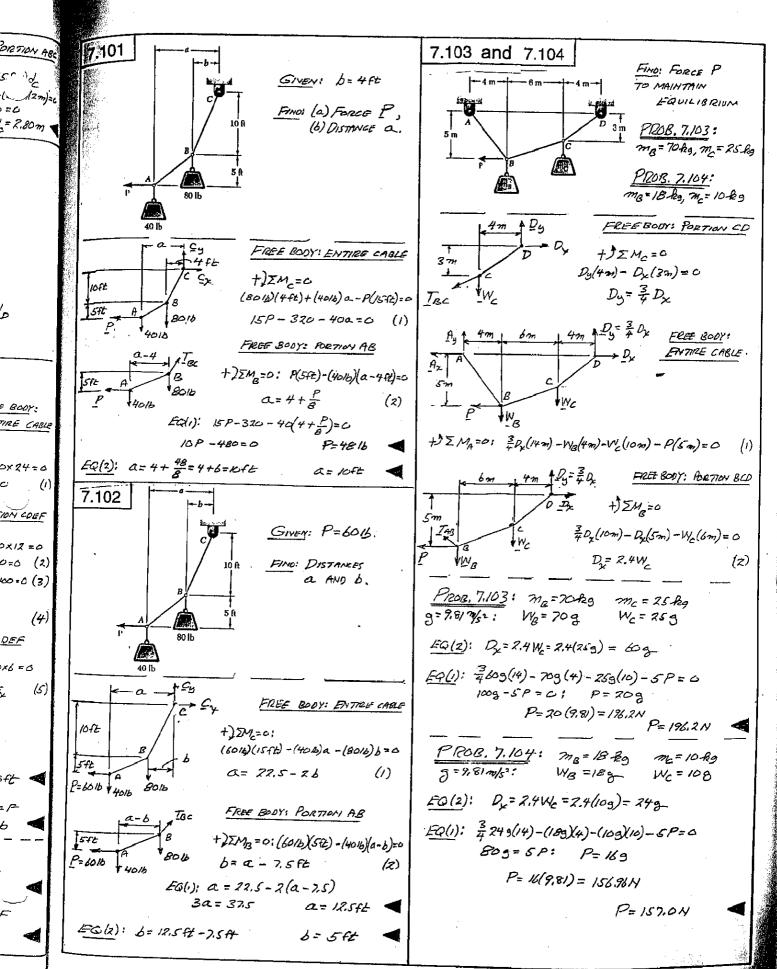


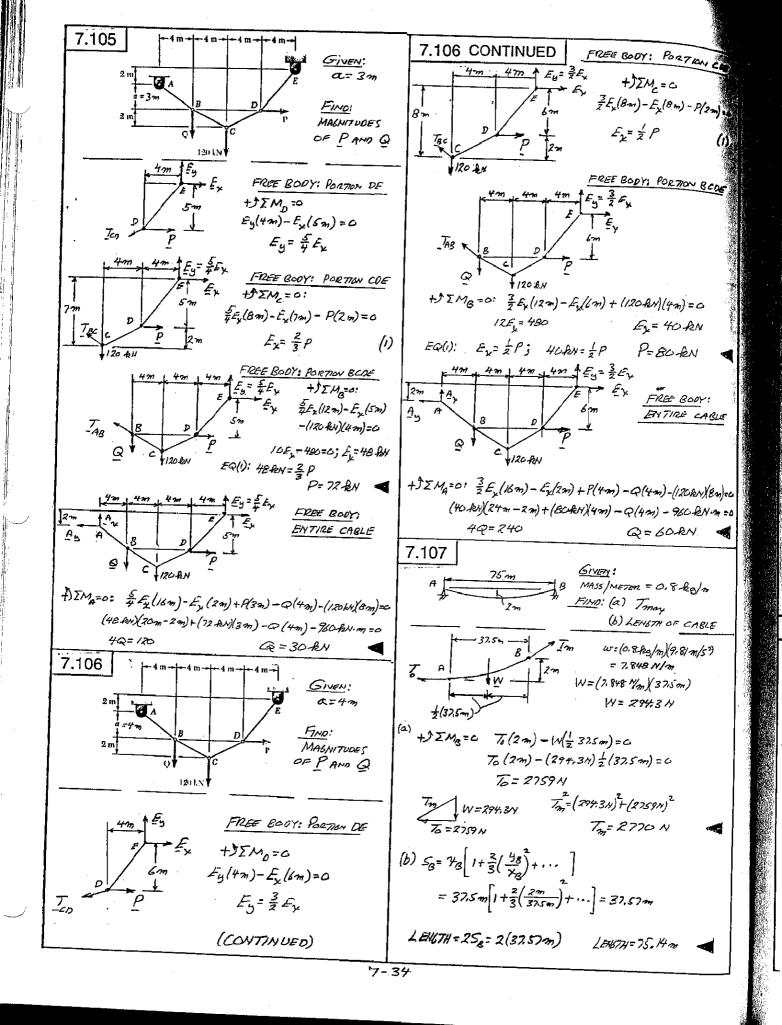


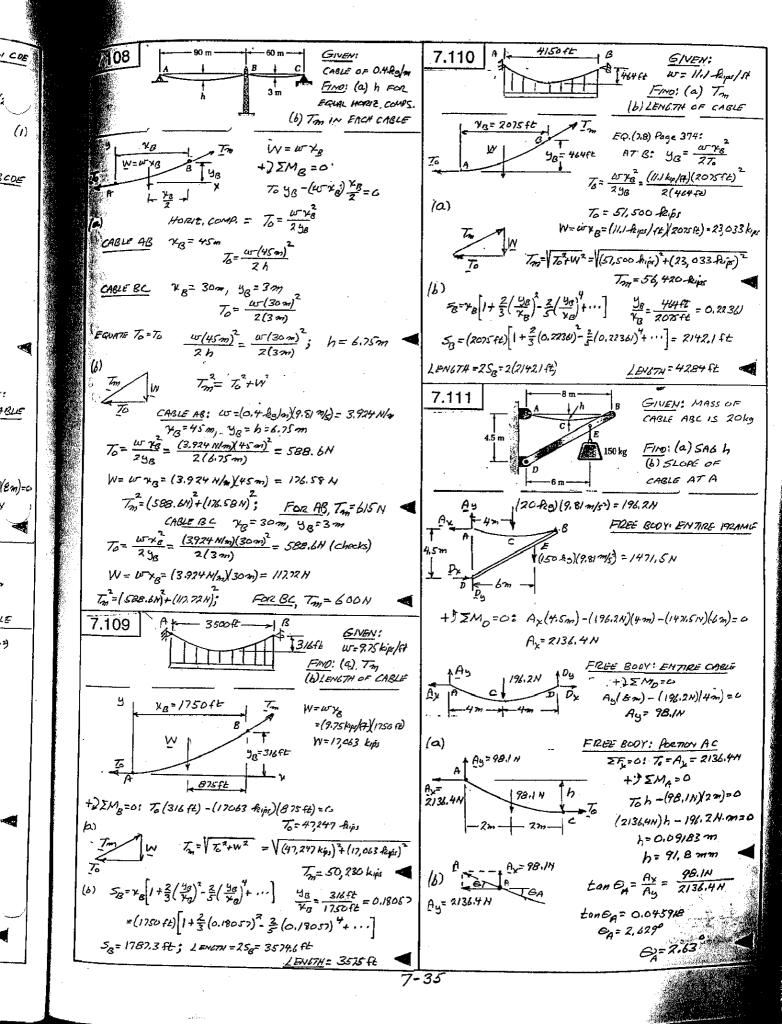


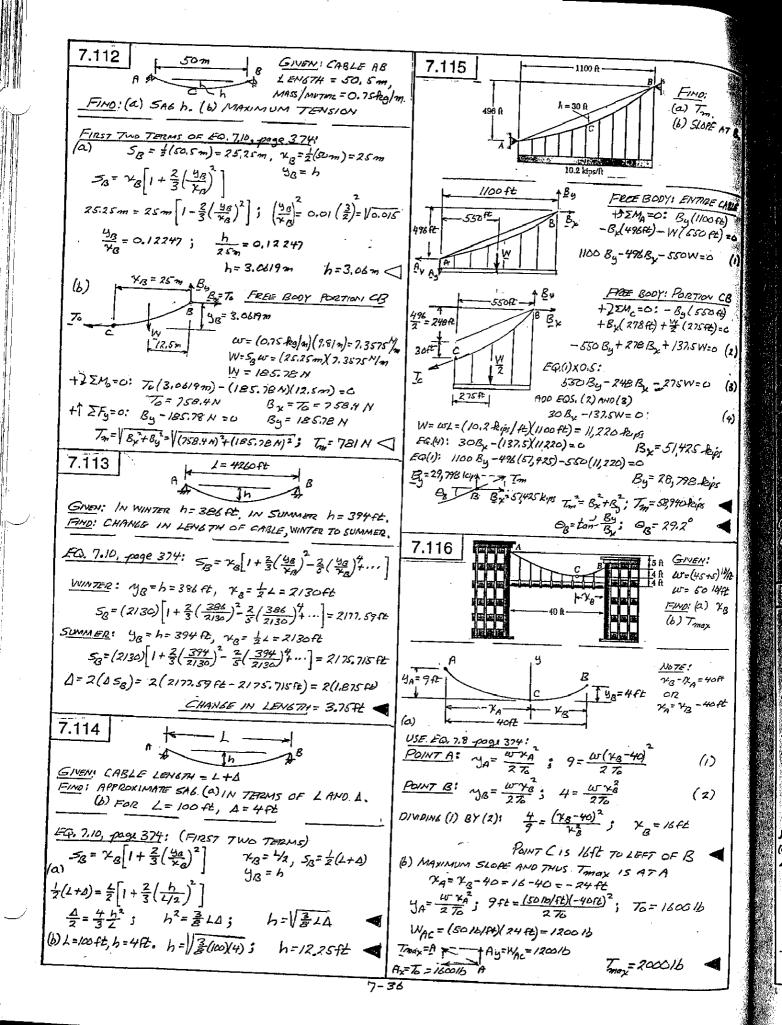


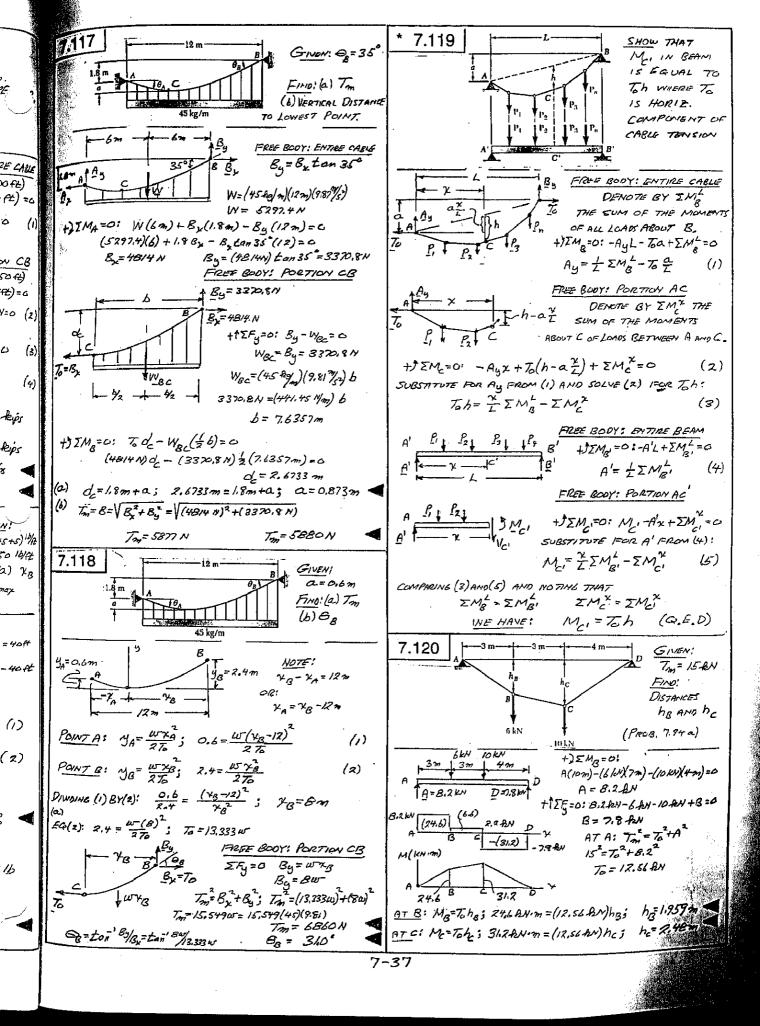


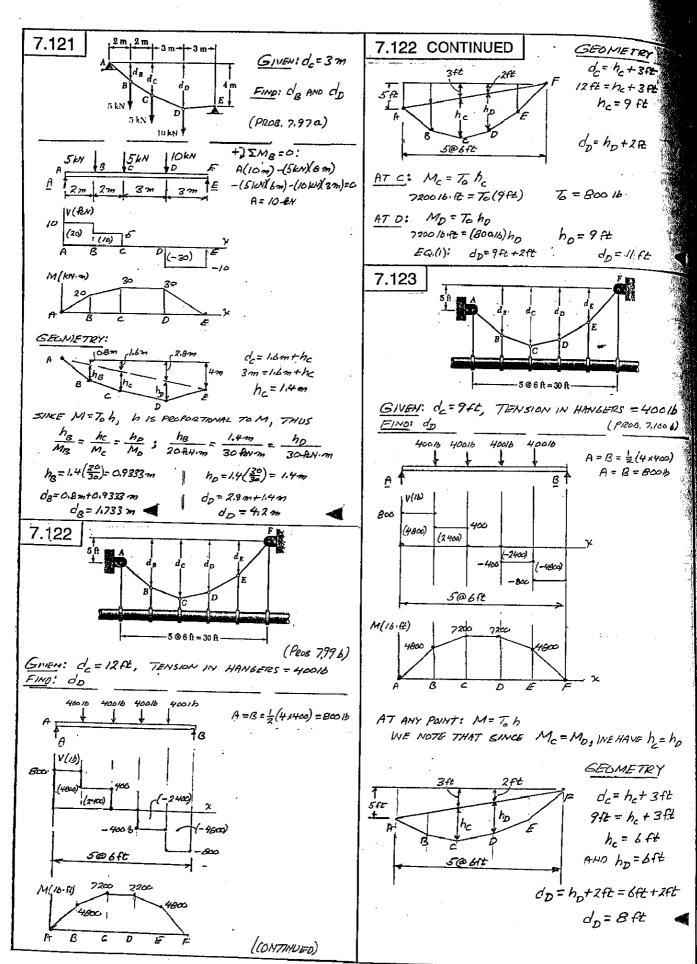


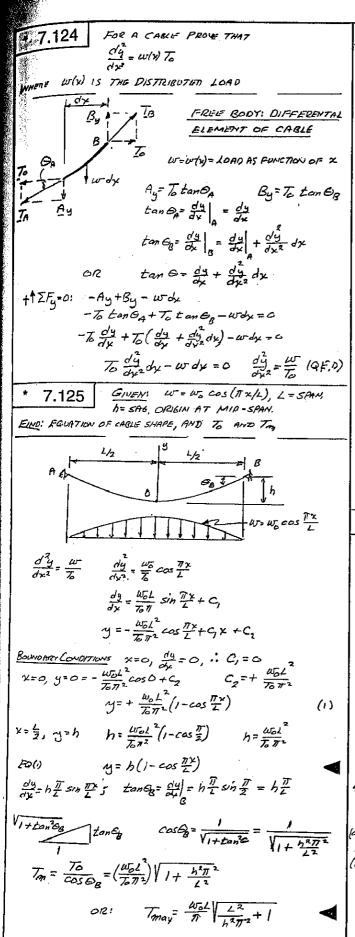










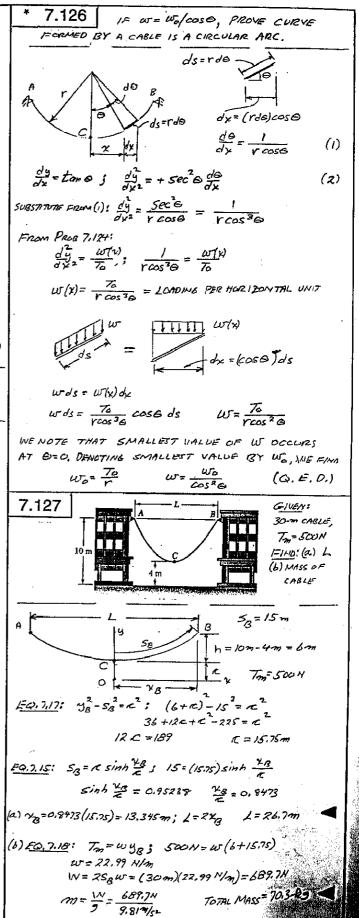


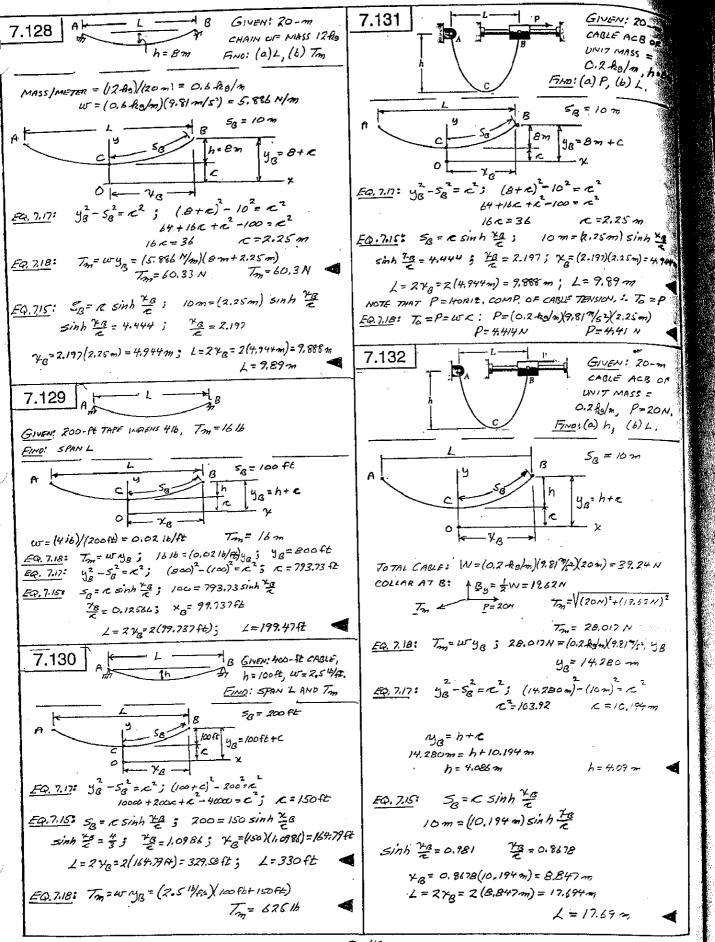
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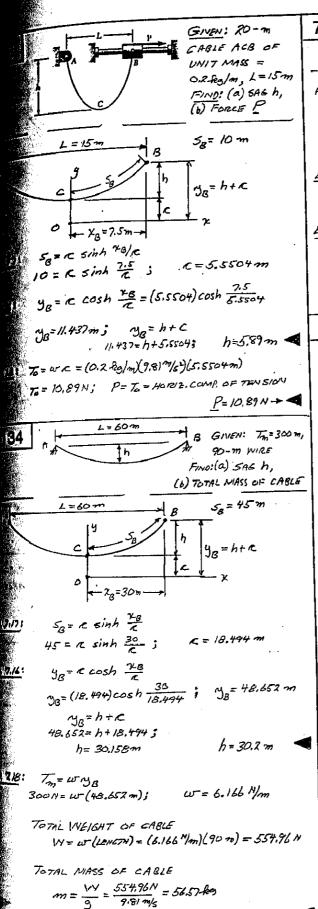
EQ. 7.1

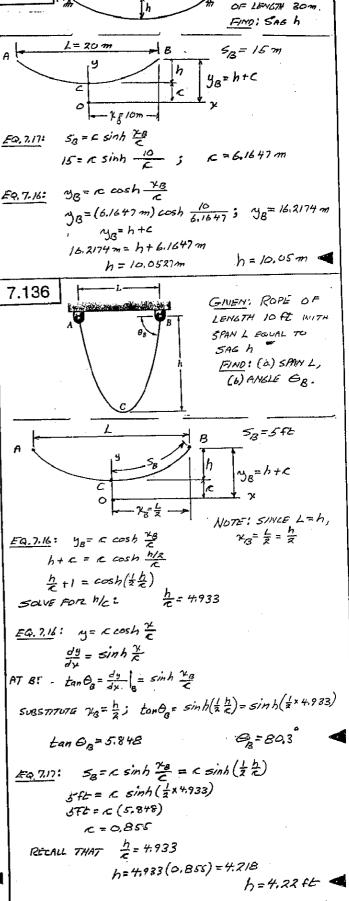
FQ. 7.10

FQ. 7.1

7.1

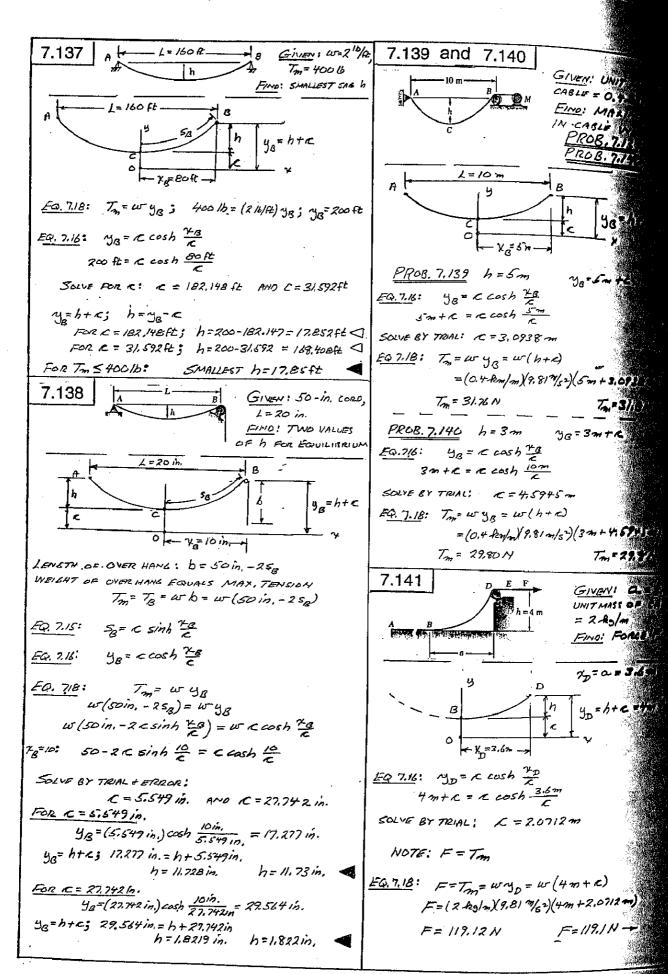
Eq.

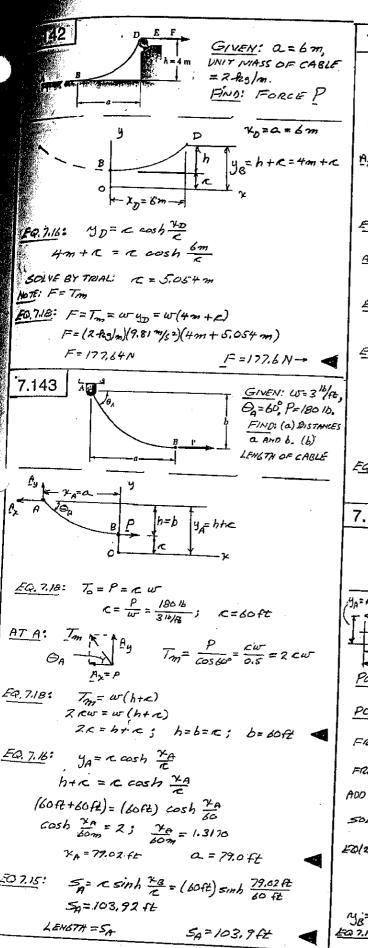


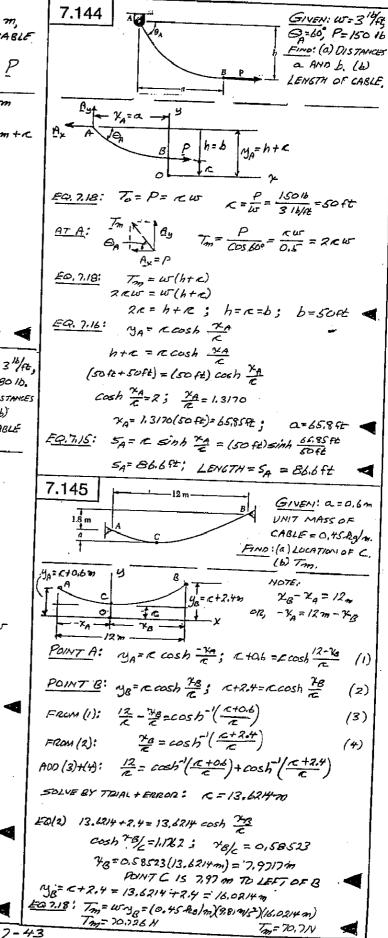


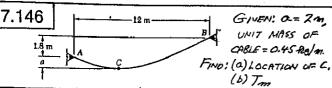
B GIVEN: CARLE

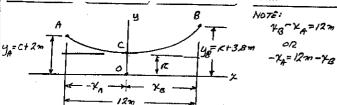
m=56.6 Rg











From (i):
$$\frac{12}{K} - \frac{4g}{K} = \cosh^{-1}\left(\frac{K+2}{K}\right)$$
 (3)

FROM(2):
$$\frac{\gamma_B}{\epsilon} = \cosh^{-1}\left(\frac{\epsilon + 3B}{\epsilon}\right) \tag{4}$$

$$ADD(3)+(4)$$
: $\frac{12}{6} = COSh^{-1}(\frac{K+2}{K}) + COSh^{-1}(\frac{K+38}{K})$

SOLVE BY TRIAL AND ENROR: K=6,8154 m

Eq.(2):
$$6.8154m + 3.8m = (6.8154m) \cosh \frac{48}{2}$$

 $\cosh \frac{48}{2} = 1.5576 \frac{43}{2} = 1.0122$

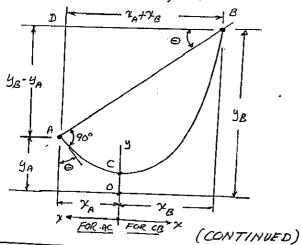
POINT (IS 6.90 m TO LEFT OF B

MB= K+3,8 = 6,8154+3,8 = 10,6154m EQ(7.18): Tim = 10 yB = (0,45 holan)(9,81 %/52)(10.6154 m) Ton= 46,86 N Tm=46.9N

*7.147 and 7.148



COLLAR AT A: SINCE y=0, CABLE I ROD



*7.147 and 7.148 CONTINUED

POINT A:
$$y = c \cosh \frac{x}{c}$$
; $\frac{dy}{dx} = \sinh \frac{x}{c}$
 $tan \theta = \frac{dy}{dx} = \sinh \frac{x_A}{c}$

$$x_{B} = \kappa \sinh^{-1} \left[\frac{10}{\kappa} - \sinh \frac{x_{A}}{\kappa} \right] \qquad (2)$$

$$y_{A} = \kappa \cosh \frac{x_{B}}{\kappa}$$
 $y_{B} = \kappa \cosh \frac{x_{B}}{\kappa}$ (3)

$$\frac{IV \triangle ABD}{V_R + V_A} = \frac{y_B - y_A}{y_R + y_A}$$
 (4)

METHOD OF SOLUTION:

FOR GIVEN VALUE OF B, CHOOSE TRIAL

VALUE OF A AND CALCULATE:

FROM EC(1): ZA

USING VALUE OF XA. AND K, CALCULATE:

1720M EQ(2): 74B

FROM EQ(3): YA AND YE

SUBSTITUTE VALUES OBTAINED FOR TA, LB, JA, JB

INTO EQLA) AND CALCULATE &

CHOOSE HEW TRIAL VALUE OF & AND REPEAT ABOVE PROCEDURE UNTIL CALCULATED

VALUE OF G IS EQUAL TO GIVEN VALUE OF G.

PROB.7.147: GIVEN VALUE: 6=30"

RESULT OF TRIAL AND EIRROR PROCEDURG C=1.803 m

74= 2.3745 m 74 = 3.6937 m

44 = 3,606 m

a=y=y4=7.109m-3.606m=3.503m a = 3,50 m

PROB. 7.148: GIVEN VALUE: @ = 45° RESULT OF TRIAL AND ERROR PROCEDURE C= 1.8652m

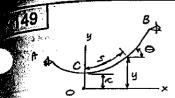
7A= 1.644 m

7-12=4.064m

MA= 2.638 m

7B= 8.346 m

a= y8 - y4 = 8,346 m - 2.638 m = 5.708 m a = 5.7/ m



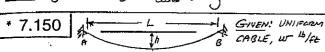
GIVEN: UNIFORM CABLE

<u>Prove</u>: (a) S=rc tan €. (b) y=rc sec €.

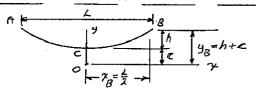
$$\cosh \frac{x}{E} = \sqrt{1 + \sinh^2 \frac{x}{E}} = \sqrt{1 + \tan^2 \Theta}$$
 (1)

$$\sqrt{1+\tan^2\theta}$$
 $\tan\theta$ $\cos\theta = \frac{1}{\sqrt{1+\tan^2\theta}}$ (2)

SUBSTITUTE (2) INTO (1):
$$\cosh \frac{v}{c} = \frac{1}{\cos \theta}$$
 (3)



FIND: (a) MAXIMUM SPAN FOR GIVEN VALUE Tom
(b) MAXIMUM SPAN FOR UF= 0,2516/ft AND Tom= 800016



WE SHALL FIND RATIO (48/2) FOR WHICH Tom IS MINIMUM

$$\frac{dT_m}{d(x_{g_{\ell}})} = \omega x_{g} \left[\frac{1}{x_{g_{\ell}}} \sinh \frac{x_{g}}{\pi} - \left(\frac{1}{x_{g_{\ell}}} \right)^2 \cosh \frac{x_{g}}{\pi} \right] = 0$$

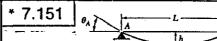
SOLVE BY TRULL AND EDRON FOR:
$$\frac{\chi}{\kappa} = 1.200$$
 (1)

$$\frac{E0.7/7}{198} \cdot y_{B}^{2} - s_{B}^{2} = c^{2} \cdot y_{B}^{2} = c^{2} \left[1 + \left(\frac{s_{B}}{c} \right)^{2} \right] = c^{2} \left(1 + 1.509^{2} \right)$$

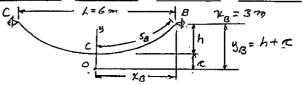
$$4 \cdot y_{B} = 1.810 c$$

EG(1): 4 = 1,509 C= 1,509 Tay/1,8100 = 0,6130 Ton

(b) FOR W= 0.25 HA AND Tom= 8000/6,



GIVEN: UNITMASS = 3 Agla, L=6 m FIND: Two VALUES OF h FOR WHICH Ton= 350 N



w=(3kg/n)(9,81m/s2)= 29.43 N/m

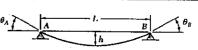
SOLVE BY TRIAL AND ETROOR FOR TWO VALUES OF IC

h= ye - 1. h= 11.893m - 11.499 m

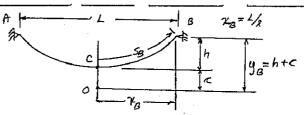
h=0.394m

C= 11.499.m





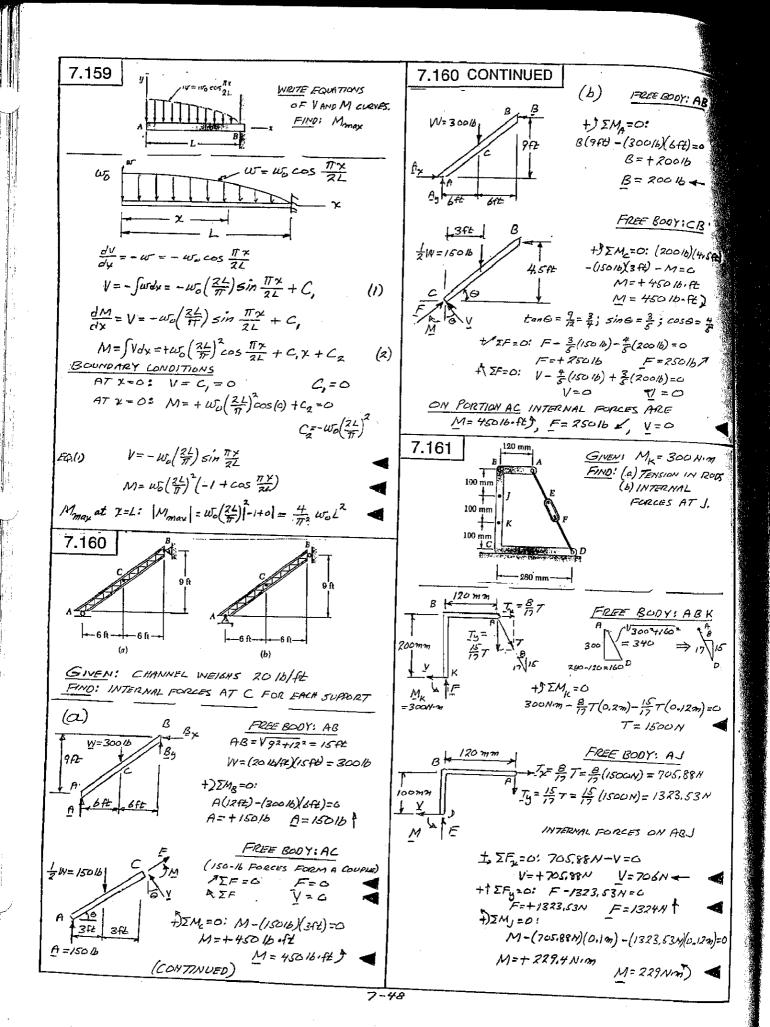
FIND THE ML RATIO FOR TOTAL WEIGHT EQUAL TO Tm.

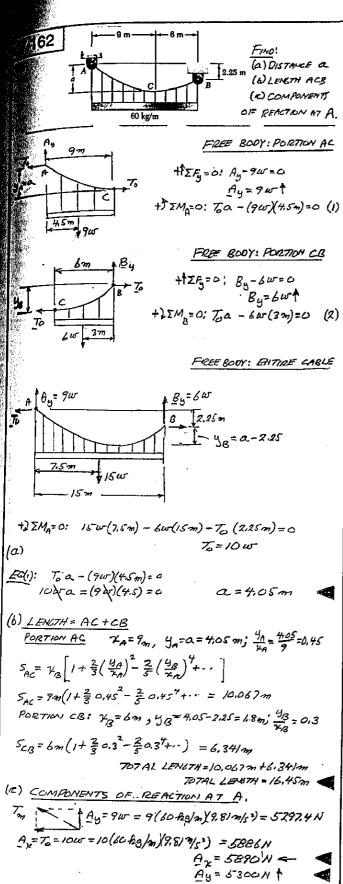


TOTAL WEIGHT: W= (250) W; : Ton= 250 W

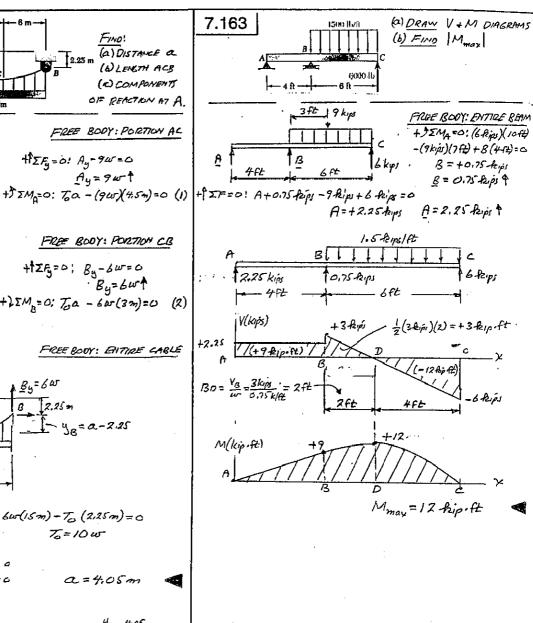
$$\tanh \frac{4a}{c} = \frac{1}{2} \quad \text{i} \quad \frac{7a}{c} = 0.5493 \quad \text{(1)}$$

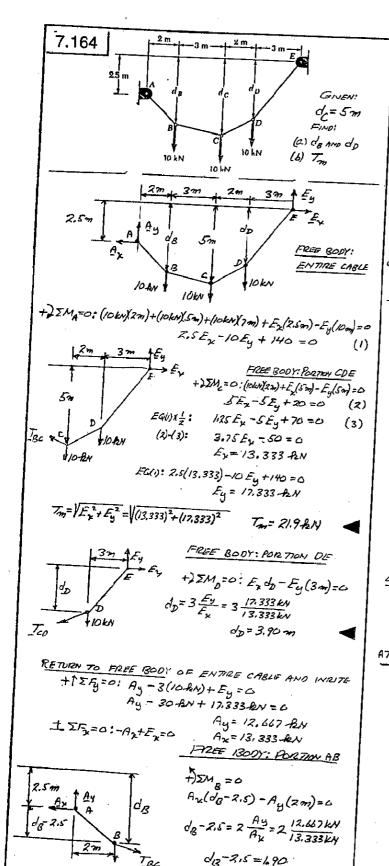
$$h = y_B - R = R \cosh \frac{\gamma_B}{c} - R = R \left[\cosh(0.5493) - 1 \right]$$

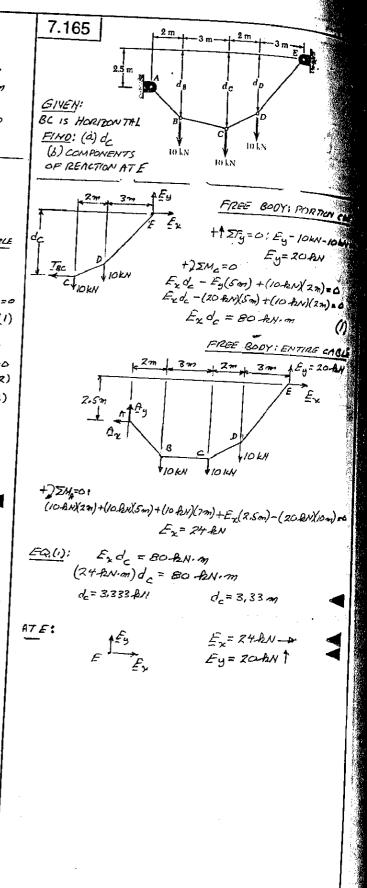




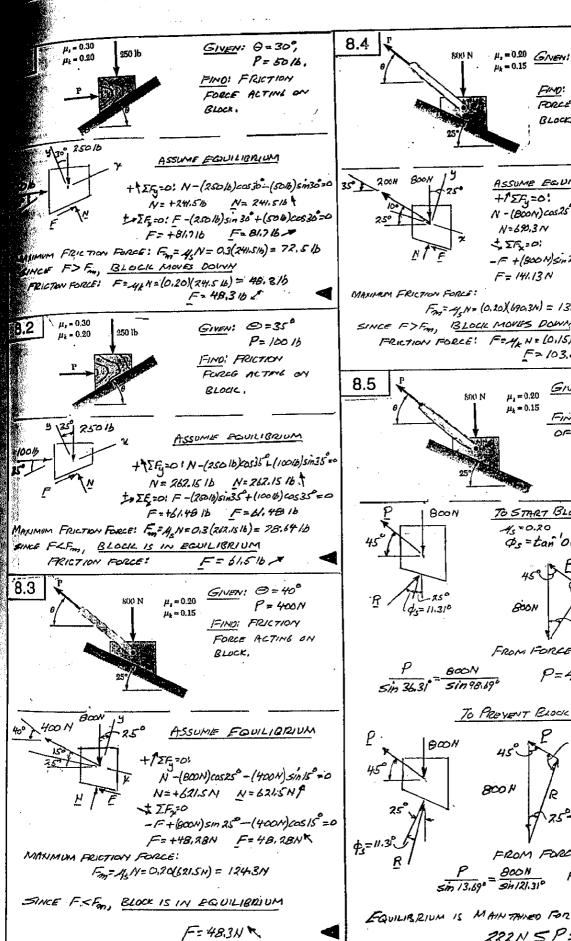
(2.)

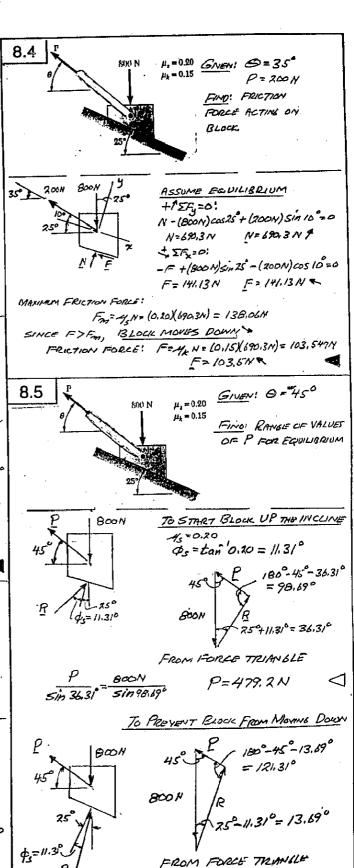






dg=4,40m





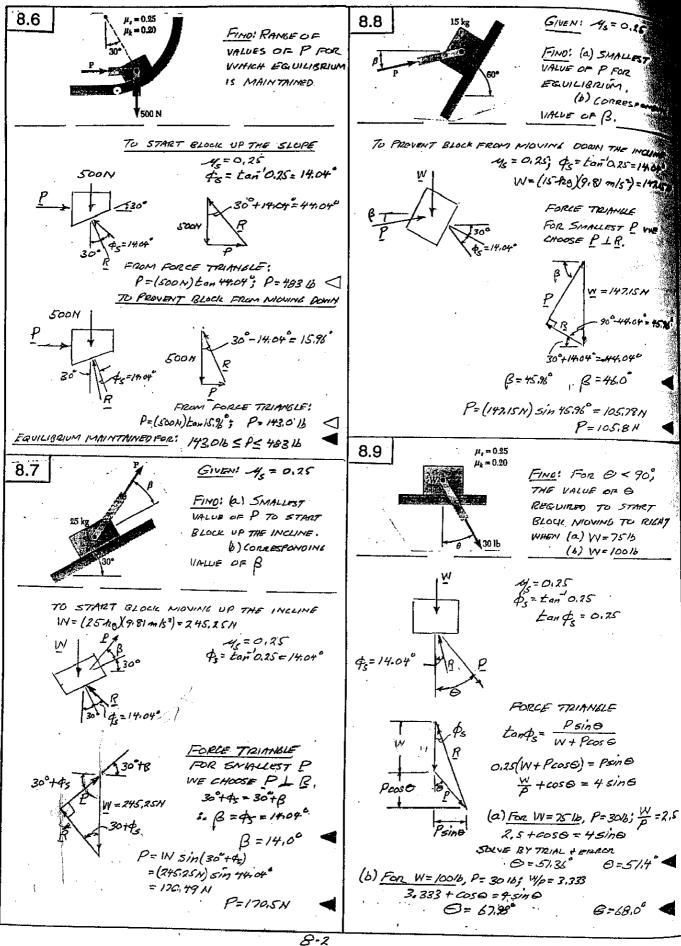
sin 13.69° = 800 N

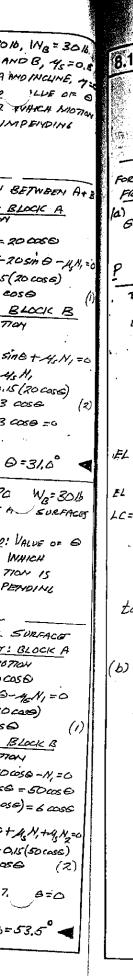
Sh 121.31°

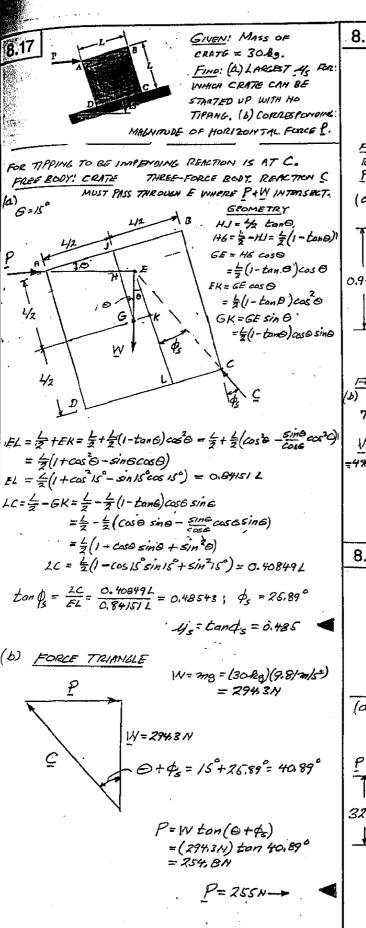
222N SP & 479N

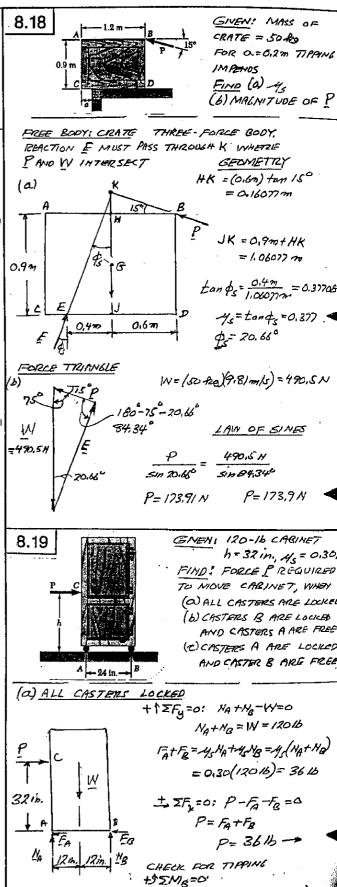
P= 221.61N

 \triangleleft





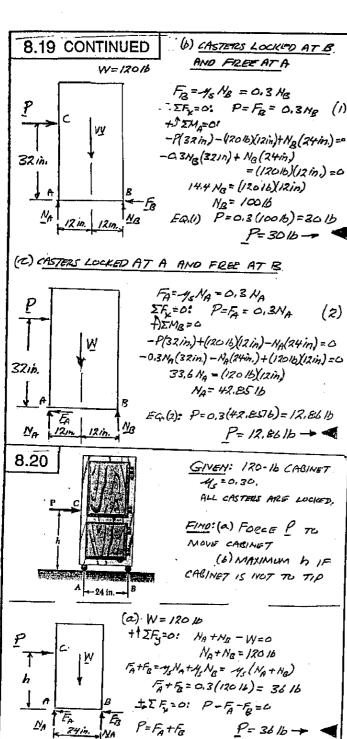


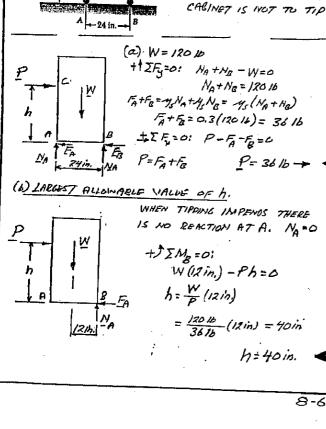


(12016)(12in.) -(3616)(32in) -140(24in)=0

(CONTINUED)

NA=+1216>0





r = RADIUS. GIVENI W= WEIGHT, 45 15 SAME AT A AMO

FIND: LARGET MIF CYLINDER IS NOT TO ROTH

W **∀**_ r F_B

8.21

8.22

SINCE MOTION INILL IMPEND FA=1/5 NA FB=45NB

DEM =0: M- FA - rN =0 M=rN+rE= rN+rys NA M= rNA(1+46)

+, IF, = 0: NA-F8=0; NA=MSNB (2) + TF4=0: NB+FA-W=0; NB=W-15NA

SUBSTITUTE FOR NB FROM (3) INTO (2):

NA= 45 (W-45 NA) NA(1+4,2) = 4/5 W SUBSTITUTE FOR INA INTE (1):

M= Wrys (1+45) M= r 45 W (1+45)

GIVEN: Y = RADIUS W=WEISHT

. FIND! LARGEST M IF CYLINDER IS NOT TO ROTATE (a) FOR 4,=0, 4,8=0.30, (b) For 4=0.25, 48=0.30.

F=48 N8

(ı)

SINCE MOTION WILL IMPEND F=4ANA +) IMB=0: M-rf-- NA=0 M=rNA+rFA=rNA+ryaNA M= MA(1+4A)

\$\sum_{\chi} \sum_{\chi} = 0: N_A - F_B = 0 NA= MBNB (2)+ 1 IFy=0: NB+FA-W=0 (3)

NB=W-YANA

SUBSTITUTE FOR No FROM (3) INTO (2) NA = 48 (W-4A NA)

NA = 40W NA(1+MAMB)=MBW

EQ.(): M= + 48W (1+4A) M=WY 18(1+4A) 1+4A4B

(a) FOR MA = 0. AND MB = 0.30:

M=Wr 0,30

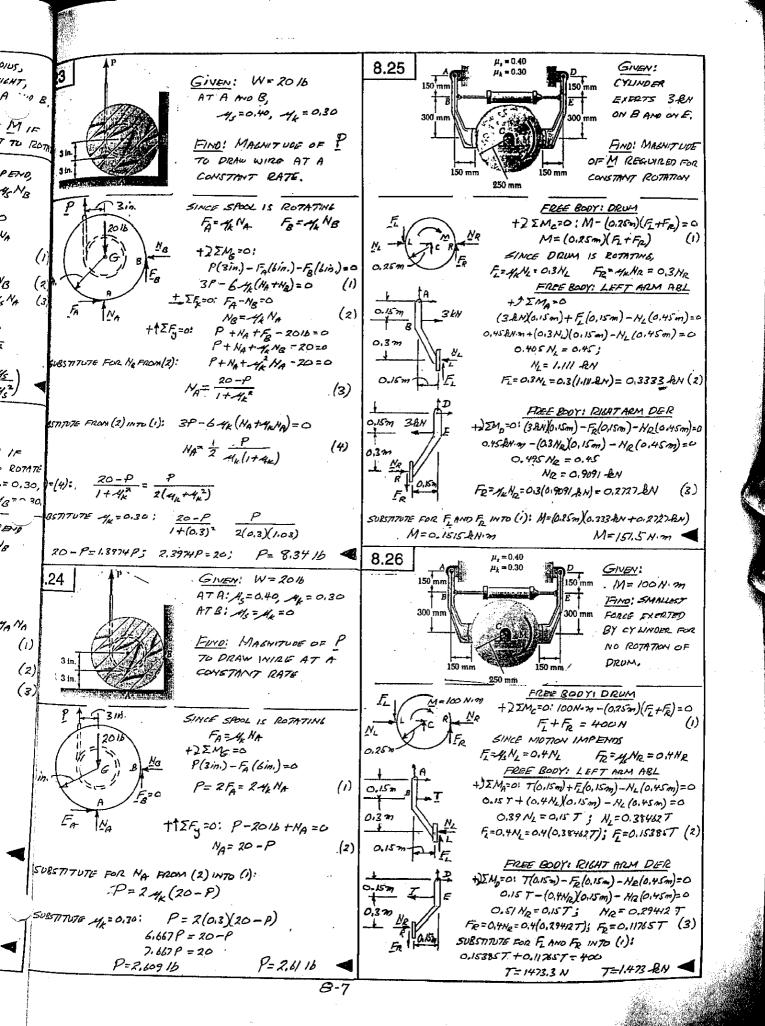
M=0,300 Wr

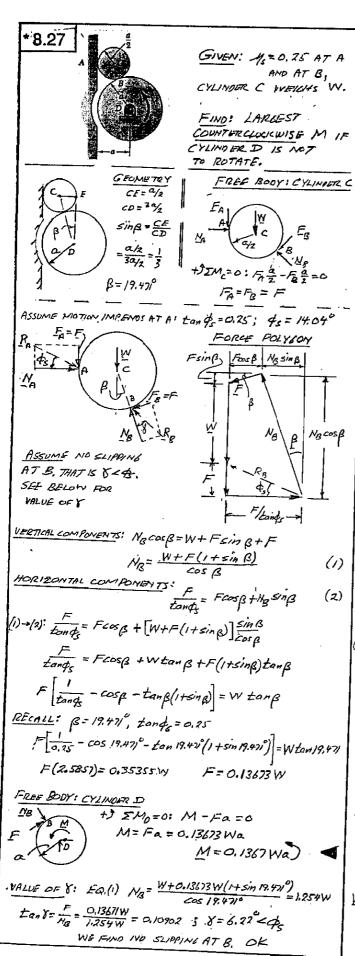
(b) FOR 4=0.25 AND MB=0.30:

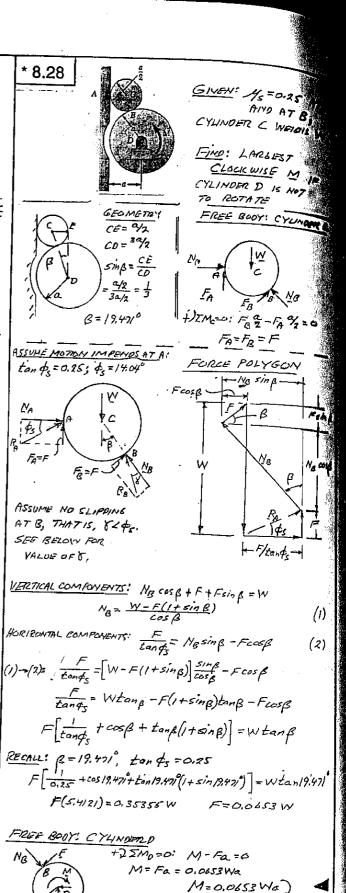
M= Wr (0.30)(1+0.25) = Wr (0.30)(1.25) 1+(0.25)(0.30)

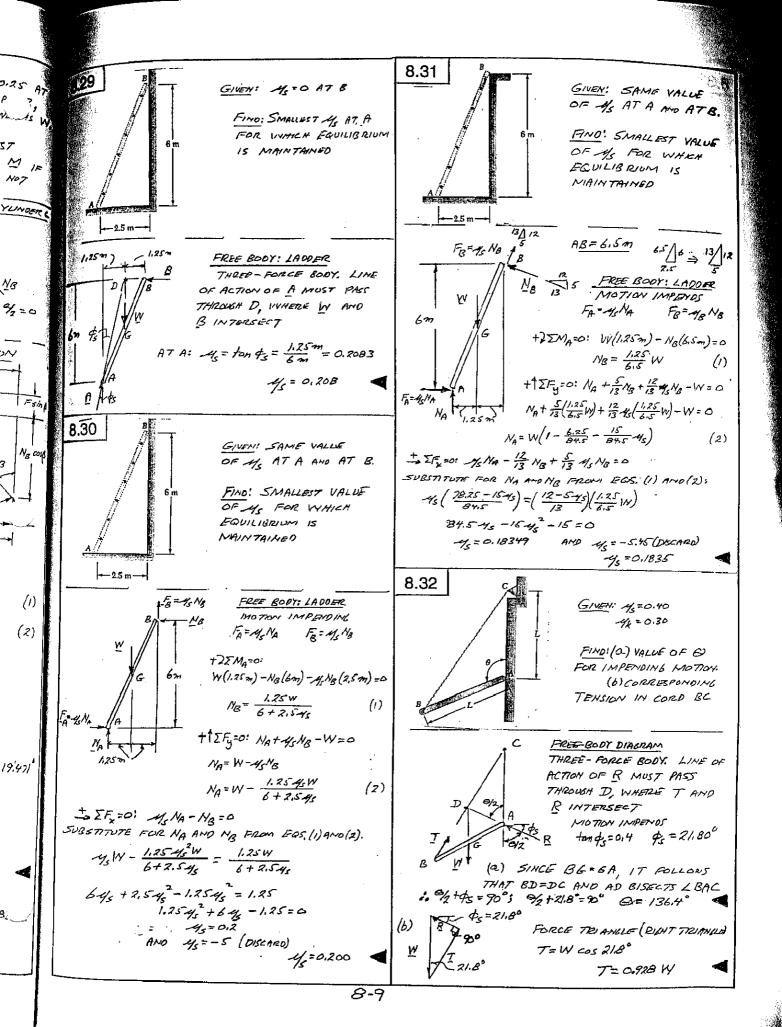
M=0,3488Wr

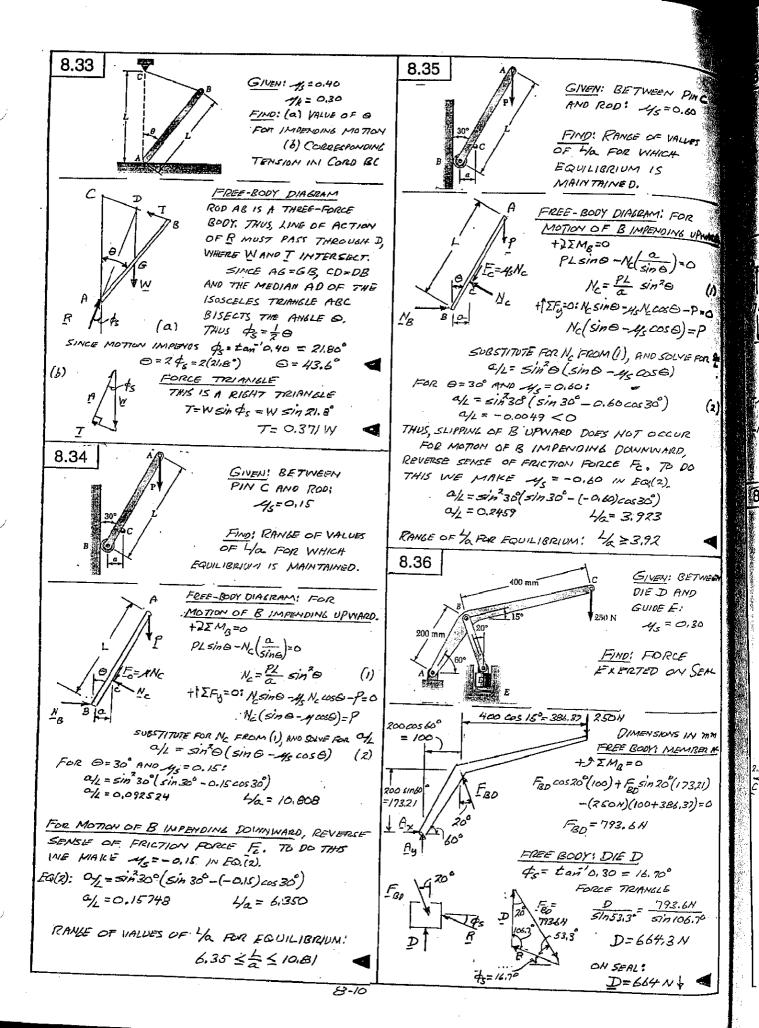
M=0.349Wr

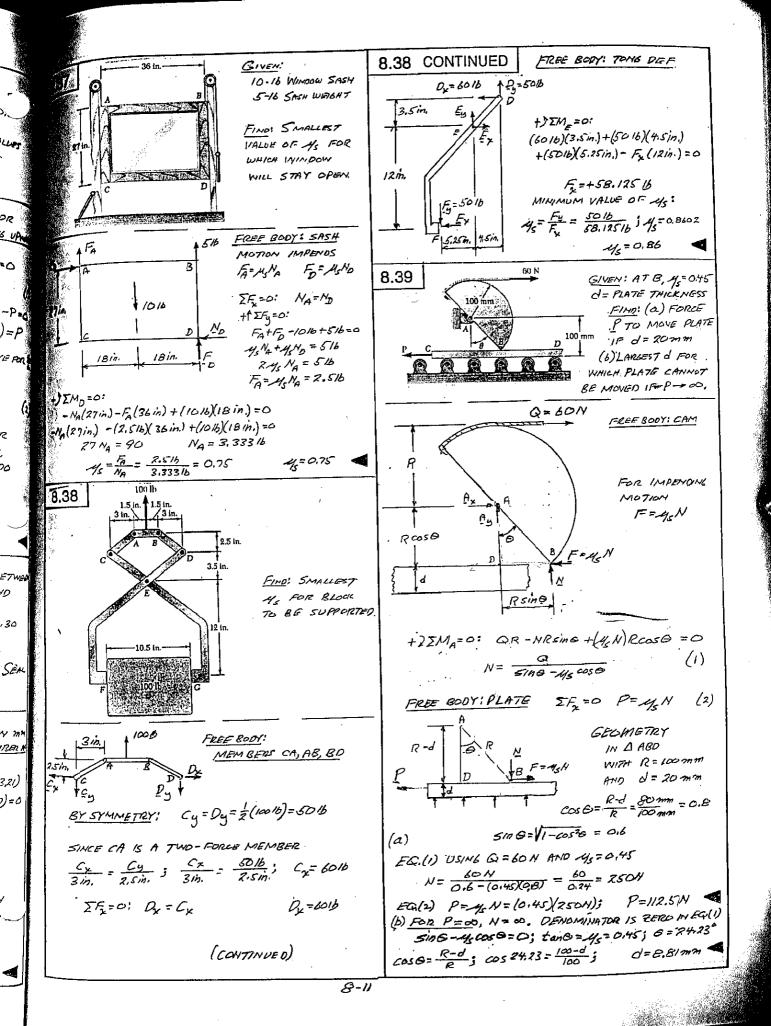


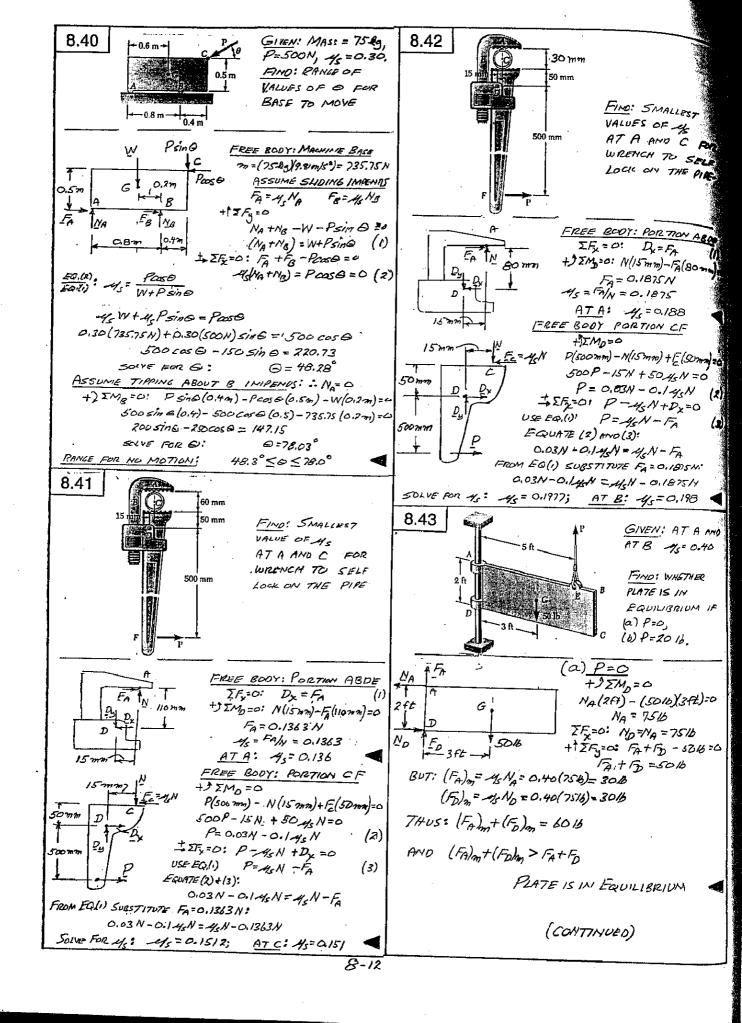


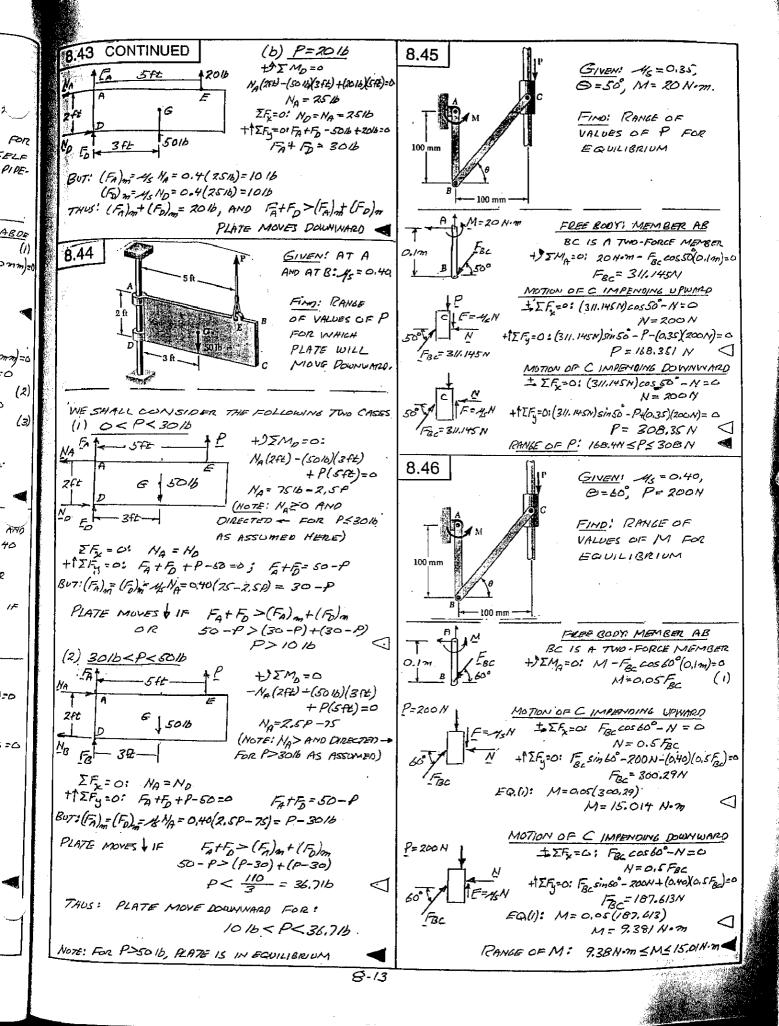


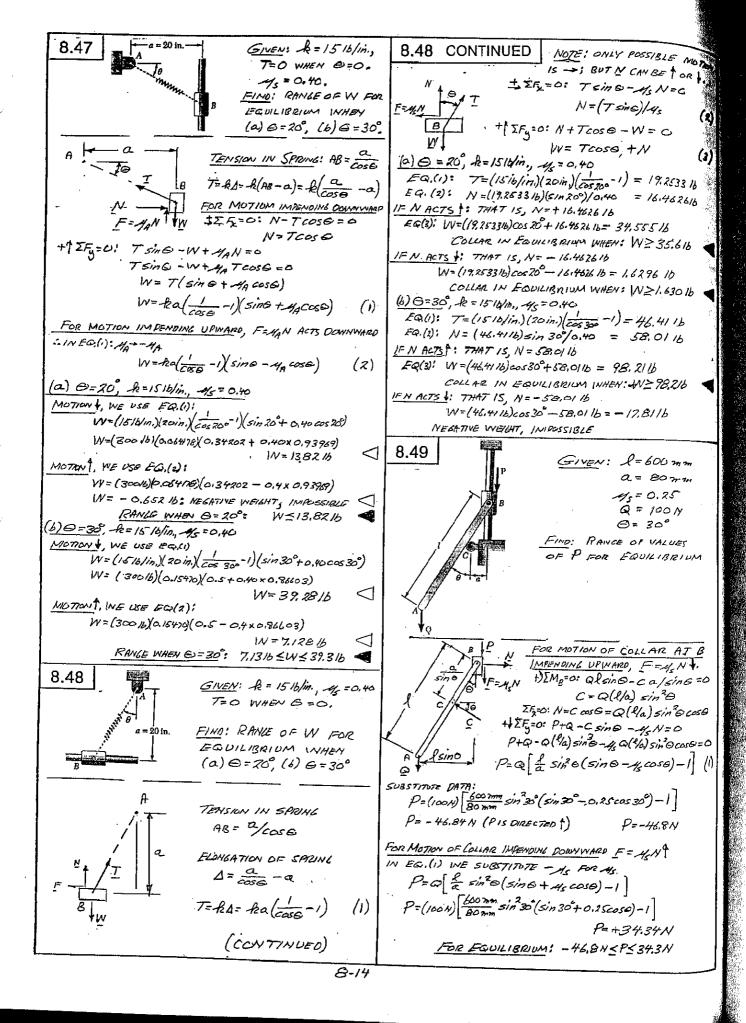


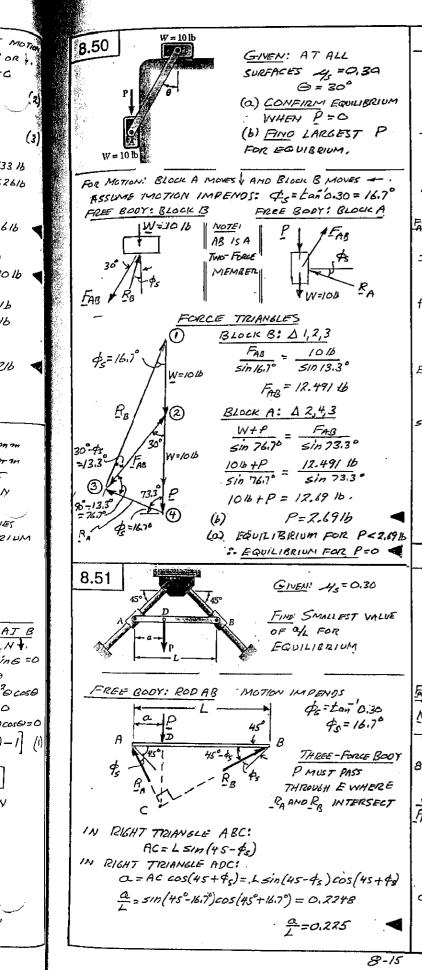












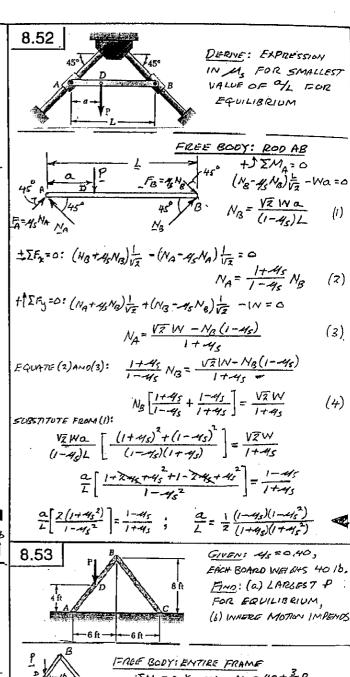
C

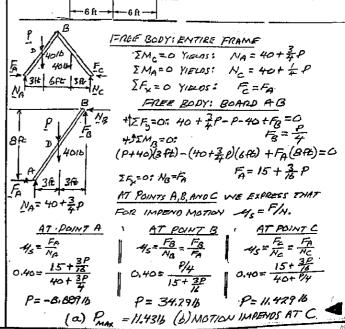
16

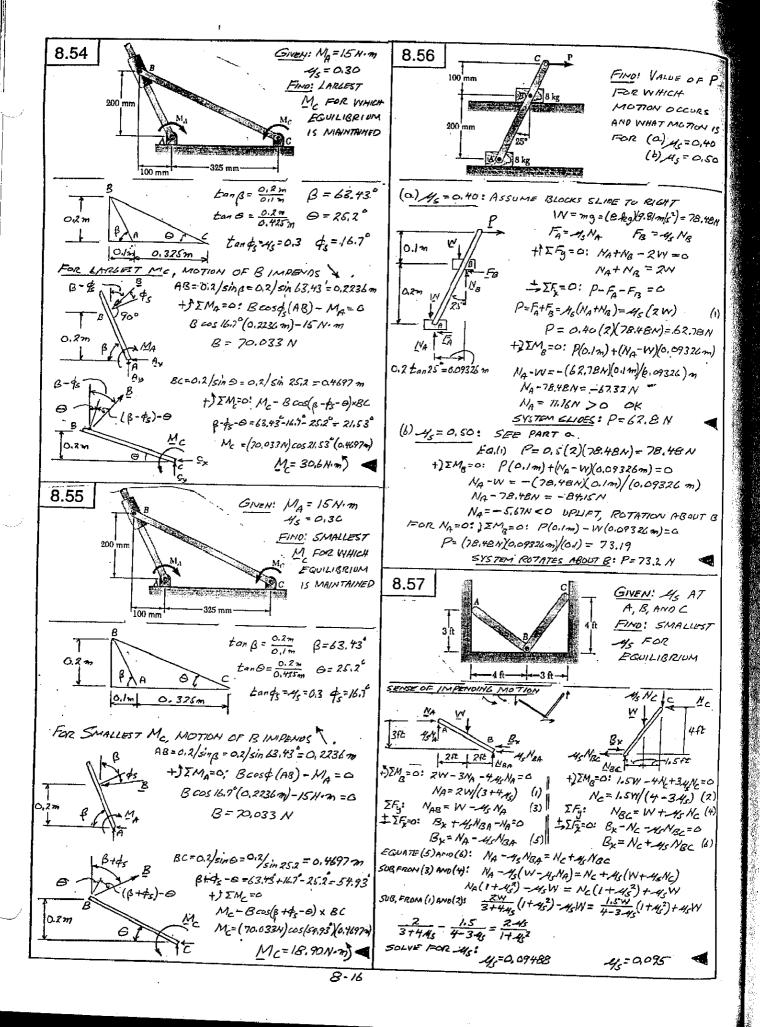
16

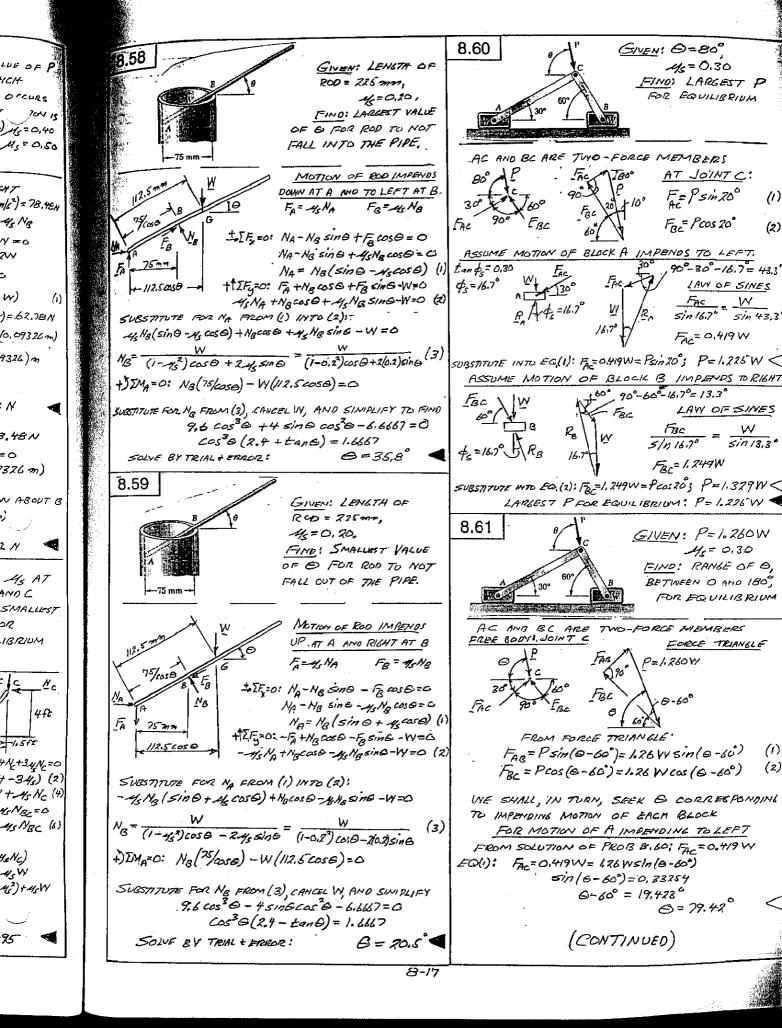
216

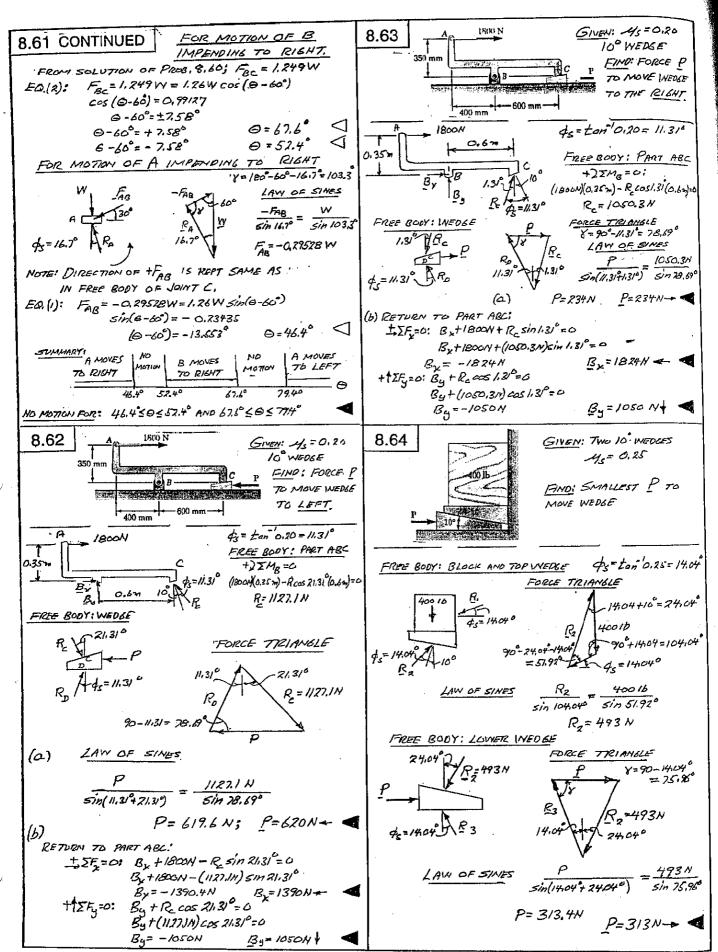
Æ

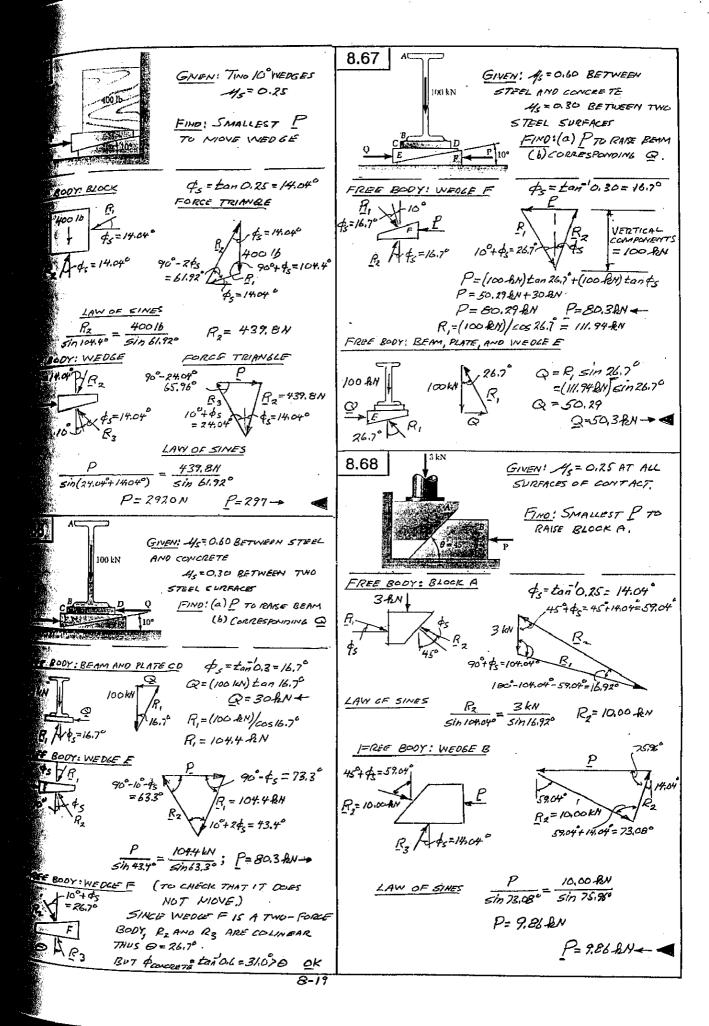


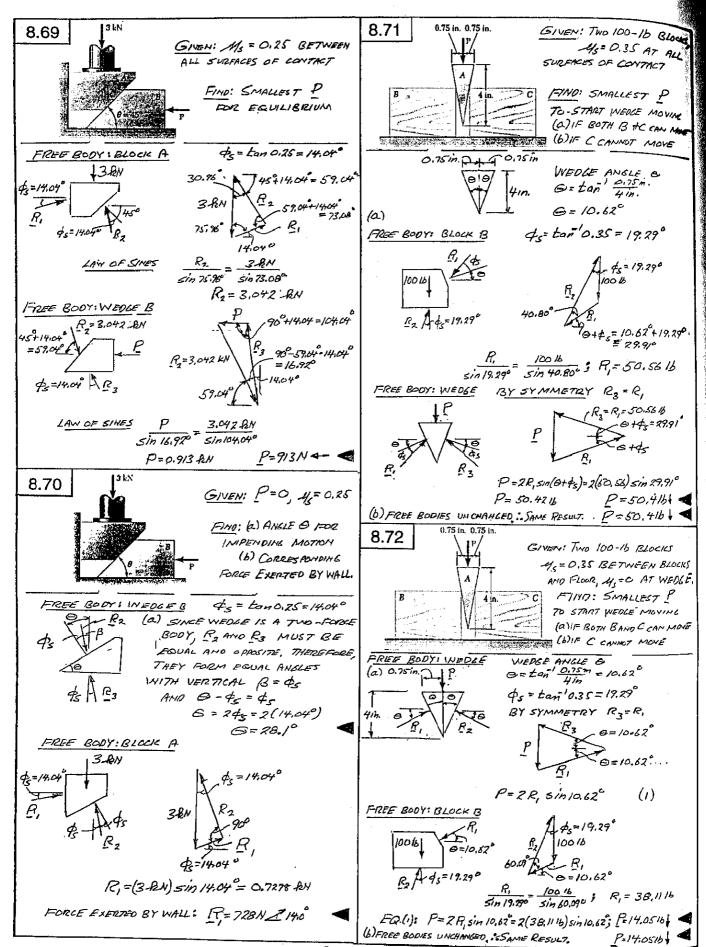


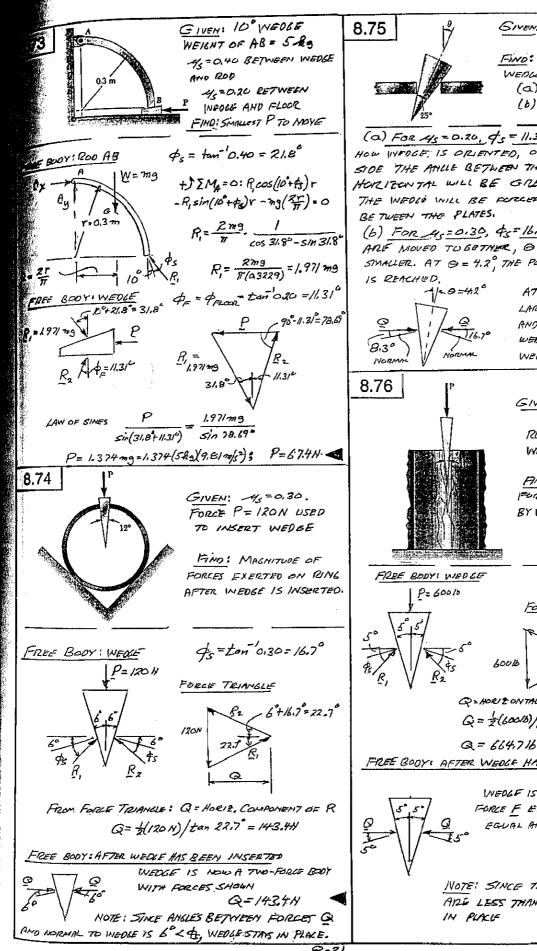












?9°

790

+19,29

56 B

5616

= 29.91

29,91°

4/

ocics N BLOCKS

7 P

OVING

AN MONE

T WEDGÊ

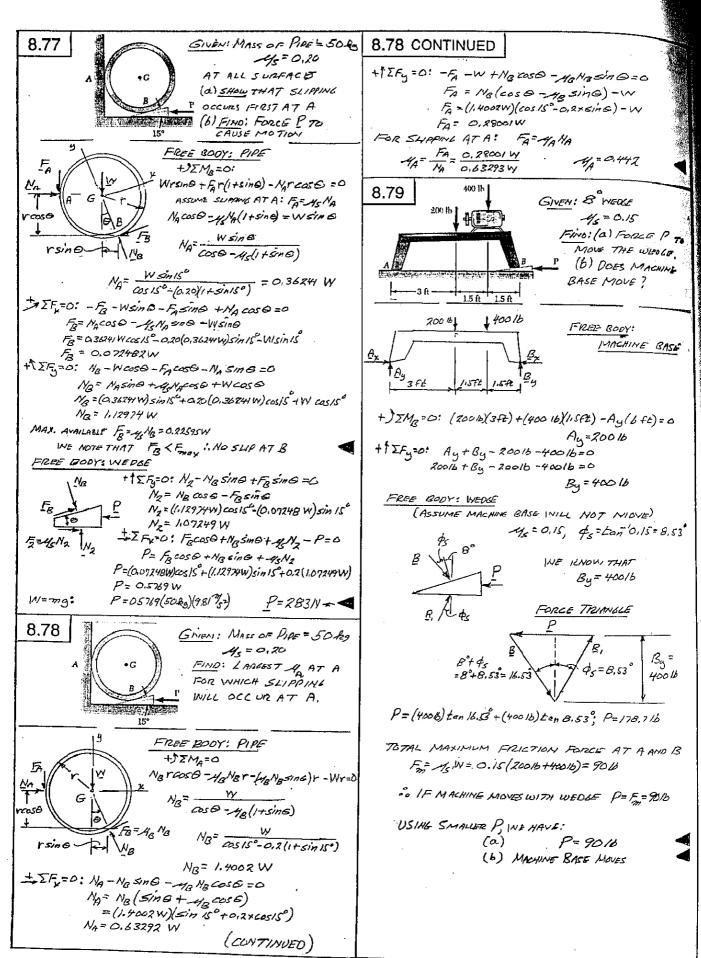
GIVEN: PLATE MOVE TOSETHER FIND: WHAT HAPPENS TO WEDGE (a) IF 45=0,20. (b) IF M= 0.30. (a) FOR 45=0.20, \$= 11.31°, PEGARDLESS OF HOW INFOCE, IS ORIENTED, ON AT LEAST ONE SIDE THE ANGLE BETWEEN THE FACE AND THE HORIZONTAL WILL BE GREATER THAN OF. THE WEOLD WILL BE FORCED UP AND OUT FROM (b) FOR 45=0.30, \$= 16.7. AS THE PLATES ARE MOVED TUBETHER, & WILL BECOME SYMPLETE. AT G = 4.2, THE POSITION SHOWN AT THIS POSITION THE LARGER ANGLE BETWEEN GR AND THE NORMAL TO THE WEDGE IS 16.70, THE WEDGE WILL SELF LOCK, GIVEN: 45 = 0.35 Force P=60016 REGULTED TO INSERT VYEOCE AND: MAGNITUOF OF FURCES EXERTED ON WOOD BY WEDGE AFTEN INSERTION \$= tan-10.35=19.29° FORCE TRIANGLE Rz_5419,29 = 24,290 Q=HORIZONTAL COMPENENT OF P. & Rz

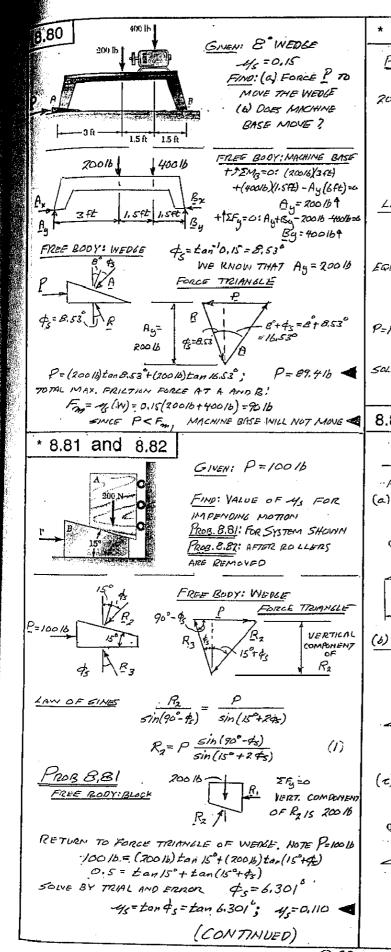
Q= = (600/6)/tan 24.290

FREE BODY AFTER WEOGF HAS BEEN INSERTED

INFORF IS NOW A TWO-FORE BODY. FORCE F EXERTED ON WOOD IS EQUAL AND OPPOSITE TO Q.

> NOTE: SINCE THE 5 ANLLES SHOWN ARE LESS THAN OS. INFOLE STAYS





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3

DEE P TO

- WEOGE

MACHINE

ME BASE

6 ft)=0

115=8,53

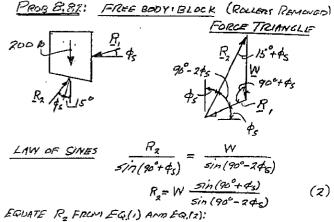
13y =

40016

9 AND B

=90%

8.81 and 8.82 CONTINUED

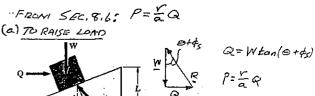


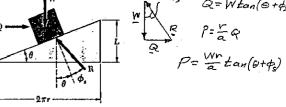
 $P = \frac{\sin(90^{\circ} - \dot{\phi_8})}{\sin(15^{\circ} + 2\dot{\phi_8})} = W = \frac{\sin(90^{\circ} + \dot{\phi_8})}{\sin(90^{\circ} - 2\dot{\phi_8})}$ P=10616; W=20016: 0.5= sin(90+4) sin(15+24) sin (90°-245) sin (90°-45)

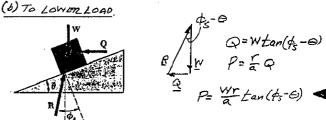
SOLVE BY TRIAL AND ERROR: \$= 5.784°

ys=tands=tan 5.784°

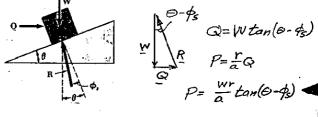
8.83 FOR THE JACK OF SEC. 8.6 (page 418) DERIVE FORMULAS FOR FORCE P FOR CASES LISTEN BELOW

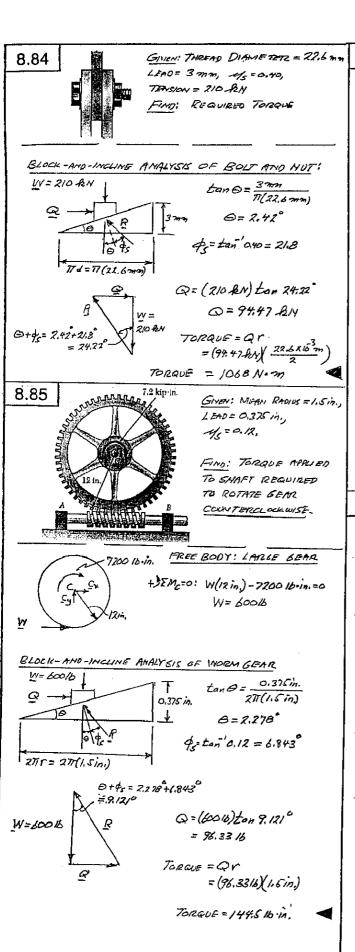


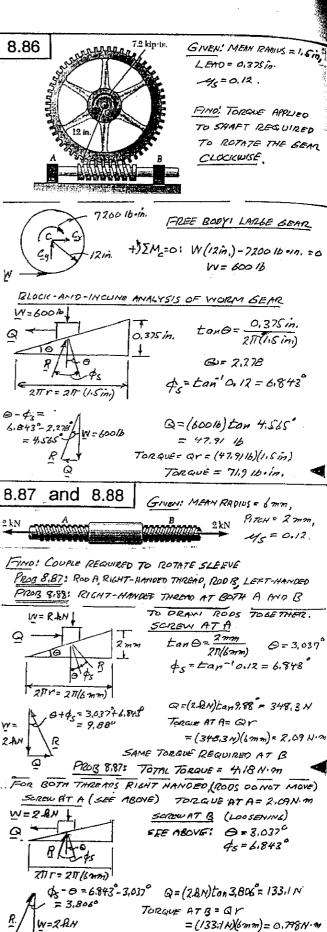




(t) TO HOLD LOAD (JACK IS NOT SELF LOCICING)



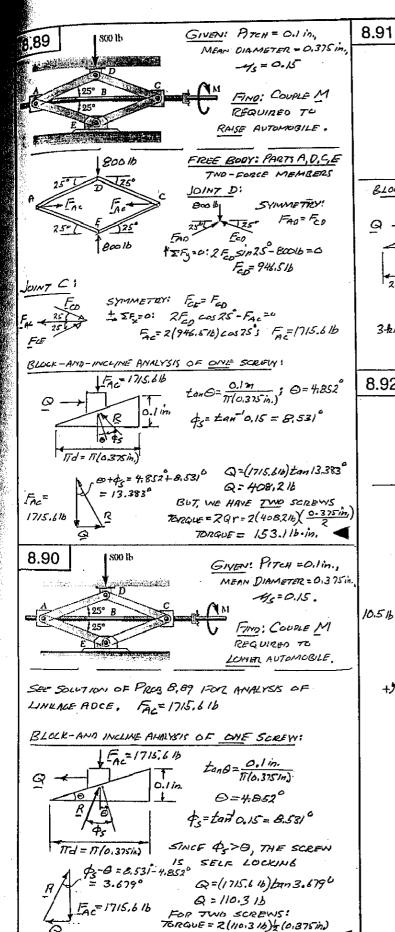




TOTAL TORQUE = 2.09 N. m + 0.798 N.m

TOTAL TORQUE = 2.89 Nom

PROB. 8.88:



Ž,

037

Nim

ve)

=0



GIVEN: LEAD = 4 mm,

MEAN RADIUS = 15 mm,

MS = 0.10,

FORCE TO BE APPLIED

TO GEAR = 3 LN.

FINO! TORQUE THAT MUST BE APPLIED TO SCREW.

BLOCK-AND-INCLINE ANALYSIS OF SERIEW

3.4N

tan0 = 4mm

217(15mm)

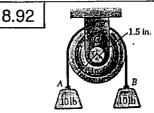
6 + 5

217 = 217(15mm)

G + 0 = 2, +3 + 5.91

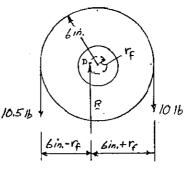
Q = (3.4N) tan 8.14 = 425

 $\frac{211r^{2}211(15mh)}{6+\phi_{s}^{2}-2.73+5.91} \qquad Q=(3hN) \tan 8.14^{2}=429N$ $\frac{8+\phi_{s}^{2}-2.73+5.91}{70nav_{f}^{2}=Qr=(429N)(0.015m)}$ $\frac{34N}{Q}$ $\frac{70nav_{f}^{2}=6.74N\cdot m}{70nav_{f}^{2}=6.74N\cdot m}$



GIVEN: PULLEY WEIGHS 516

FIND: COEFFICIENT OF STATE PRICTION IF A O.S-16 WEIGHT ADDED TO BLOCK A STARTS ROTATION.

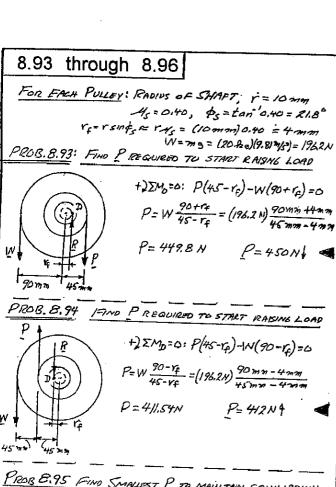


+) $\sum_{b=0}^{\infty} = 0: (10.516)(6in.-r_f) - (1016)(6in.+r_f) = 0$ $(0.516)(6in.) = (20.516)(r_f)$ $r_f = 0.14834in.$

 $r_t = r \sin \phi_s$ $\sin \phi_s = \frac{0.14634 \text{ in.}}{1.5 \text{ in}} = 0.09756$ $\phi_s = 5.5987^\circ$ $\phi_s = tan \phi_s = tan 5.5987^\circ$ $\phi_s = 0.09003$

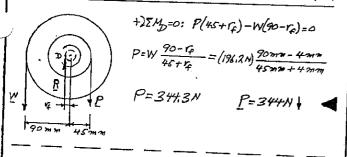
1/5=0,098

TORENE = 41.416 . in.



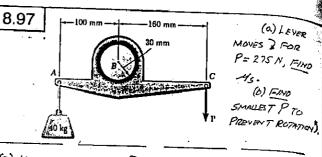
P=W 90-Y= = (196.2N) 90 mm - 4 mm P= 412N4 PROB 8.95 FIND SMALLEST P TO MAINTAIN EQUILIBRIUM

P=450N1



PROB. 8.96 FIND SMALLEST P TO MAINTAIN L'QUILIBRIUM +) 5Mp=0: P(45+rp)-W(90+rp)=0 P=14 90+1+ = (196.2N) 90mm +4mm 45+14 = (196.2N) 45mm+4mm

P= 376.4N P=376 N



8.99

FOR

PUL

+124

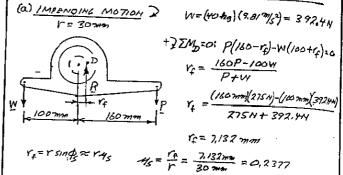
T_{EF}

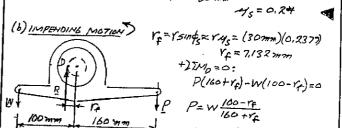
8.

AT.

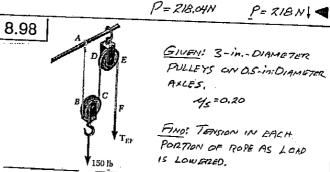
12E

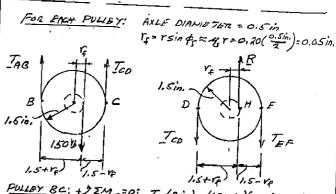
VE



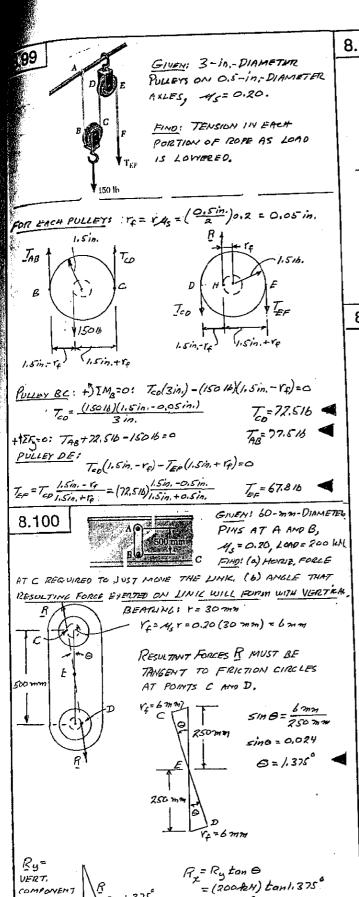


P=(392,4H) 100mm - 7,132mm





PULLEY BC; +) EMB=0: Too (3in) - (150 16)(1.570,+14)=0 TEO= 3 (150 16) (1.5 in + 0.05 in); To= 77.5 16 +1 SFy=0: TAB + 77.5 16 - 150 16= 6; TAB= 22.5 16 PULLEY DE: +JZM4=0: TEO(1.5+re) - TEE(1.5-re)=0 Ter= T 1.5+ 1/4 = (77.51) 1.5 in. +0.05 in. T= 82.816 4



40-1.375°

= 200 AN

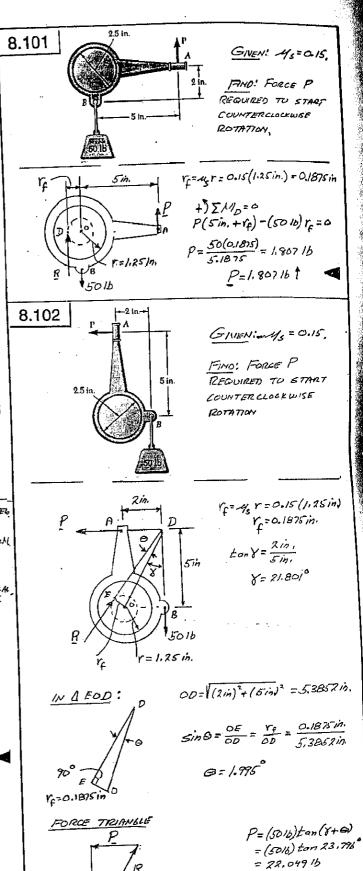
= 4.80 PM

HORIZ, FORCE = 4. BORN

244

4)00

39244)

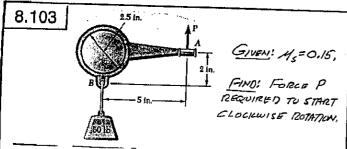


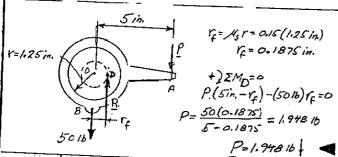
8+0=21.801+1.995

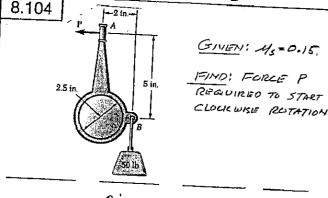
= 23,796°

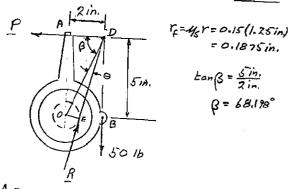
P= 22.016+

50 ID









IN / FOD:

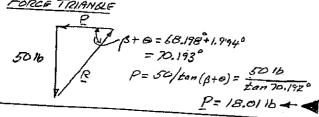
$$00 = \sqrt{(2in)^2 + (5in)^2}$$

$$00 = 5.3852 in.$$

$$00 = \frac{0.1875 in.}{5.3852 in.}$$

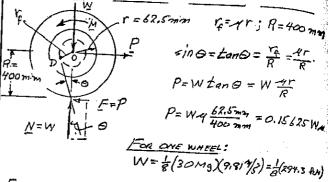
$$0 = 1.994^6$$

FORCE TRIANGLE



GMEN: RAILROAD CAR OF MASS 30 Mg of 8.105 EKHT 600- mm - DIAMETER WHEEL WITH 125-mm-DIAMETER AXIES. 45 = 0.020, 4K = 0.015.

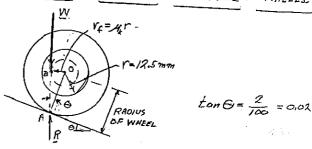
FIND: HORIZONTAL FORCE REQUIRED (a) TO STAN CAR MOVING, (b) TO KEEP IT MOVING,



FOR EIGHT WHEELS OF RAILROAD CAR ZF = 8(0.15825) = (294.3 Pen) 4 = (45.984 4) KIN

- (a) TO START MOTTON: 1/5=0.020 IP = (45.984X0.020) = 0,9/97 KN; ZP=920N ◀
- (b) TO MAINTAIN MOTION: MR=0.015 EP=(45.984)(0.015) = 0.6297 for, ΣP=690N ◀

8.106 GIVEN! SCOOTER IS TO ROLL DOWN A 2 PERCENT SLOPE AT CONSTANT SPEAD. AXLES OF WHEELS ARE 25 mm IN DIAMETER, 4 = 0,10. Fino: REQUIRED DIAMETER OF WHEELS

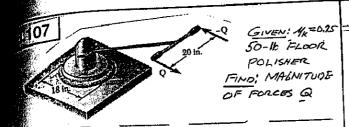


STACE SCOOTER ROLLS AT CONSTANT SPEED, EACH WHEEL IS IN EQUILIBRIUM. THUS W AND R MUST HAVE COMMION LINE OF ACTION TANGENT TO THE FRICTION CIRCLE.

$$V_f = M_b V_a (0.10)(12.5 mm) = 1.25 mm$$

$$OA = \frac{OB}{tan \Theta} = \frac{V_f}{tan \Theta} = \frac{1.25 mm}{0.02} = 62.5 mm$$

DIAMETER OF WHEEL = 2(OA) = 125mm



SEE Fig. 8.12 (page 343) AND EQ. 8.9 (page 344)
USING: R=9in., P=5016, AND Uk=0.25

IN=\(\frac{2}{3}\mathrm{A}_k PR=\frac{2}{3}(0.25)(50 16)(9in)=7516.in.}{\text{ZMy=0 YIELOS:}} \text{M=Q(20in.)}

7516.in. = Q(20in.)

Q=3.7516

8.108

GIVEN: COUPLE

M = 30 N·m

REQUIRED TO START

ROTATION

FIND! Us

50 mm

120 mm

SELE FIG. B.12 (page 343) AND EQ. B. B (page 344).

USING: P. = 25mm = 0.025m

R= 60 mm = 0.060 m

P= 4,000 N, M = 30 Nim

 $M = \frac{2}{3} - \frac{1}{3} P \frac{R_2^3 - R_1^3}{R_2^2 - R_1^2}$

25 W.

1.3 AN)

A).

0,10,

-25.

201

EACH

30N·m= \frac{2}{3} 45 (4000N) \frac{(0.060 m)^3 - (0.025 m)^2}{(0.060)^2 - (0.025 m)^2}

30Him = 2 45 (4000N)(0.06735m); M5= 0.167

* 8.109 FOR SHAFT AND BEARING ASSUME NORMAL FORCE PER UNIT AREA IS INVERSELY

PROPORTIONAL TO Y. SHOW THAT M IS 75% OF VALUE GIVEN BY FORMULA (8.9) ON PACE 344).

USING FIG 8.12 (page 343), WE ASSUME $\Delta N = \frac{A}{V} \Delta A$: $\Delta A = V \Delta \Phi \Delta V$

AN= France = ROOAr

NE WRITE, P= ION OR P=SUN

P=SSR 400r = 27/RR 3 - R = 7/7/R

AN= PAGAY

DM= rDF= ryk DN= ryk PDBAr

 $M = \int_{2\pi}^{2\pi} \int_{R}^{R} \frac{M_{k} P}{2\pi R} r dr d\theta = \frac{2\pi M_{k} P}{2\pi R} \cdot \frac{R^{2}}{2} = \frac{1}{2} M_{k} PR$

FROM EG(E.9) FOR A NEW BEARING MARIO 3.4K PR

THUS MARKY = 1/2 = 3

M=0.75M NEW

* 8.110 ASSUMING BEARING WEAR AS GIVEN
IN PROB. 8,109, 5 MON THAT MAGNITUDE
OF COUPLE TO OVERCOME FRICTION IN A
WORN-OUT, COLLAR BEARING (SEE Fig 8,12) IS $M = \frac{1}{2} M_K P(R, + R_2)$

USING FIG. 8112 (page 343), WE RESOME AN = PAA

AA = rabar; AN = P rabar = Pabar

BUT! P = IAN OR P = SdN

P = S Rabbar = 2TT (R2-R)-R

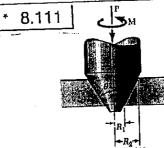
RABAR

RABAR

THUS, $-R = \frac{P}{2T(R_2 - R_1)}$, AND $\Delta N = \frac{P \Delta \Theta \Delta r}{2T(R_2 - R_1)}$

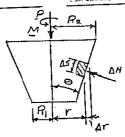
 $AM = r \Delta F = r \frac{q_{k} \Delta N}{r} = r \frac{P \Delta \Theta \Delta r}{2\pi (R_{2} - R_{1})}$ $M = \int_{-R_{1}}^{2\pi} \frac{R_{2}}{2\pi (R_{2} - R_{1})} r dr d\Theta = \frac{2\pi A_{k} P}{2\pi (R_{2} - R_{1})} \cdot \frac{R_{2}^{2} - R_{1}^{2}}{2}$

SINCE $R_2^2 - R_1^2 = (R_2 - R_1)(R_2 + R_1)$ $M = \frac{1}{2} M_K P(R_1 + R_2)$



ASSUME: UNIFORM
PRESSURE BETWEEN
SURFACES OF CONTACT

SHOW THAT $M = \frac{2}{3} \cdot \frac{4kP}{5in\Theta} \cdot \frac{R_2^3 - R_1^3}{R_2^2 - R_1^2}$



 $\Delta N = R \Delta A$ $\Delta A = (r \Delta \phi) \Delta S = (r \Delta \phi) \frac{\Delta r}{S \ln \Theta}$ $7 + O S = R \Delta A = \frac{R r}{2} \Delta \phi \Delta A$

AN=RAA= for Afar

VERTICAL COMPONENT OF AN: (AN)y= AN SING= &rodor P=I(AN)y= E&rodor

OR, USING INTEGRALS $P = \int_{R_1}^{2\pi} \int_{R_2}^{R_2} R r d\phi dr = 2\pi R \frac{R_2^2 - R_1^2}{2}$ $R_1 = \frac{R_2^2 - R_2^2}{2}$ $R_2 = \frac{R_2^2 - R_2^2}{2}$

Thus, $R = \frac{\rho}{\pi (R_2^2 - R_i^2)}$ $\Delta N = \frac{Rr}{\sin \theta} \Delta \phi \Delta r = \frac{4\kappa \rho r^2 \Delta \phi \Delta r}{\pi \sin \theta (R_2^2 - R_i^2)}$

INTEGRATING! $R_{2} = \frac{1}{2\pi} \frac{1}{1} \frac{1}{1$

 $M = \frac{2}{3} \cdot \frac{J_{S} P}{Sin0} \cdot \frac{R_{s}^{3} - R_{s}^{3}}{R_{s}^{4} - R_{s}^{3}}$

8.112

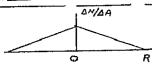
GIVEN: POLISHER OF WEIGHT = 5016 4/x = 0.25

ASSUME! NORMAL FORCE

BETWEEN FLOOR AND DISK

LIARIES LINEARLY FROM A MAXIMUM

AT CENTER TO ZERO AT EOGE FIND: MAGNITUDE. Q OF FORCES TO PREVENT MOTION.



AN= & (1-F)

DA- rab ar

$$AN = \frac{1}{R}\left(1 - \frac{r}{R}\right)rA\Theta A r$$

$$P = \sum \Delta N = \int \int \frac{1}{R}\left(1 - \frac{r}{R}\right)rd\Theta A r = \frac{r^3}{2}\left[\frac{r^2}{2} - \frac{r^3}{3R}\right]_0^R$$

THUS: A= 3P TRE AND AN - 3P (1- T) rABBY

MOMENT OF PRICTION FORCE ON AA IS

$$\Delta M = r \Delta F = r \gamma_{R} \Delta H = \frac{3PM_{e}}{7rR^{2}} \left(1 - \frac{r}{R}\right) r^{2} \Delta C \Delta r$$

$$M = \sum_{n=0}^{2} A_{n} = \int_{0}^{2} \frac{3PA_{n}}{\pi R^{2}} \left(r^{2} - \frac{r^{3}}{R}\right) d\theta dr = \frac{2\pi}{\pi} \cdot \frac{3PA_{n}}{R^{2}} \left[\frac{r^{3}}{3} - \frac{r^{4}}{4R}\right]_{0}^{2}$$

$$M = \frac{1}{2} A_{n} PR$$

4=0.25, P=501b, R=9in

M= = (0.25) 5016)(91n) = 56.25 16.in.

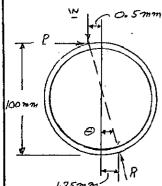
BUT: Q(20in.)=M; Q= M = 56.25 16-in; Q= 2.8116

8.113



GIVEN: 900-kg, BASE; ICU-MM DIAMETER PIPES, ROLLING RESISTANCE IS

0.5m BETWEEN PIPES AND BASE +1,25mm BETWEEN PIPES FIND: PTOMANTAIN MOTION AND CONCRETE FLOOR.



tan6= 0,5mm +1.25mm

tane=0.0175

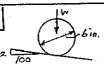
P=Wtane P = 0.0175 W

W=mg=(900-kg)(9.81 m/s)

P= (0.0175)(900 ftg)(9.81 m/s2) P= 154.51 N

P=154.4N

8.114



GIVEN: DISK ROLLS AT CONSTANT VELOUTY FIND: COEFFICIENT OF ROLLING RESISTANCE

DIEK IS IN EQUILIBRIUM

SIMILAR TRIANGLES

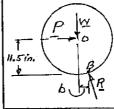
$$\frac{b}{r} = \frac{2}{100}$$

b= 2 100 v = 2 (6 in.); b= 0,060 in.

8.115

GIVEN: 2500-16 AUTOMOBILE WITH 23-in .- DIAMETER TIRES, COEFFICIENT OF ROLLING RESISTANCE = 0.05 in.

FIND: HORIZONTAL FORCE TO MOVE AUTOMOBILE CY HORIZONTAL ROAD AT CONSTANT SPEED

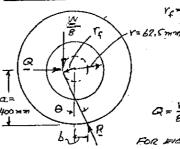


+) IM =0: P(11.5in.) -W b=G P(11,5in.)=(2500 16)(0.05 in) P= 10.869 lb

P=10.8716

8.116

GIVEN: 30-Mg RAILROAD CAR ON EIGHT BOO-mm-DIAMETER VYHEELS WITH 125-mm ALLES, Ms = 0.020, M = 0.015, COFFFICIENT OF ROLLING RESISTANCE O.5 mm FIND: HORIZ. FORCE (a) TO START MOTION, (b) TO MAINTHIN MICTION.



FOR ONE WHEEL

tand = sind = Te+b

tong= 4r+b

 $Q = \frac{W}{8} \tan \theta = \frac{W}{8} \frac{4r+b}{a}$

FOR WISHT WHEELS OF CAIL P=W=4r+b

W=mg=(30Mg)(9.81 %=)= 294.3 DN a=400 mm, r=62.5mm, b=0.5mm

(a) TO START MOTION: 4 = 45=0.02 P= (294.3 P2N)(0.020) 62,5000) +0.5000

P= 1.2876 KN

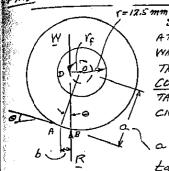
P=1.288 LN

(b) TO MAINTAIN CONSTANT SPEED of = 4/1 =0.015 P= (294,3 BN) (0.015)(62,5 mm) +0,5 mm

P=1.0576-BN

P=1.058RN

GANEN! SCOOTER IS TO ROLL DOWN A 2 PERCENT SLOPE AT CONSTANT SPEED, NES OF WHEELS ARE 25 mm IN DIAMETER. = 0.10, COEFFICIENT OF ROLLING RESISTANCE = 1.75 mm. FIND REQUIRED DIAMETER OF WHEELS.

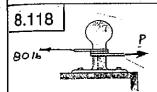


SINCE SCOOTER ROLLS AT CONSTANT SPEED, EACH WHEEL IS IN FOULIBRIUM. THUS W AND R MUST HAVE COMPION LINE OF ACTION TANGENT TO THE FRICTION CIRCLE.

a = RADIUS OF WHEEL tan 6= 2 = 0.02

SINCE & ANDY, ARE SMALL COMPARED TO Q, tan 6 = V++b = Mx++b = 0.02 DATA: 1/k = 0.10, '6 = 1.75 mm, V=12.5 mm (0.10)(12,5mm)+1,75mm = 0.02

a = 150 mm; DIAMETER = 2a = 300 mm.



(a) FOR TWO FULL TURNS OF HAWSER AND P = 5000 10, FIND MS (b) FIND NUMBER OF TURKS, IF P=20,000 1b.

(a)
$$\beta = 2 T \nu_{RNS} = 2(2n) = 4n$$

 $T_1 = 801b$ $T_2 = 50001b$
 $l_1 \frac{T_2}{T_1} = 4s\beta$ $4s = \frac{1}{8} l_1 \frac{T_2}{T_1} = \frac{1}{4\pi} l_1 \frac{50001b}{601b}$

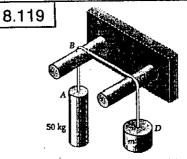
(b) T, = 8016, Ta = 20,000 16, 45 = 0.329

$$l_{11} \frac{T_{2}}{T_{1}} = M_{5}\beta$$
 $\beta = \frac{1}{4} l_{11} \frac{T_{2}}{T_{1}} = \frac{1}{0.329} l_{11} \frac{20,000 \text{ 15}}{80 \text{ y}}$

B= 1 (250) = 5.5215 = 16,783

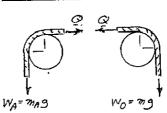
NUMBER OF TURNS = 16.783

NUMBER OF TURNS = 2.67



GIVEN: 1/5=0.40

FIMD: RANGE OF MASS on FOR EQUILIBRIUM



FOR MOTION OF A IMPENDING DOWNWARD

FOR EACH ROD B = T/2, Ms = 0.4

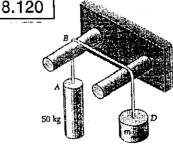
MULTIPLY EQUATIONS MEMBER BY MEMBER

$$\frac{Q}{m_{A9}} \cdot \frac{m_{9}}{Q} = e^{4s(\beta+\beta)} \cdot \frac{m}{m_{A}} = e^{0.4(2)\frac{\pi}{2}} = 3.514$$

FOR MOTION OF A IMPENDING UPWARD, WE FIND IN A GIMILAR WAY

$$\frac{m_A}{m} = C = \frac{0.4(2)^{\frac{17}{2}}}{3.574} = 3.514; \quad m = \frac{50 \, \text{kg}}{3.574} = 14.23 \, \text{kg}$$

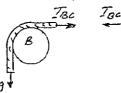
RAHGE FOR EQUILIBRIUM: 14.23 kg = m = 175.7 kg



GIVEN: MOTION OF D IMPEMOS UPWARD WHEN m=20kg,

Fing: (a) 45 (b) TENSIAN IN BC

FOR EACH ROO! B= 1/2



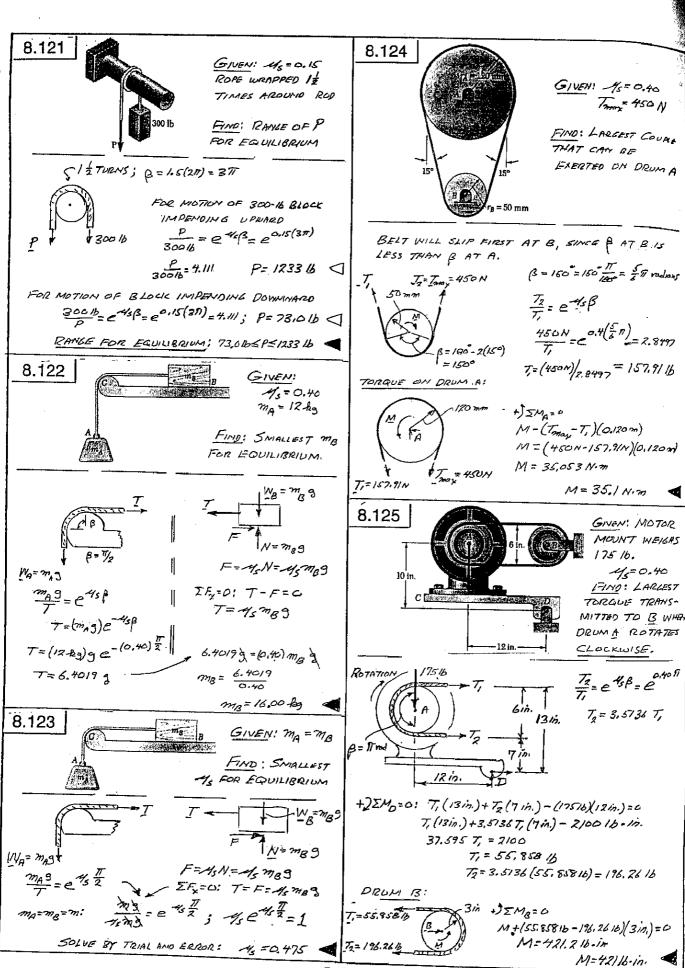
TBC = C45B EQU:

EG(2): TBC = e 45B

MULTIPLY EQUATIONS MEMBER BY MEMBER

50 29 = e45 T; 45T = 0.963; 45 = 0.2917 45=0,292

EG(2) Tec = 0.2917(= 1.582; Tec=1.582 (20 20 (9.8) 1/6) Tec=310N



8.12

ROTAT.

β=17 ~

+2

DR

72=14

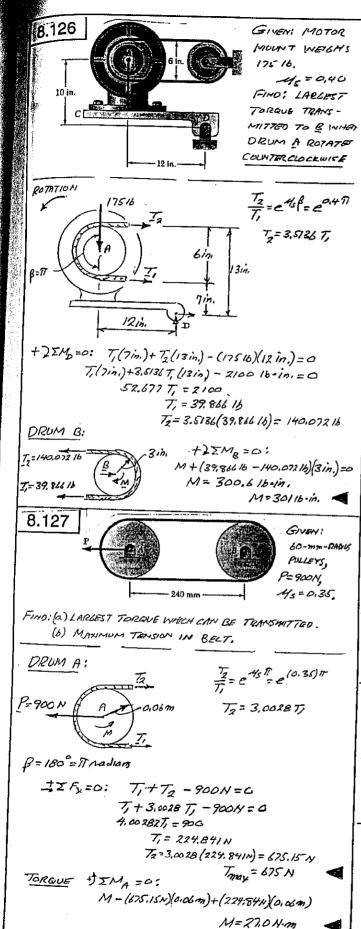
T,= 39

8.

Fin

P

8-32



.40

COUPLE

PUM A

15

nadaus

8497

116

لهده

4

545

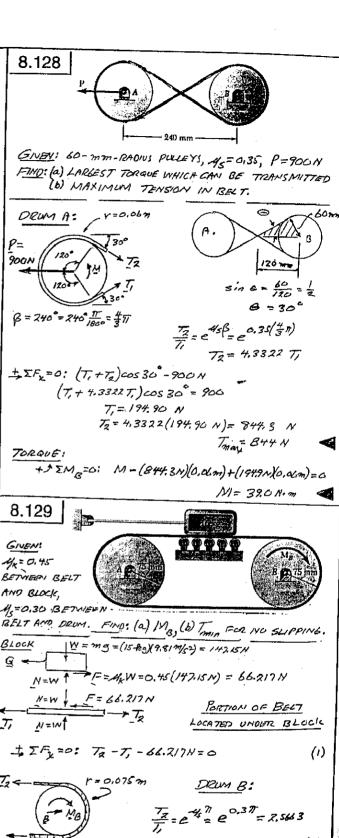
37

۲-

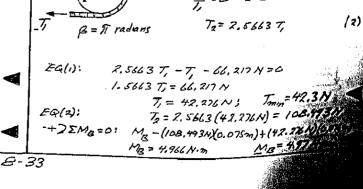
2-5

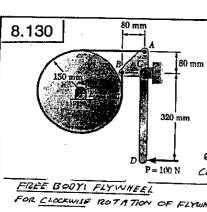
n

~



GIVEN!



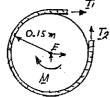


GIVEN: 1/K = 0.25

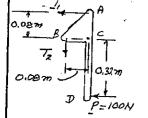
FIND: MAGNITUDE OF
COUPLE APPLIED TO
FLYWHEEL FOR
CLOCKWISE ROTATION
SHOW THAT
RESILT IS SAME FOR
COUNTERCLOCKWISE ROTATION

FOR CLOCKWISE ROTATION OF FLYWHELL TO AND TI ARE

TI LOCATED AS SHOWNI.



 $\beta = \frac{3}{4}(360) = \frac{3}{4}(20) = \frac{3}{2}T \text{ vadians}$ $\frac{T_2}{T_1} = e^{4L\beta} = e^{0.25(\frac{3}{2}T)} = 3.2482$ $T_2 = 3.2482 T_1 \qquad (1)$



FREE BODY: HANDLE

 $+\int \Sigma M_c = 0$ (2) $(T, +T_2)(0.08m) - (100N)(0.32m) = 0$ $(T, +3.2482T_1) = 400N$

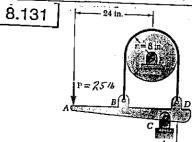
T,= (400 N)/4,2482 = 94.157 N T₆=3,2482(94,157N)=305.842 N

RETURN TO FREE BODY OF FLYWHEEL

+) \(M_E = 0: M + (T, -T_2)(0.15m) = 0

M + (94.157N - 305.842N)(0.15m) = 0

M= 31.752N·m M= 31.8 N·m IF ROTATION IS REVERSED (TO BE)) To AND TO ARE INTERCHANGED; EQS.(1) AND(2) ARE NOT CHANGED, THUS VALUES OF TO, To, AND MI ART THE SAME.



GIVEN! 4 = 0,25

FIND: MAGNITURE
OF COUPLE
APPLIED TO DRUN
FOR ROTATION
(a) COUNTER CLOCKWIGE
(b) CLOCKWISE

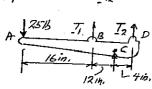
(a) COUNTERCLOCK WISE ROTATION FREE BOOK DRUM

Y=8in, B = 180° = TT radions

To 40 0.35TF



 $\frac{T_2}{T_1} = e^{th} \ell_2 e^{0.25T} = 2.1933$ $T_2 = 2.1933 T_1$



FREE BODY: CONTROL BAR +) IMC=0 T, (12 in.) - T_(4 in)-(256)(28 in)=0 T,(12)-21933T,(4)-700=0 T_1=216,9316 T_2=2.1933(2169316)=475.8016 (CONTINUED)

8.131 CONTINUED

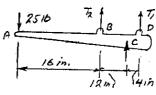
RETURN TO FREE RODY OF DRUM +) \(\SM_{e}^{=0} : M + T_{i} / (8 in.) - T_{2} (8 in.) = 6 \)
\[
M + (2/6.96 th) (8 in.) - (475.80 16) (8 in.) = 6 \]
\[
M = 2070.9 / (b.in.)
\]
\[
M = 2070.9 / (b.in.)

(b) CLOCKWISE ROTATION



Y = Bin, B = T rad $\frac{T_{Z}}{T_{z}} = C^{T} = C^{25} = 2.1933$ $T_{Z} = 2.1933 T_{z}$

FREE BODY: CONTROL ROD



T₂ (12in) - T₁ (4in) - (25k)(28i) w

R.1933T₁(12) - T₁ (4) - 700 = 0

T₁ = 31,363 1b

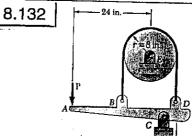
T₂ = 2.1933(31,363 1b)

T₂ = 68.788 16

RETURN TO FREE 2008 OF DRUM
+1 ΣΜ=0: M+T, (8in.) - T2 (8in.) =0
M+(31.36316)(8in.)-(68.78816)(8in.)=0

M=299,416.in.

M=29916.in.

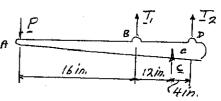


FIND: MAXIMUM AS
FOR BRAKE TO BE
SELF LOCICING FOR
COUNTERCLOCKUISE
ROTATION OF DRUM

7, 1^E / 1^E /

 $\beta = 180 = \pi \text{ radians}$ $\frac{T_2}{T_1} = e^{45}\beta = e^{45}\pi$ $\frac{T_2}{T_2} = e^{45}\pi T_1$

FREE BODY! CONTROL 1200

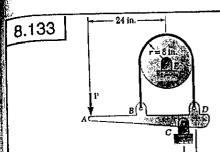


+ \$\(\Sigma \) = 0: P(28 in) - T, (12 in) + T_2(4 in) = 0

28P - 12T, + e^4T, (4) = 0

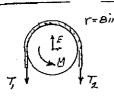
FOR SELF-LOCKING BRAILE P = 0 $12T_1 = 4T_1 e^{4T_1}$ $e^{4sT_1} = 3 \qquad M_sT = lm 3 = 1.0986$ $4s = \frac{1.0986}{T} = 0.3497$

-95=0,350



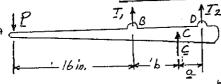
GIVEN: MG = 0.30
ROTATION D.

FIND: MINIMUM
VALUE OF a FOR
WHICH BRAKE
IS NOT SELFLOCKING.



 $r = Bin_{11}$ $\beta = \pi$ radians $\frac{T_2}{T_1} = e^{4t_0}\beta = e^{0.30\pi} = 2.5663$ $T_2 = 2.5663 T_1$

FREE BODY: CONTROL ROD



b=16in-a

+) IMc=0: P(16in+b)-T,b+T2a=0
FOR BRAKE TO BE SELF LOCKING, P=0

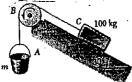
Ta=T,b; 2.5663 xa= x(16-a)

2.5663a = 16 - a 3,5663a = 16

a=4.49m.

8.134

7,=719



GIVEN: MS = 0.35

MK = 0.25

PIHO: SMALLEST M

FOR WITCH BLOCK C

(A) REMAINS AT REST, (b) STRETS

MOVING UP, (C) CONTINUES MOVING UP.

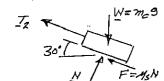
Ro TATION (2 = $120^\circ = \frac{7}{3}$) T_2

 $B = 120^{\circ} = \frac{7}{3} IT \text{ vod.}$ FREE BODY: DRUM $T_{2} = \frac{1}{3} IT = \frac{2}{3} IT$ $I_{3} = \frac{1}{3} IT = \frac{2}{3} IT = \frac{1}{3} IT = \frac{2}{3} IT = \frac{1}{3} IT$

(a) SMALLEST M FOR BLOCK C TO REMAIN AT REST CABLE SLIPS ON ORUM 2(0,25) TO EMPLOYED TO THE STATE OF THE STA

EG(1) WITH MIK = 0.25; T2=mge = 1.688/mg

BLOCK C: AT REST, MOTION IM PENDING



 $W=m_{c}9$ + $f = p: N-m_{c}g \cos 30^{\circ}$ $N=m_{c}g \cos 30^{\circ}$ $F=M_{c}N=0.35m_{c}g \cos 30^{\circ}$ $m_{c}=100 \text{ hg}$

+ X F=0; T2 + F-meg sin30°=0 1.6881 mg + 0.35 mg cos30 - neg sin30°=0 1.6881 m = 0.19689 me m=0.11663 me=0.11663(100kg); m=11.66 kg (CONTINUED) 8.134 CONTINUED

(b) SMALLEST M TO START BLOCK MOVING UP

NO SLIPPING AT BOTH DRIVE AND BLOCK 45 = 0.35 EQ(1): 72 = mg = 2(0.25)7/3 = 2.0814 mg

To 30 W= meg

MOTION IMPENDING TO MC = 100 kg +1 SF=0: N-mg cos 30° N= mcg cos 30° F=18N=0.35 mcg cos 30°

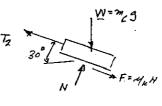
 $+\Sigma F=0$: $T_2-F-m_0g\sin 30^2=0$ $2.0814mg-0.35m_0g\cos 30^2-m_0g\sin 30^2=0$ $2.0814m=0.80311m_0$ $m=0.38585m_0=0.38585(100Ra)$ m=38.6-Rag

(C) SMALLEST ON TO KEEP BLOCK MOVING UP

DRUM: NO SLIPPING MS=0.35

EQ(1) WITH $y_5 = 0.35$ $T_2 = mg = mg = mg = T_2 = R.0814 mg$

BLOCK C: MOVING UP PLANE, THUS of = 0.25



MOTION UP +1 2F=c

N-mg cas 30 = 0

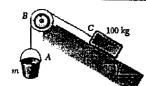
N=mg cas 30

F=4,N=0,25mcg cas 30

+ \ IF=0: T2-F-mg sin 30 = 0 2.0814mg-0.25mg cos30-mg sin 30 = 0 2.0814m = 0.71651 mc

m=0.34424 mc=0.34424 (100 kg) m=34.4 kg



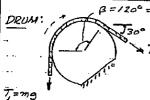


GIVEN: DRUM B 15 FIXED. 45=0.35

4x = 0,25

FIND: SMALLEST M FOR WHICH BLOCK C (a) REMAINS AT REST, (b) STARTS MOVING UP, (C) CONTINUES MIGNING UP.

(a) BLOCK C REMAINS AT REST, MOTION IMPENDS > B=1200 = 3 Tradians

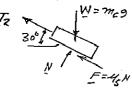


$$\frac{T_2}{m_0} = e^{-4k\beta} = e^{0.35\left(\frac{2\pi}{8}\right)}$$

T2= 2.0814 mg

BLOCK C

MOTION IMPENOS



1 EF=0: N-mg cos30 =0. N= 71/2 9 cos 300 F=15N=0.35 mg cos 300

+ K ΣF=0: T2 + F - m2 g = in 30 = 0 2.0814 mg + 0.35 mg cos30 -mg sin30=c 2.0814 mg = 0.19689 mc m = 0.09459 m = 0.09459 (100 Azg)

m= 9.46 Rg

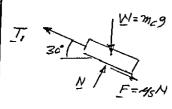
(b) BLOCK C STARTS MOVING UP DRUM:

4=0.35 B=1200= 27 radians IMPENDING MOTION

> OF CABLE F $\frac{mg}{T} = e^{0.35\left(\frac{2}{3}\pi\right)}$

Ti = mis = 0.48045 mg

BLOCK C MOTION IMPENIES



+/ ΣF=0: N-mg cos 30° N= meg cos 300 F=45N=0,35mg cas30°

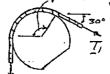
+ IF=0: T, -F-meg sin 30°=0 0.48045mg-0.35mg cos30 -0,5mg=0 0,48045m=0.80311MC m=1.67158 mc=1.67158 (100.Ag)

m=167.229 (CONTINUED):

8.135 CONTINUED

(C) SMALLEST m TO KEEP BLOCK MOVING

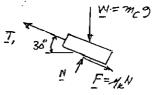
DRUM: MOTION OF CABLE (4 = 0:25 B = 120 = 3 T radians



$$\frac{T_2}{T_1} = e^{4\mu\beta} = e^{0.25(\frac{2}{3}n)}$$

200 = 1.881 T= mg = 0.59238 mg

BLOCK C! BLOCK MOVES &



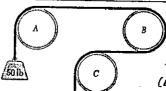
+ FF=0: N-mag cas 30. N= meg cosso F=4,N=0.25729 cos30

+ IF=0: T, -F-mag sin 30=0 0,59238 mg - 0,25mg cos30 -0,5 mg =0 0,59238 m = 0.71651 mc m = 1.20954 mc = 1.20954(100 kg) m=121,029

8.136

72 = e48

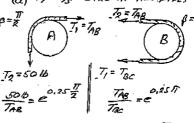
Ta=mg



GIVEN: 1/5=0.25 4K=0.20 FIND: (a) SMALLET ' W FOR EQUILIBRIUM (b) LARGEST W THAT

CAN BE RASED IF PIPEB 15 120TATED WITH A+C FIXED.

(a) 44 = 45 = 0,25 AT ALL PIPES



T2 = TBC

50B = 4.8015; W= 10.394B

(b) PIRE B ROTATED 5

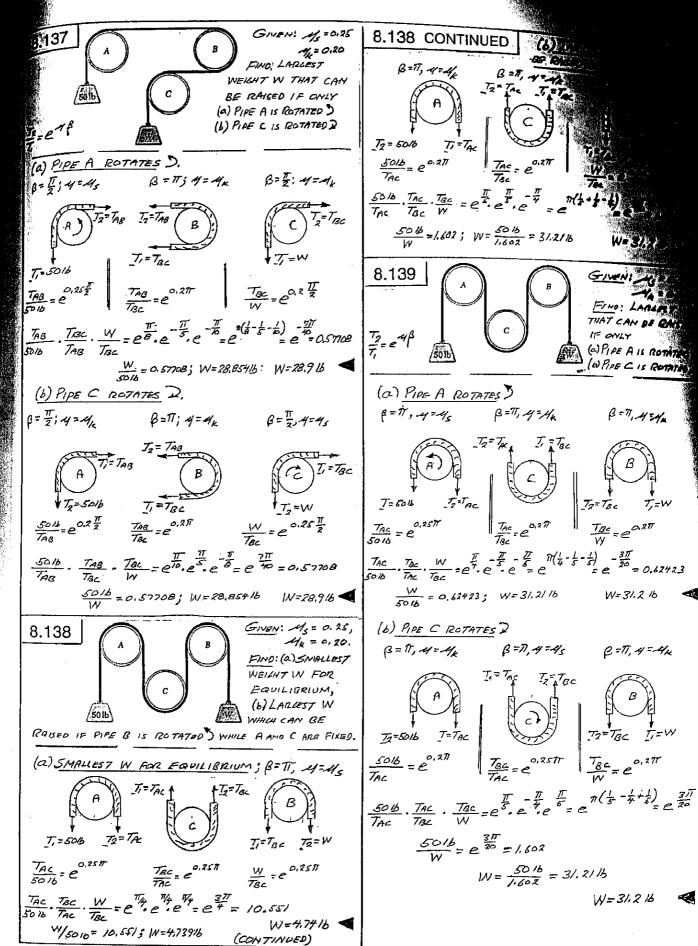
B=# 3 4=42 B=11; 4=40

TETAS TETAS

Tz=5016

5016 = 0.85464; W= 5016 W= 58544 = 58,504 16

W=58.51/5



94432 ٠<u>۵</u>۵

°≎53°

45=0.25

JIL IBRIUM THAT

= TBC

B = 7

1/4

- 130

20 SMALLERT

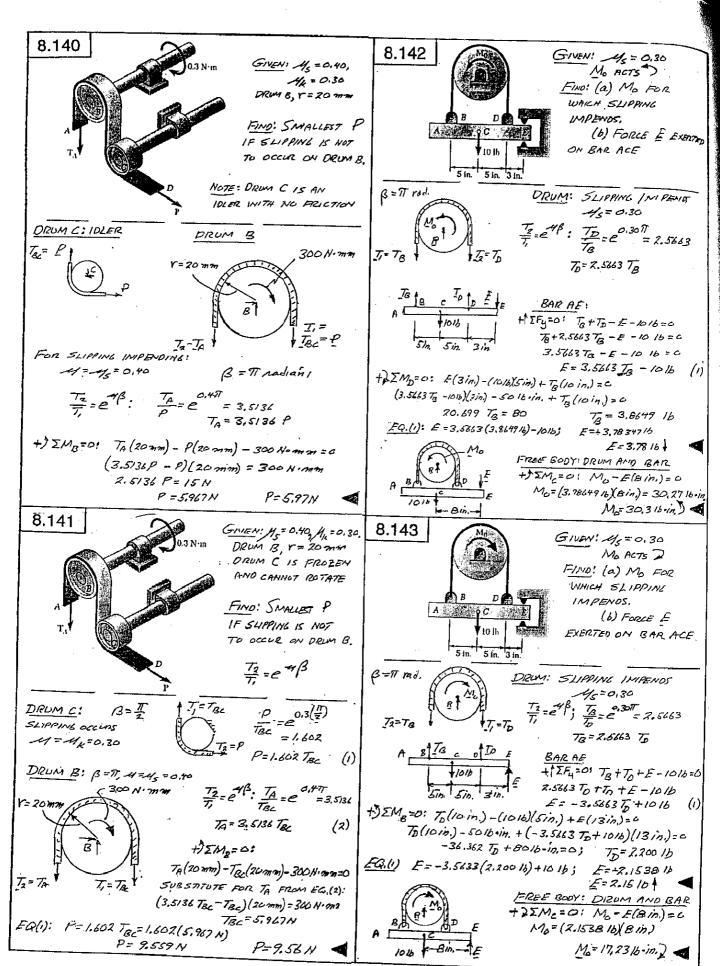
FINO: LANGE THAT CAN DE CAN

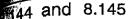
(a) PIPE A IL ROTATI (WPIPE C IS ROTATE

W=31.2 B

B=TT, 4=-4x

I TEC



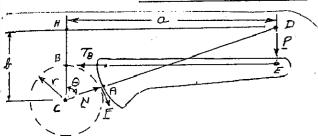




GIVEN: a=200 mm, V=30 mm. ASSUME VALUE OF ME IS THE SAME AT ALL SUBFACES OF CONTACT FIND: SMALLEST VALUE OF MY FOR WHICH THE WRENCH IS SELF-LOCKING IF IN PROB. 8.144 6=65°. O=75° PROB. 8.145

FOR WILENCH TO BE SELF-LOCKING (P=0), THE VALUE OF MY MUST FILEVENT SLIPPING OF STRAY WHICH IS IN CONTACT WITH THE PIPE FROM POINT A TO POINT B AND MUST BE LARGE ENOUGH SO THAT AT POINT A THE STRAP TENSION CAN INCREASE FROM ZERO TO THE MINIMUM TENSION REGUIRED TO DEVELOP "BELT PRICTION" BETWEEN STRAP AND PIPE.

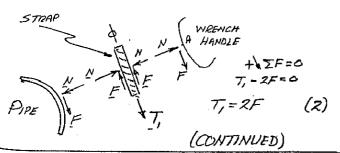
FREE ROOY: WRENCH HANDLE



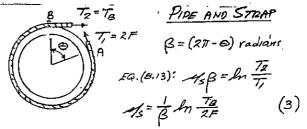
GEOMETRY IN ACDH: CH= a-/tan 6, CD= a/sino DE = BH = CH-BC $AD = CD - CA = \frac{\alpha}{5m\Theta} - r$

ON INDENCH HANDLE +) SMD=0; TB(DE)-F(AD)=0 (I) $\frac{T_B}{F} = \frac{AD}{DF} = \frac{\overline{sin\theta} - r}{a}$

FREE BOOY: STRAP AT PONTA



8.144 and 8.145 CONTINUED



PETURN TO FREE BODY OF WRENCH HAYDLE ± IF.=0: NsinG+FcosO-TR=0 N sino = TB - cos 0 SINCE FEMS N, WE HAVE 1 sina = TB - cos 6 (4)

NOTE: FOR A GIVEN SET OF DATA, WE SEEK THE LARGER OF THE VALUES OF MS FROM EQS. (3) AND (4)

PROB. 8.144: a = 200mm, r=30mm, 0=65 - 51h 65° - 30 mm = 190.676 mm = 3,014/

B = 211-0=211-65-1100= 5.1487 radiais

EQ(3): 4/5 = 1/487 rad Pm 3.014 = 0.41015 = 0.0797

FO(4): $-4s = \frac{\sin 65^{\circ}}{3.0141 - \cos 65^{\circ}} = \frac{0.90631}{2.1575} = 0.3497$

WE CHOOSE THE LARGER VALUE: ME = 0,350

PROB. 8.145: a=200 mm, r=30 mm, B=75°

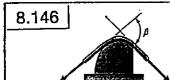
200mm - 30mm 23,570mm

B=211-0=211-75 75 = 49742

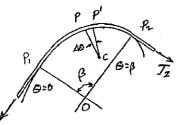
L=Q.(3): 45= 1 1 1,5056 = 1.3225 = 0.2659

Eq.(4): $M_S = \frac{\sin 75^\circ}{7.5086 - \cos 75^\circ} = \frac{0.96953}{7.2468} = 0./333$

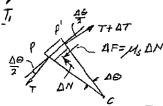
VVE CHOOSE THE LARGER VALUE: 1/5=0.266



PROVE THAT EQS. (8.13) AND (8.14) ARE VALID FOR ANY SHAPE SURFACE



NOTE B IS THE ANGLE BETWEEN BOTH TANGENTS AT P. +P. AND NORMALS AT P, +Pa,



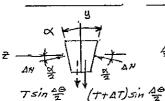
NEXT, NOTE THAT THE DERIVATION OF

ON PAGES 436 AND 437 DIO NOT DEPEND ON THE RADIUS OF CURVATURE BEING CONSTANT, THEREFORE THIS EQUATION MIAY BE OBTAINED FROM THE FREE-BODY DIAGRAM SHOWN HERE.

INTEGRATING EGG) IN @ FROM O TO B AND IN T FROM T, TO TZ, WE OBTAIN AGAIN

8.147

COMPLETE DERIVATION OF EQ.8.15



ZANSmg

SOLVE (1) FOR DAY AND SUBSTITUTE IN (2):

ATCOS AG Sing - Ms (2T+AT) sin AG=0

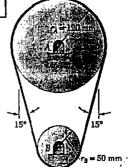
DIVIDE ALL TERMS BY AG: $\frac{\Delta T}{\Delta G} \cos \frac{\Delta C}{2} \sin \frac{\omega}{2} - 4 \left(T + \frac{\Delta T}{2}\right) \frac{\sin \frac{\Delta D}{2}}{4C} = 0$

LET AG APPROACH PERO

INTEGRATE IN & FROM O TO B AND IN T FROM

$$\ln \frac{T_2}{T_1} = \frac{u_s \beta}{\sin u_2} \text{ or, } \frac{T_2}{T_1} = e^{u_s \beta} \int_{s \ln u_2}^{\infty}$$

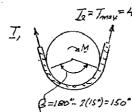
8.148



GIVEN: Mg = 0,40 Tmax= 450 N V-BELT WITH X=34

FIND: LARGEST COUNT THAT CAN BE EXERTED ON PULLEY

SINCE B IS SMALLER FOR PULLEY B, THE BELT WILL EUP FIRST AT B.

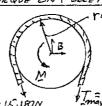


$$\beta = 156^{\circ} \left(\frac{\pi \text{ rad}}{180^{\circ}} \right) = \frac{5}{6} \pi \text{ rad},$$

$$\frac{T_2}{T_1} = e^{-45\frac{\beta}{5}} \frac{51n}{5} \frac{45}{5} \frac{1}{10} \frac{18^{\circ}}{10} = e^{3,389},$$

$$\frac{450N}{T_1} = 29.63; \quad T_1 = 15.187N$$

TORQUE ON PULLEY A



+) IMB=0 M-(Tmax-T,)(0.12m)=0 M-(450N-15.187N)(0.12m)=6 M=52.18 N.m M= 52.2 N.m

Tmay 450N T,= 15.187N

8.149

240 mm

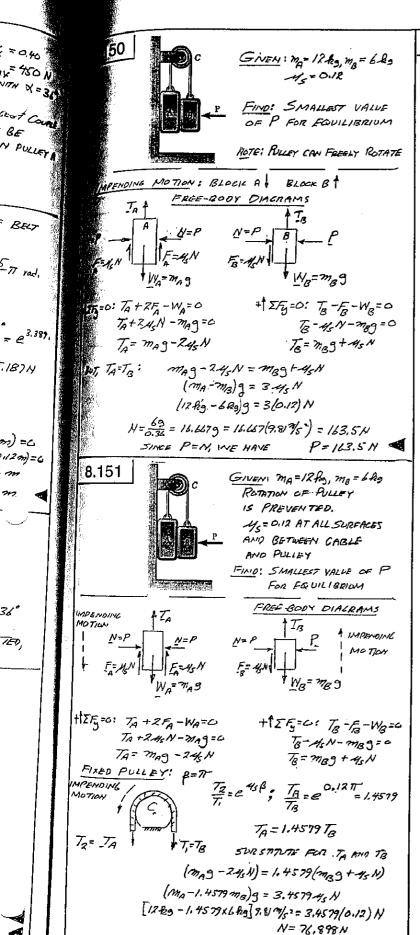
GIVEN: 60-mm-RADIUS V-RELT PULLEYS WITH X = 36 P= 900 N, 45=0.35 FIND: LARGEST TORGUE WHICH CAN BE TRANSMITTED, MAXIMUM TENSION IN V-BELT

B=11 rad PULLEY A: P= 900N

T2= 35.1 T

1 SE =0: TI+T2 + 900 N=C T, +35.1 T, -900N=0 T, = 24,93 N; T Ta = 86,1(24,93 N)= 875.03 N +) IMA=0 M-T2(0,06m)+T,(0,06m)=0 M-(875,03N/0,06m)+(24,93N/0,06m)=0 . M = 51.0 N.m

Tmx= 875 N Tmax = T2



SINCE P=N, WE HAVE

= 0,40

BE A PULLEY

BELT

-77 rad,

= e 3.387.

.187N

>n) =८

217

36°

120,

11200)=6

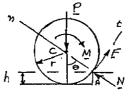
1× 550 N

8.152



GIVEN: As=0.90, 12-in - RADIUS WHERE 60% OF WEIGHT 15 ON FRONT WHERES.

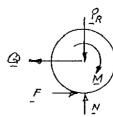
FINO: LARGEST & FOR AUTO TO CLIMB CURB (a) FRONT-WHEEL DRIVE, (b) REAR-WHEEL DRIVE



(a) FRONT-WHEEL DRIVE ONE FRONT WHEEL: Y = 12in. t/ SF,=0: F-Psin 0 =0 * IF = OI N-PCOSE = CO SLIDING IMPENDS: 45 F = Psing = tan 0

tan 6=45=0,90; 0=41,987 h=r-rcos0=r(1-cos6)=(12in.)(1-cos 41.987) h= 3,0805 in.

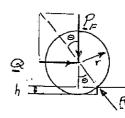
(b) REAR WHEEL DRIVE EACH REAR WHEE CARRIES O. ZW AND EACH FRONT WHEEL CARRIES O.3W. LET Q BE FORCE EXERTED BY CHASSIS ON EACH WHEEL



FREE BODY: NEAR WHEEL Po= O.ZW

+1 ZFy=0: N-0.2W=0 N=0,2W F=F=45N=0,90(0.2W) F=0.18W

±Σ=0: F-Q=0 Q=F=0,18W



FREE BODY: FRONT WHELE P==0,3W r= 12 in.

FRONT WHEEL IS A TWO-FORCE BODY tano= Q = 0.18W = 0.6 G= 30,96°

h=r-rcos 0 = r(1-cos 6) = (12 in,)(1- cos 30,96°) = 1.7101 in h=1.710in.

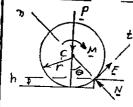
NOTE: COMPARING PROBS 8.152 AND B.153, WE NOTE THAT -FOR FRONT WHEEL DRIVE THE RESULT IS INDEPENDENT OF WEIGHT DISTRIBUTION FUR REAR-WHEEL DRIVE THE HEAVIER THE LOAD ON THE REAR WHEELS, THE LARGER THE CURB HEIGHT H WILL BE

P=76.9 N



GIVEN! 1/5=0.90, 12-in - RADIUS INNERES FOUAL INDIGHT ON

FIND: LARGEST h FOR AUTO CLIMB CURB (a) I-RONT-WHEEL DRIVE, (b) REAR-WHEEL DRIVE



(a) FRONT-WHEEL ORIVE ONE FRONT WHEEL Y=1214 +/ EF=01 F-PsinG=0 Y IF = 0: N-PCOS 6 = C SLIPPING IMPENDS:

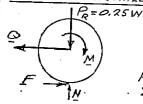
Ms= F = Psine = Land

ton 6 = 4, =0,90; 6 = 41,987"

h=r-rcos = y(1-cos 6)=(12in)(1-cos 41.9870) h=3,0805in. h=3.08 in.

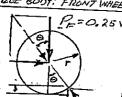
(6) REAR WHEEL DRIVE

FREE BOOY! REAR WHEEL



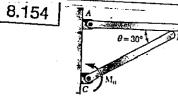
LET Q BE FORCE EXERTED BY CHASSIS ON EACH WHEEL + TFy=0: N-0.25W=0 N=0.25W F=195N=0.90(0,25W)=0.225W Σ/z=c: Q = 0.225W

FREE BODY: FRONT WHEEL P==0.25W



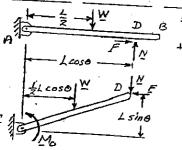
r=12% TWO-FORCE BODY tanb= = = 0.226W = 0.9 G=41.987° h=r-reos0= r(1-cos6) h=(12in)(1-cos 41.987°)=3.0866in

h= 3.08 in. (SEE NOTE AT END OF SOLUTION OF PROB 8.152



GIVEN! EACH ROD IS OF LENGTH L AND WEIGHT W. 1/5=0.46

FIND: RANGE OF VALUES OF ME FOR EQUILIBRIUM



FOR IMPENDING CLOCKWISE MOTTON 4) [Mp=0

N(LCOS 0) - W(=)=0 N=W

1==415N= = 7500

+) IM=0: Mo-W(1/2 LOSS) - W/20050 (LOSS) + MSW/20050 (LSINE)=0 Mo= 1 WL (cose +1 - 45 tang)

Mo= 1 INL (cos 30°+1-0, 40 tan 30°)

MG= 0.81754 WK

Mo=0,818WL V (CONTINUED)

8.154 CONTINUED

FOR IMPENDING COUNTERCLOCKWISE

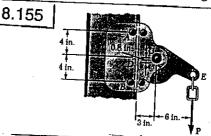
MOTION OF THE ROOS, INE CHANGE THE SIGN OF MS IN EQUI).

-- Mo = 1 WL (COSO + 1 + 45 tand) = 12WL(cos 30° +1 +0.40 tan 30°)

Mo=1.0484WL Mo=1,048WL

RANGE OF MO FOR EQUILIBRIUM!

0.818 WL < MO < 1.048 WL



FIND: SMALLEST A. BETWEEN RAIL AND CAM AND BETWEEN RAIL AND PINS FOR EQUILIBRIUM

Α£y 0.8% ⅓ F=MsND 310. bin.

FREE BOOY: CAM +) \(\SM_c = 0; No(0.8in)-45 No(3in)-P(6in)00

FREE BODYISLEEVE AND CAM \$ 2Fx=0: ND-NA-N8=0 4in. NATNG = ND رج/

HΣFy=0: FA+FB+FB-P=0 OR US(NA+NB+NO) = P EUBSTITUTE FROM (2) INTO (3) 45(ZNO)=P ND= 1740

(2)

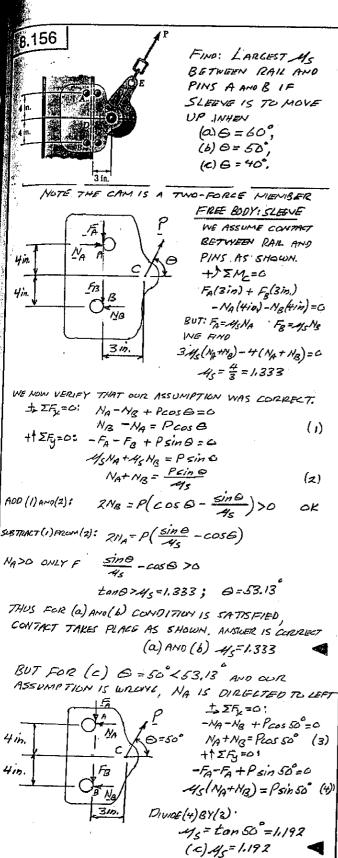
EQUATE EXPRESSIONS FOR MD FROM (1) ANO(4) $\frac{P}{2445} = \frac{6P}{0.8 - 345}$; 0.8 - 345 = 1245-4/c=0.0533

NOTE: TO VERLIEY THAT CONTACT AT PINS A AMO B TAKES PLACE AS ASSUMED WE SHALL CHECK THAT NASO AND NB=0.

From (4): No = + = P = P = 7(0.0533) = 9.375 P

FROM FREE BODY OF CAM AND SLEEVE DEMB=0 NA(Bin) - ND(4in) - P(9in) = 6 ENA =(9.375P)(4)+9P NA= 5.8125P>0 OK

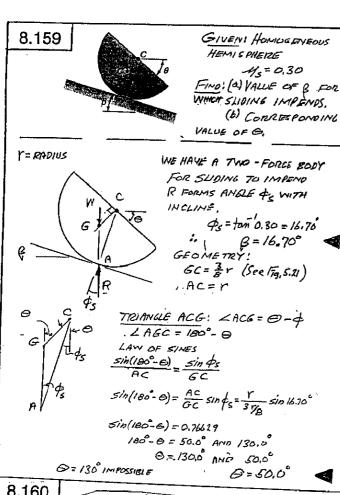
FROM (2): NA+HB=HD 5.8125P+HB=9.375P MB= 3.5625 P>O OK

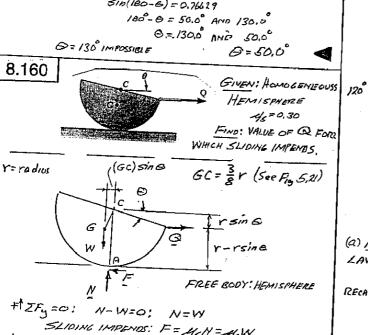


GIVEN! 20-Ry TURE AB, 45=0,30, FIND: LARGEST & FOR TUBE TO SLIDE HORIZONTALLY WHEN (a) a=0, (b) a=0.75m. FOR MAY &, SLIDING AND ROTATION ABOUT C BOTH IMPEND (a) THREE-FORCE BODY FORCE P MOST PASS THROWAN POINT D WHERE IN AND C INTERSECT. SINCE SLIPPING IMPENOS & FORM ANGE &S WITH TUBE \$= tan 4 = tan 0.30 ISOSCELES TRIANGLE Ac = 16.70° = 90 - 45 = 90 - 16,7 @=73.3 +) ZMc=0: (Pcosps) L-W==0 P= 1N/2 cos \$ = (20 &0)(9.81 7/52), P= 102.4 N (6) THREE-FORCE BODY (See ABOUD IN A CDG: DG = 0.75 m = 2,50 m IN AADG: $\frac{1}{\tan \Theta} = \frac{DG}{AG} = \frac{2.5m}{1.5m}$ tana=1,667, 0=59,04° B=59,0° +) IM =0: (P sin B)(2,28m) - W(0,78m)=0 P= 0.333 W= 0.333 (2020)(9,8/Mg) P=76.3 M P= 26,27N 8.158 GIVEN: 45=0,30 20-Rg TUBE AB FINO: (a) SMALLEST P TO MOVE TUBE, (b) WHETHER TUBE SLIDES OR ROTATES. ASSUME SLIDING ZF4 N=W-Psin60 F=45N= 45 (W-PSING) ZFz: Pcos60 = F= M5(W-Psin60) 0.3 W = 0.3948 W COS600 + 45 511600 ASSUME ROTATION ABOUT C - MEG+ B (Psindo)(2.75m)-W(1.25m)=4 NOTE: FOR G >53.13, MS IS INDEPENDENT OF B.
FOR O < 53.13, MS DEPENDS ON O P=0,5249 W 1.25m TUBE SLIDES FOR SLIDING: P=0,3948W=0,3948(20Re)49.817/5) P= 77.5 N

8.157

AND 15 As=tan6





The free booy: Hemison Y = FREE BOOY: HEM

6= 26.39°

$$SING = \frac{Ms}{\frac{3}{8} + Ms} = \frac{0.36}{0.375 + 0.30} = \frac{4}{9}$$

0=26.4°

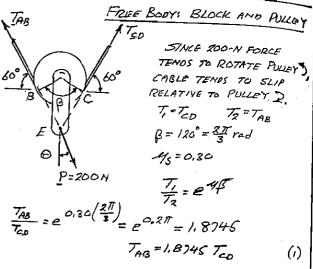
8.161 A

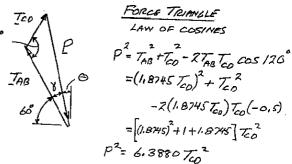
GIVEN: AXLE OF PULLEY IS FROZEN AND CANNOT ROTATE WITH RESPECT TO BLOCK

JS = 0.30

FIND: (a) MAXIMUM VALUE OF & FOR PQUILLERIUM.

(b) REACTIONS AT SUPPORTS A AND D





 $T_{CO} = 0.39585P \qquad (2)$ (a) MAXIMUM ALLOWARLE VALUE OF Θ ; $LAW OF SIMES: \frac{\sin \delta}{T_{CD}} = \frac{\sin 120^{\circ}}{P}; \sin \delta = \frac{T_{CO}}{P} \sin 120^{\circ}$

RECALLING FQ(2): $\sin \theta = \frac{0.39565P}{P} \sin 120 = 0.34264; \quad \xi = 20.04^{\circ}$

 $\sin 8 = \frac{1}{p}$ $\sin 170 = 0.34764; (= 20.04)$ $\Theta = 90^{\circ} - (60^{\circ} + 20.04^{\circ})$ $\Theta = 9.96^{\circ}$

(b) REALTIONS AT A AND D. P=200 NEQ(2): $T_{CD}=0.39565(200N)=79.13 N$

IFG(1) TAB=1.8745 Top=1.8745 (79.134)= 148.33N

THUS A= 148.38 160 = 148,33 N

D= 79.1 N2 60°